

Towards Bidirectional Ratcheted Key Exchange

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RUB

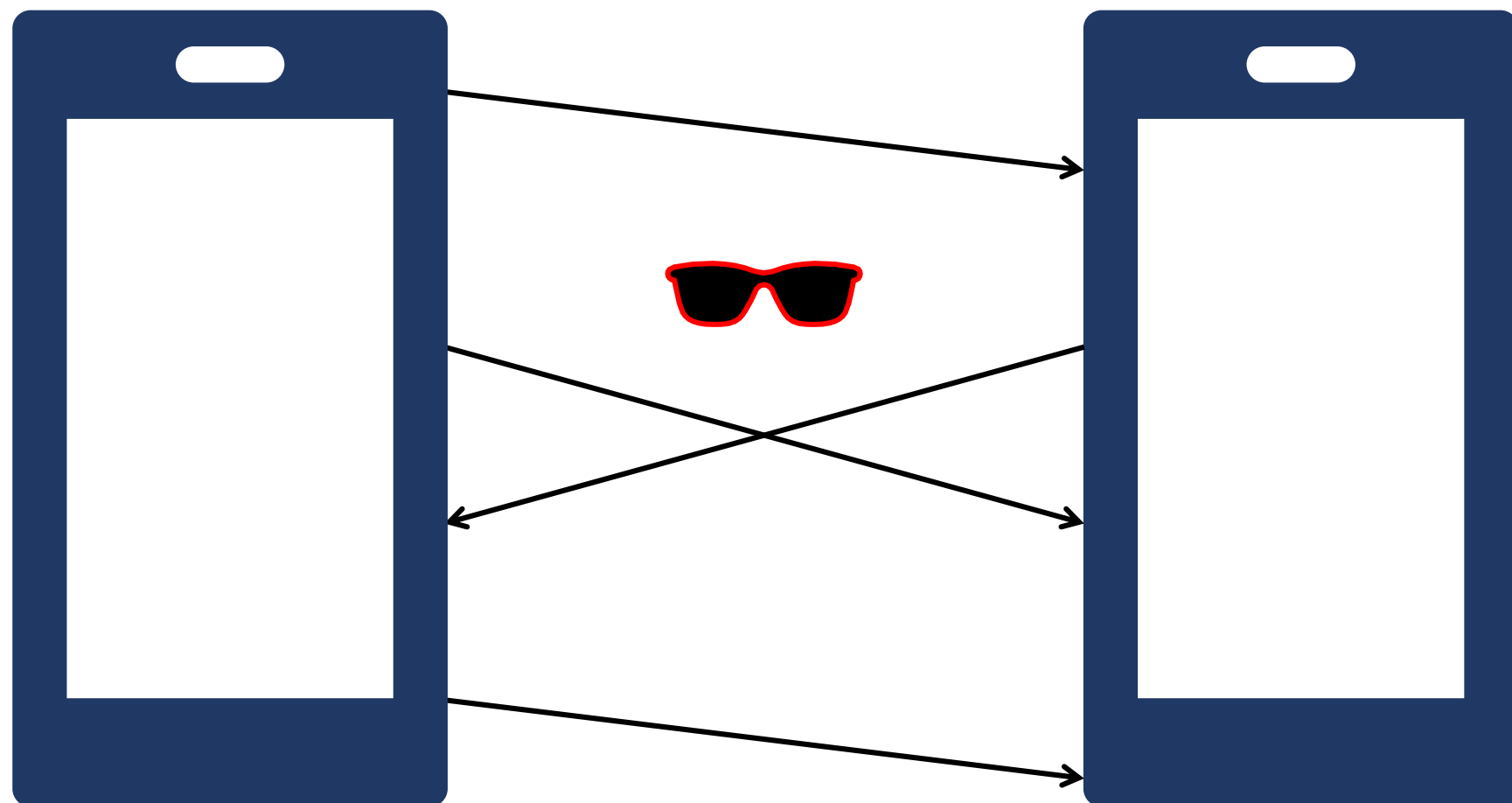


ROYAL
HOLLOWAY
UNIVERSITY
OF LONDON

- What is Ratcheting?
Modeling RKE
Construction Intuition
Results

Introduction

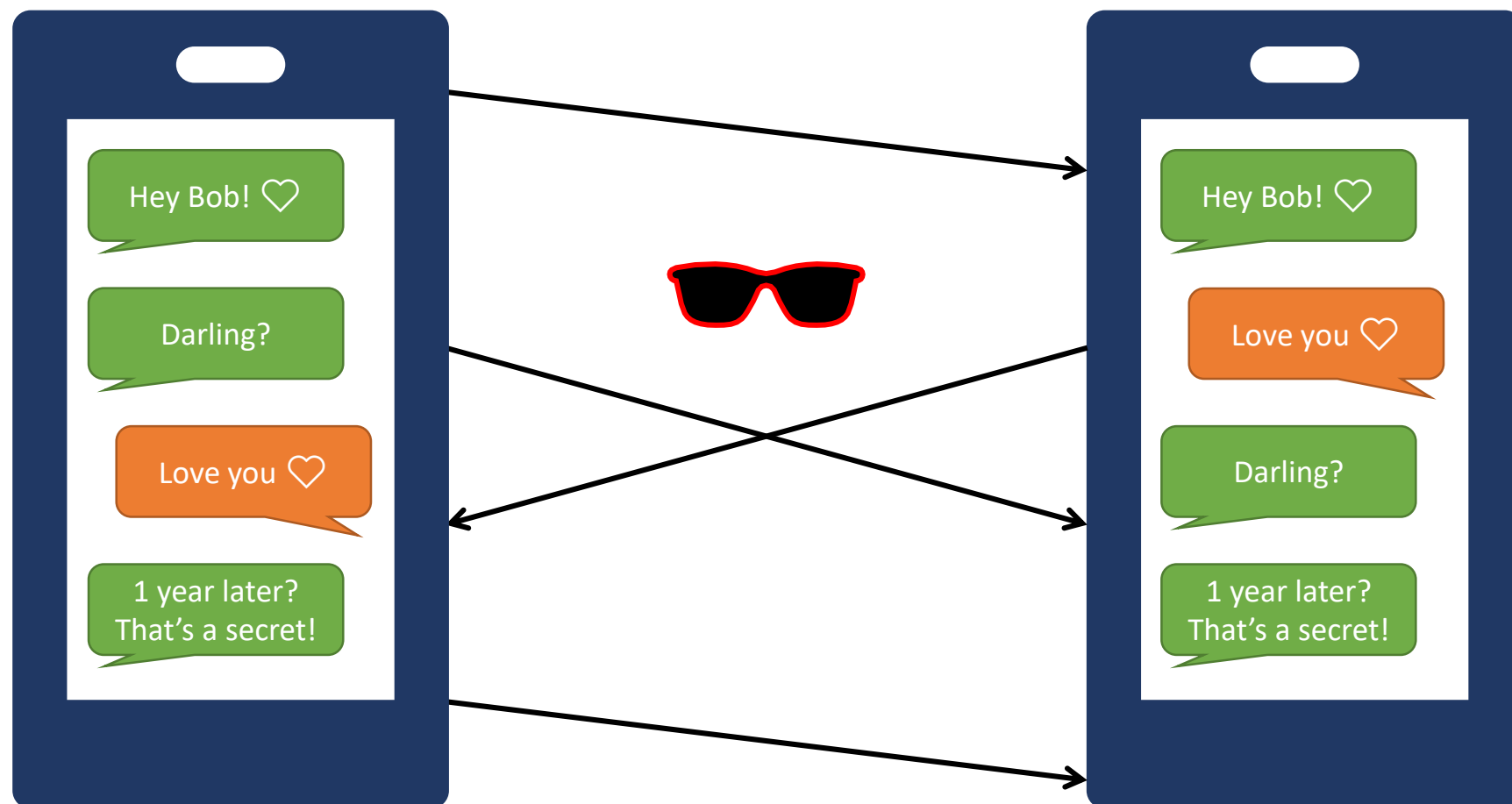
- Alice and Bob communicate
- Active adversary



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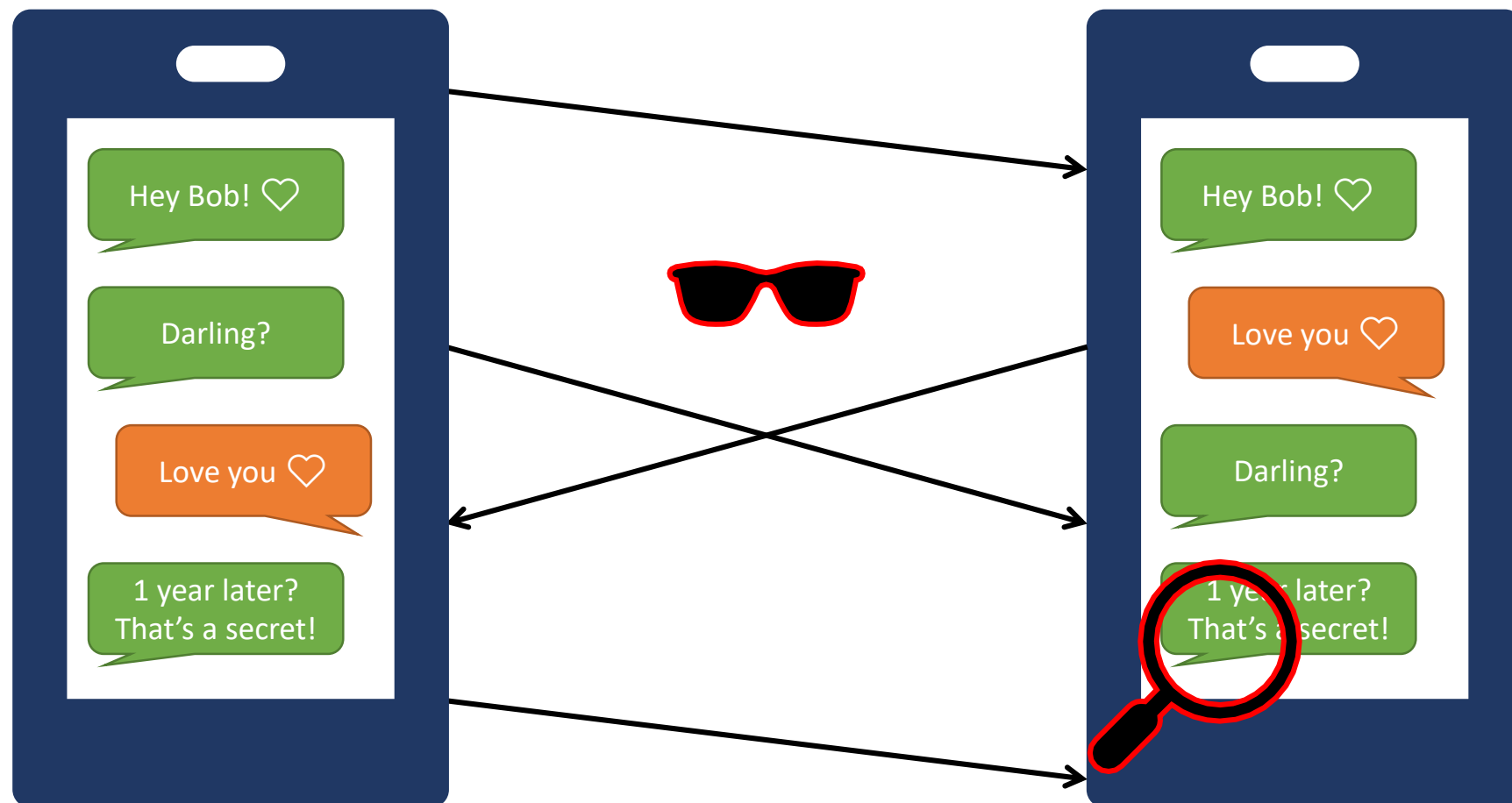
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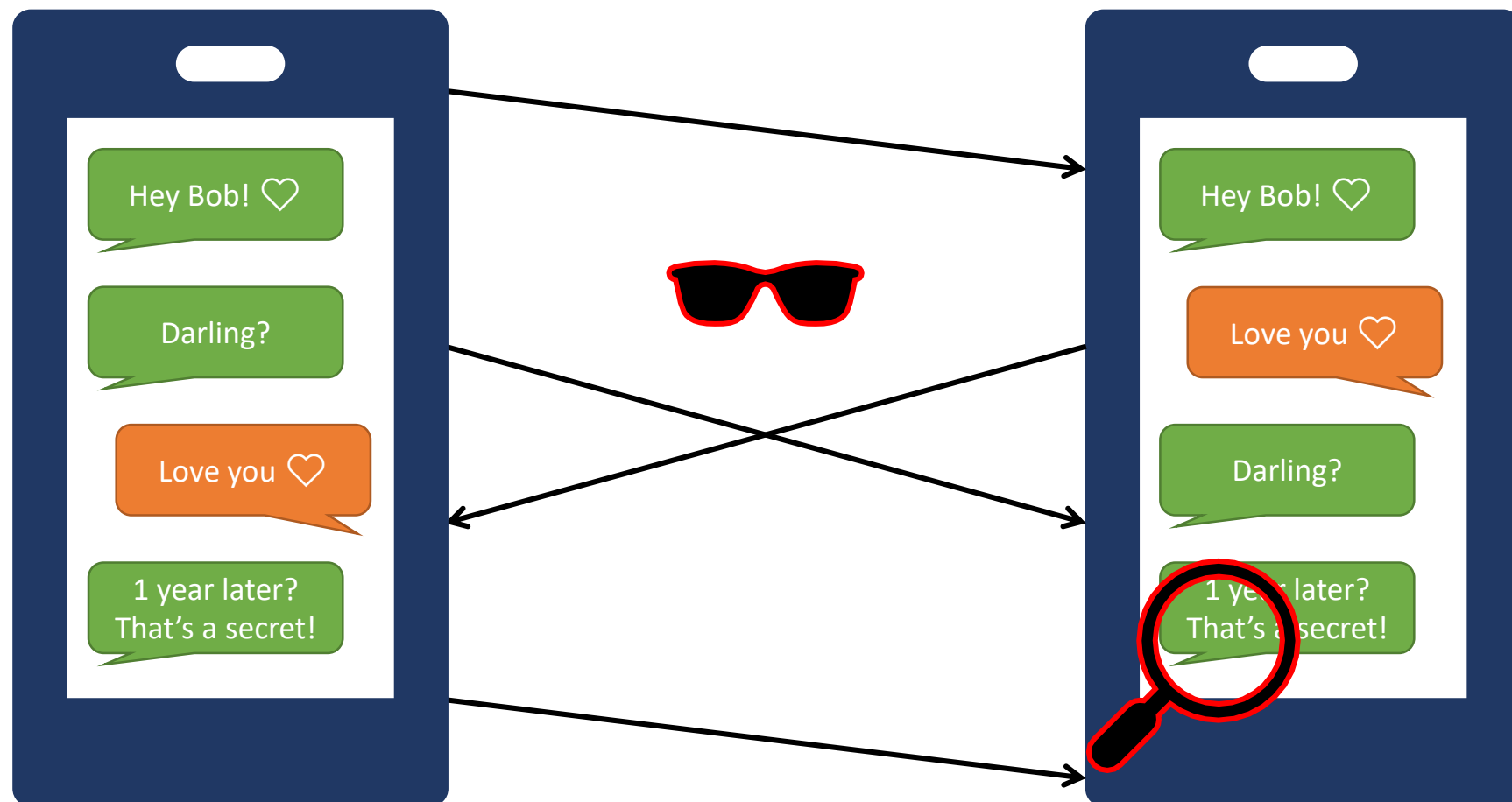
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- Active adversary
- Long term communication
 - Local (full) state temporarily exposed



- What is Ratcheting?
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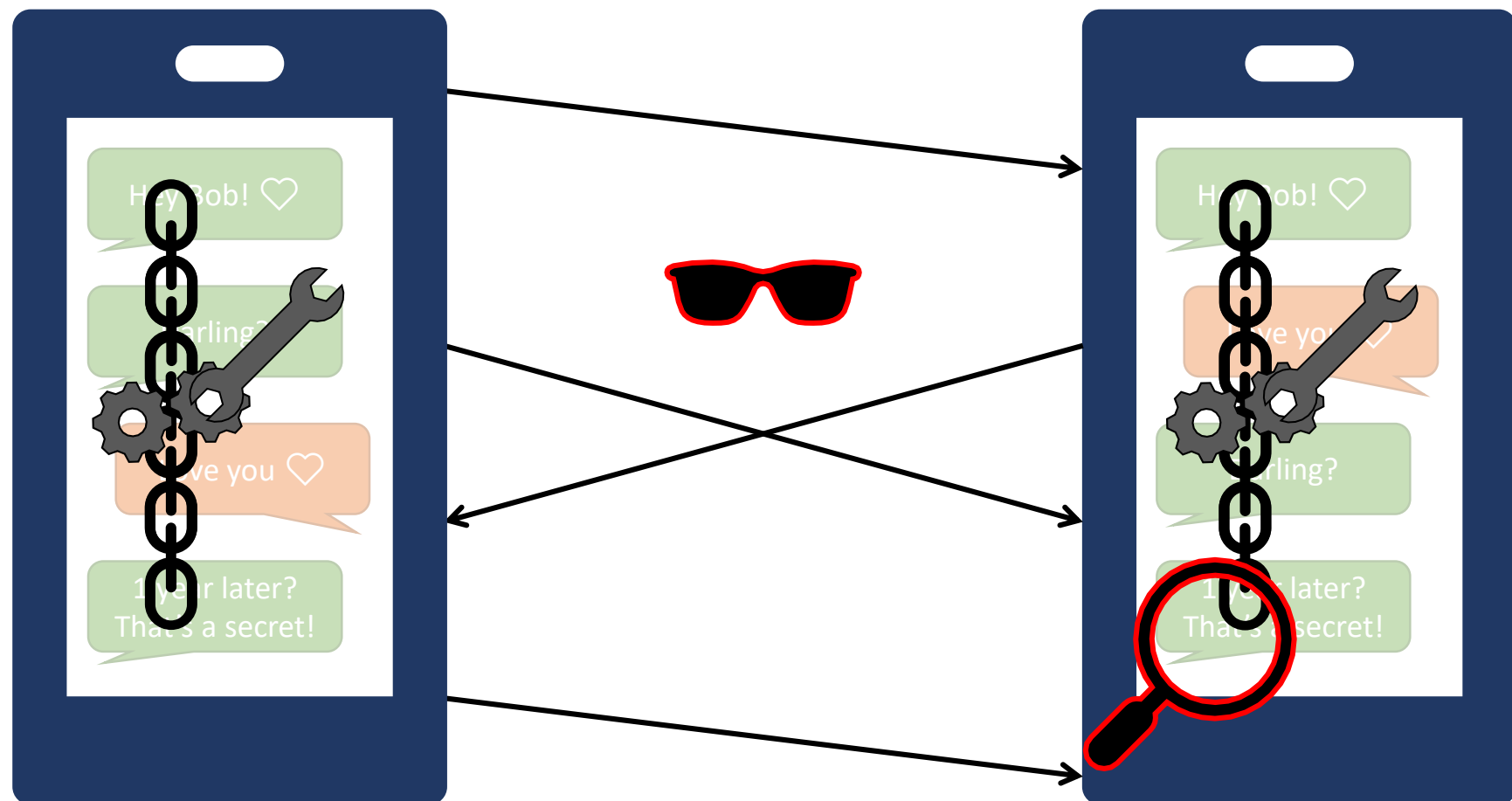
- Alice and Bob communicate
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- Long term communication
 - Local (full) state temporarily exposed
- Practical protocols w/o precise security definition
 - E.g., Signal 



What is Ratcheting?


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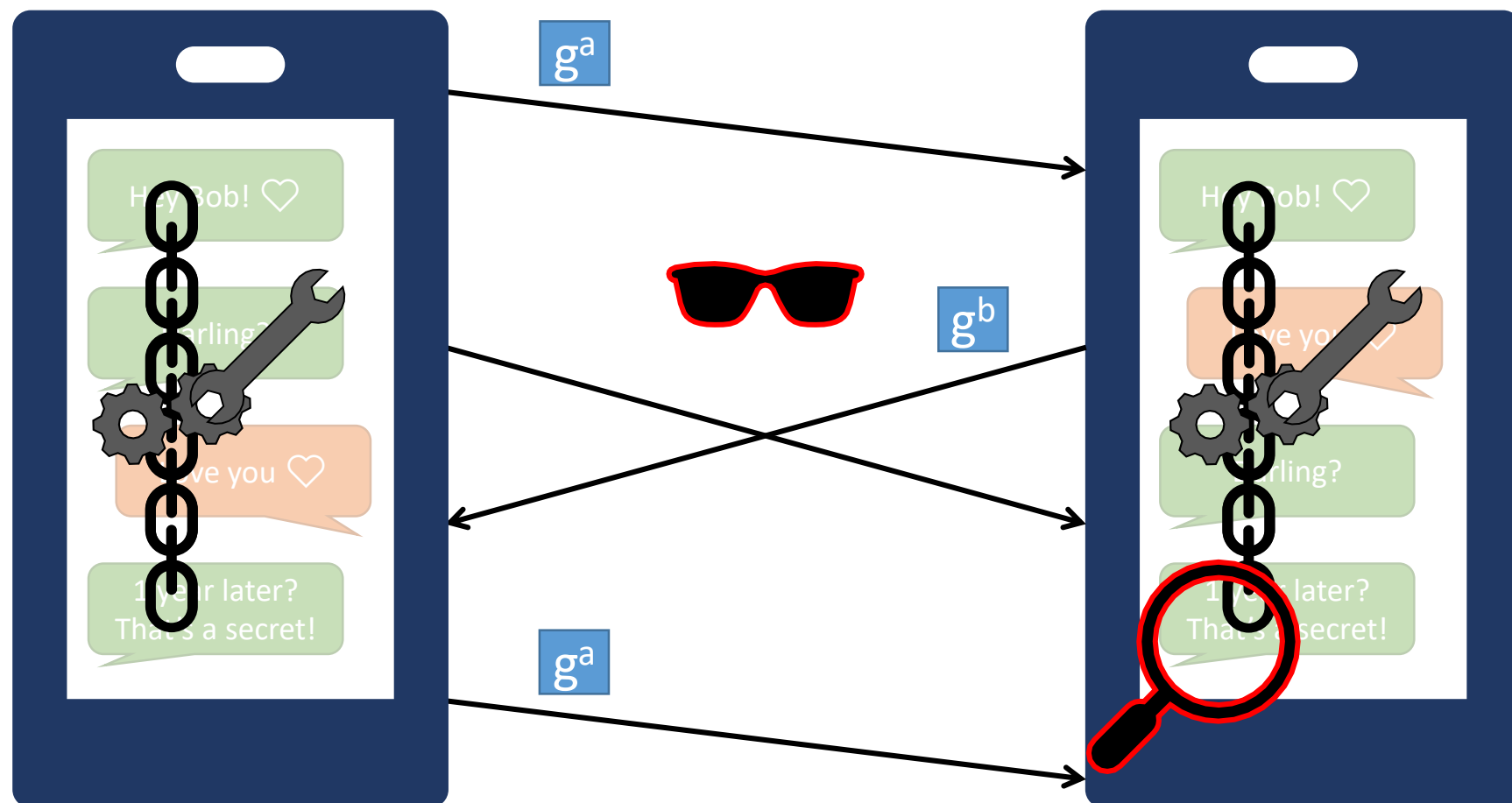
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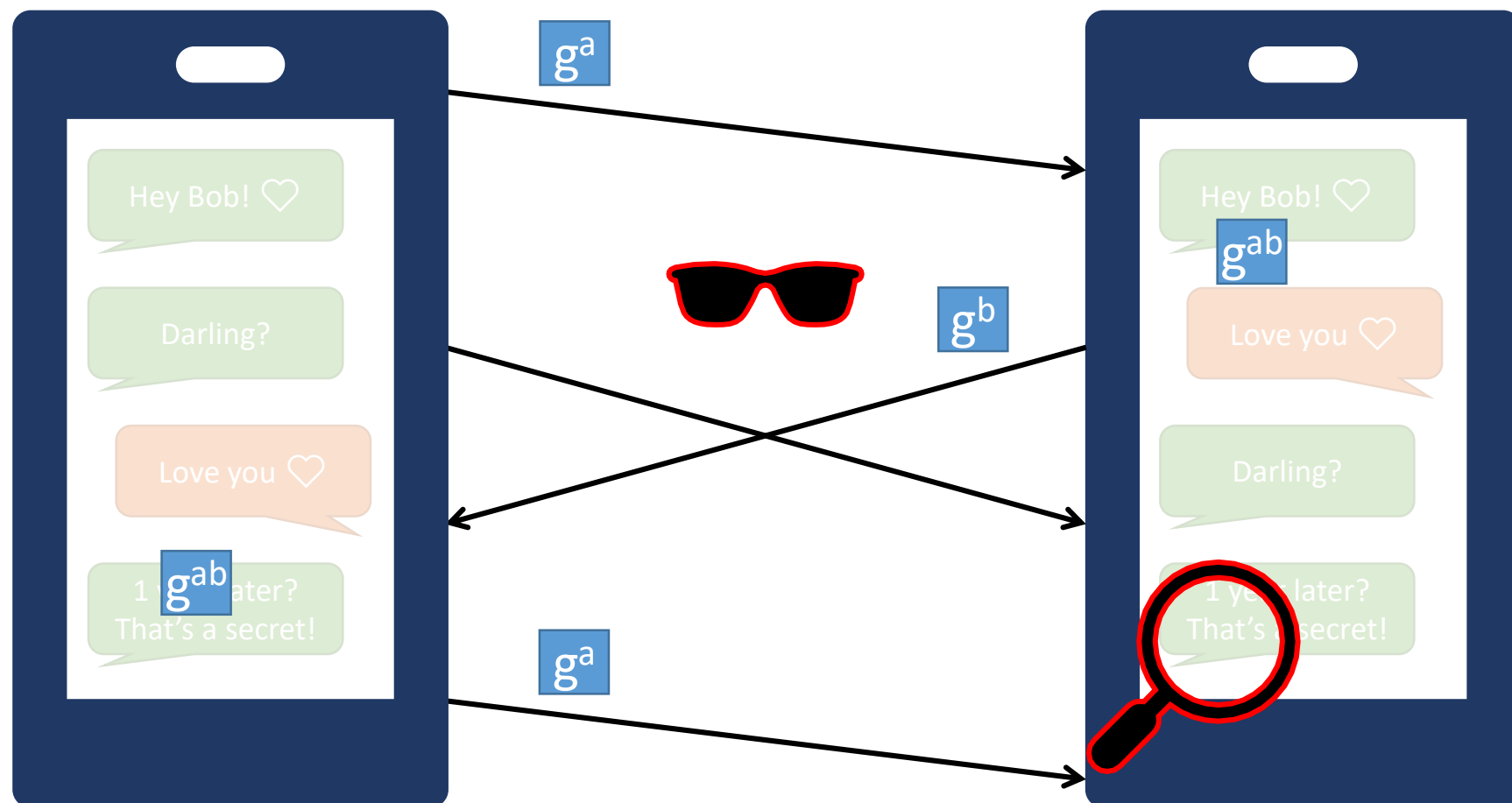
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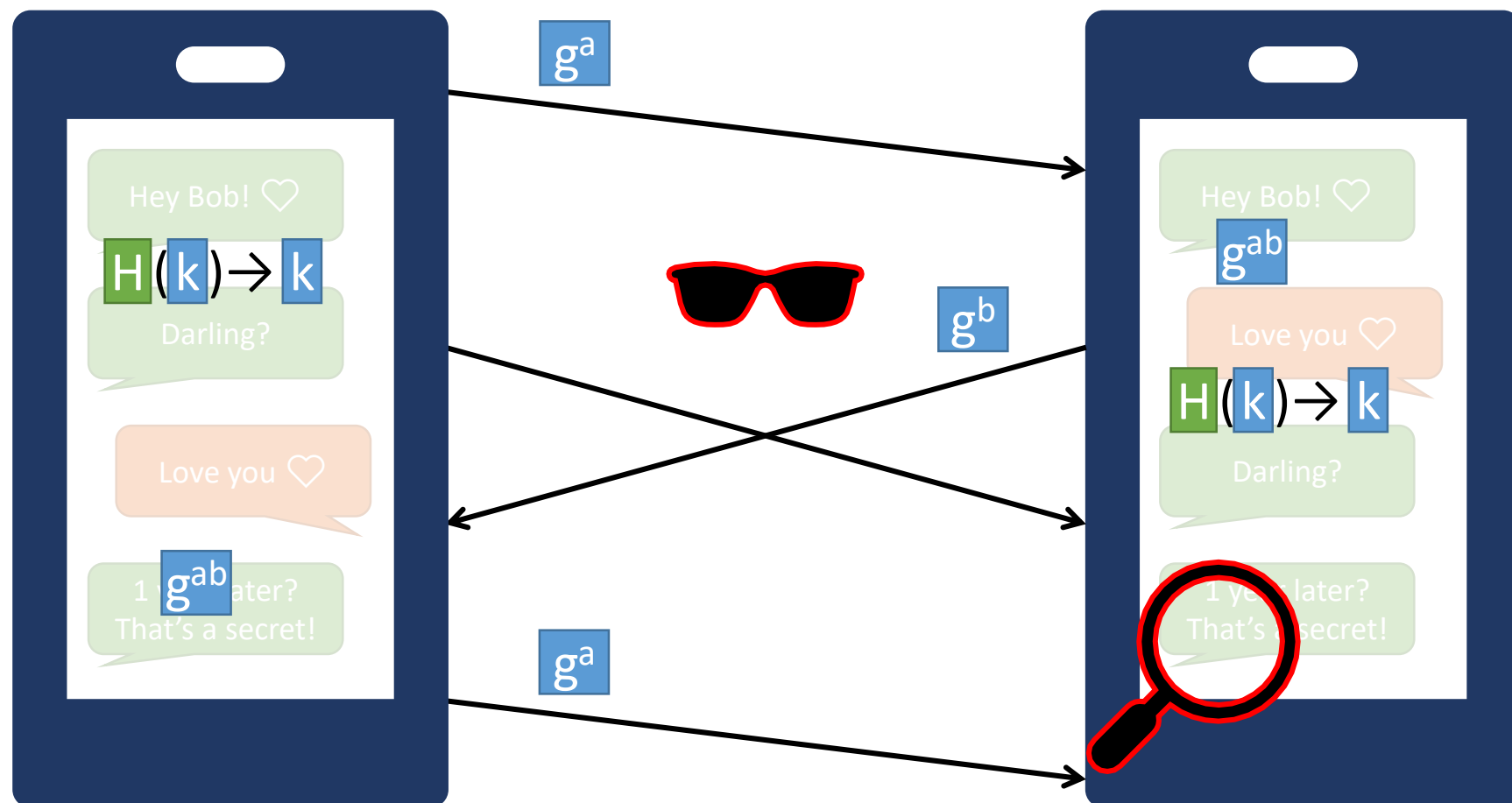
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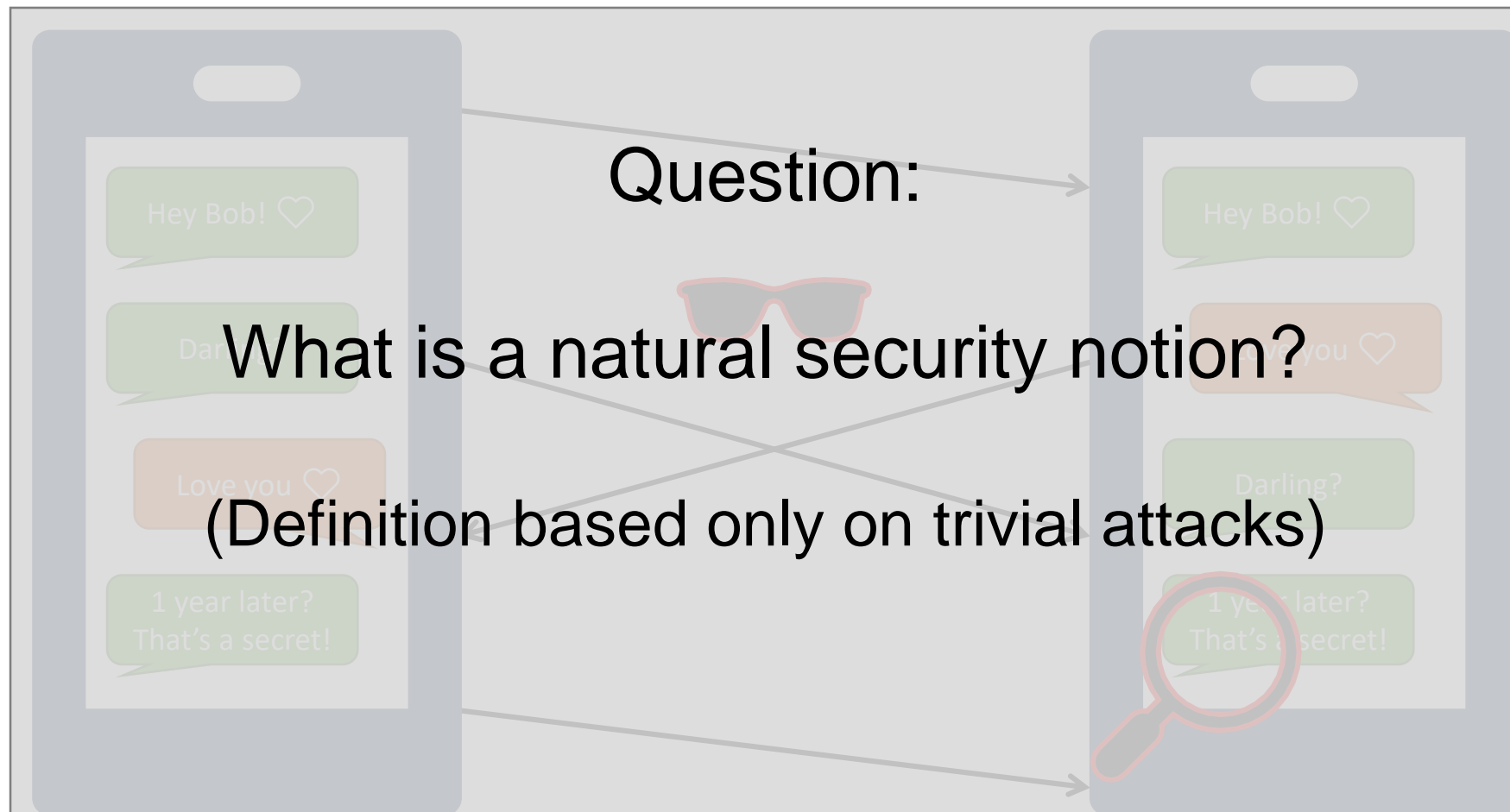
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Natural Security Notion for Ratcheting?

- Alice and Bob communicate
- Active adversary
- Long term communication
 - Local (full) state temporarily exposed

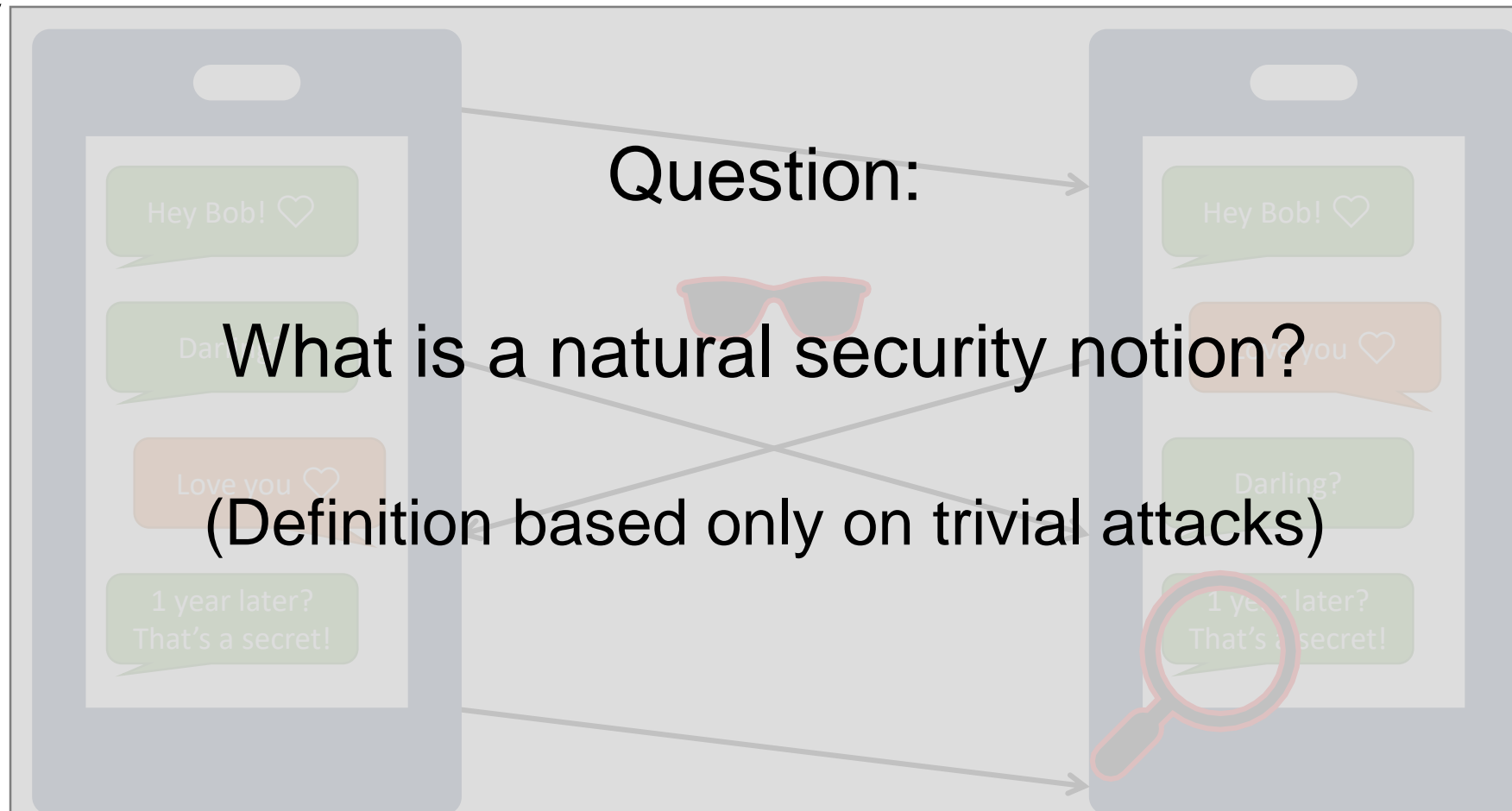


- What is Ratcheting?
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Natural Security Notion for Ratcheting?

- Natural security notion

- Definition based only on trivial attacks
- Bellare et al. on unidirectional communication C'17
 - Bob cannot be exposed



- What is Ratcheting?
Modeling RKE
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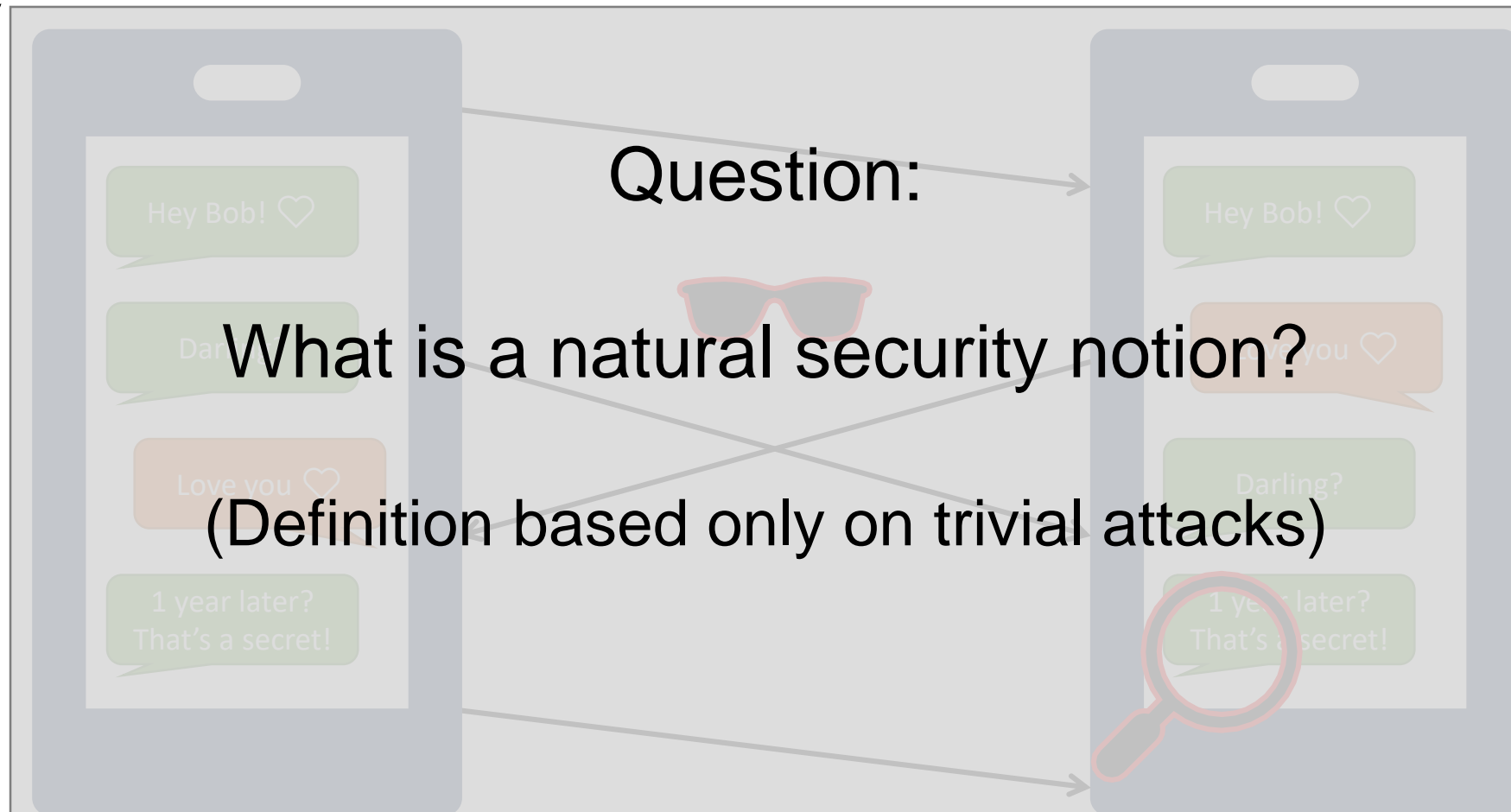
Natural Security Notion for Ratcheting?

- Natural security notion

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 - Bob cannot be exposed

Our models require and constructions provide *full* security under:

- Asynchronous communication
- Exposure of both parties



Agenda

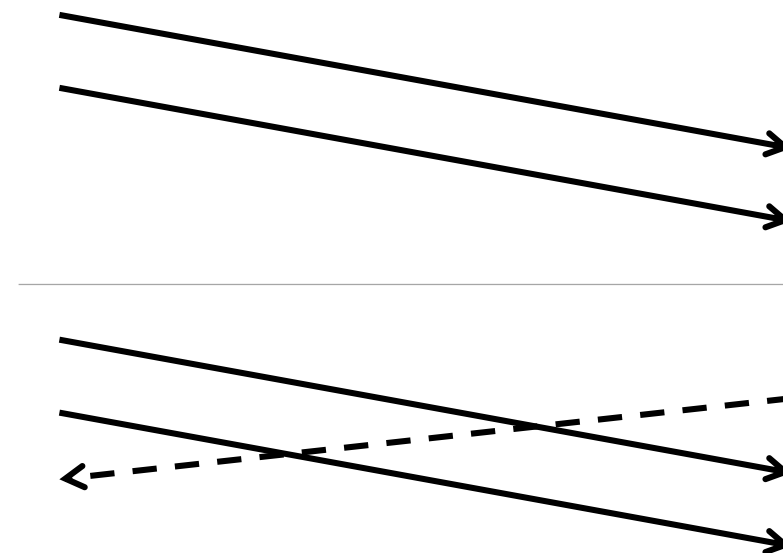
1. The Primitive Ratcheted Key Exchange

2. General Adversary Model

3. Unidirectional Ratcheting → Model and Construction

4. Sesquidirectional Ratcheting → Model and Construction

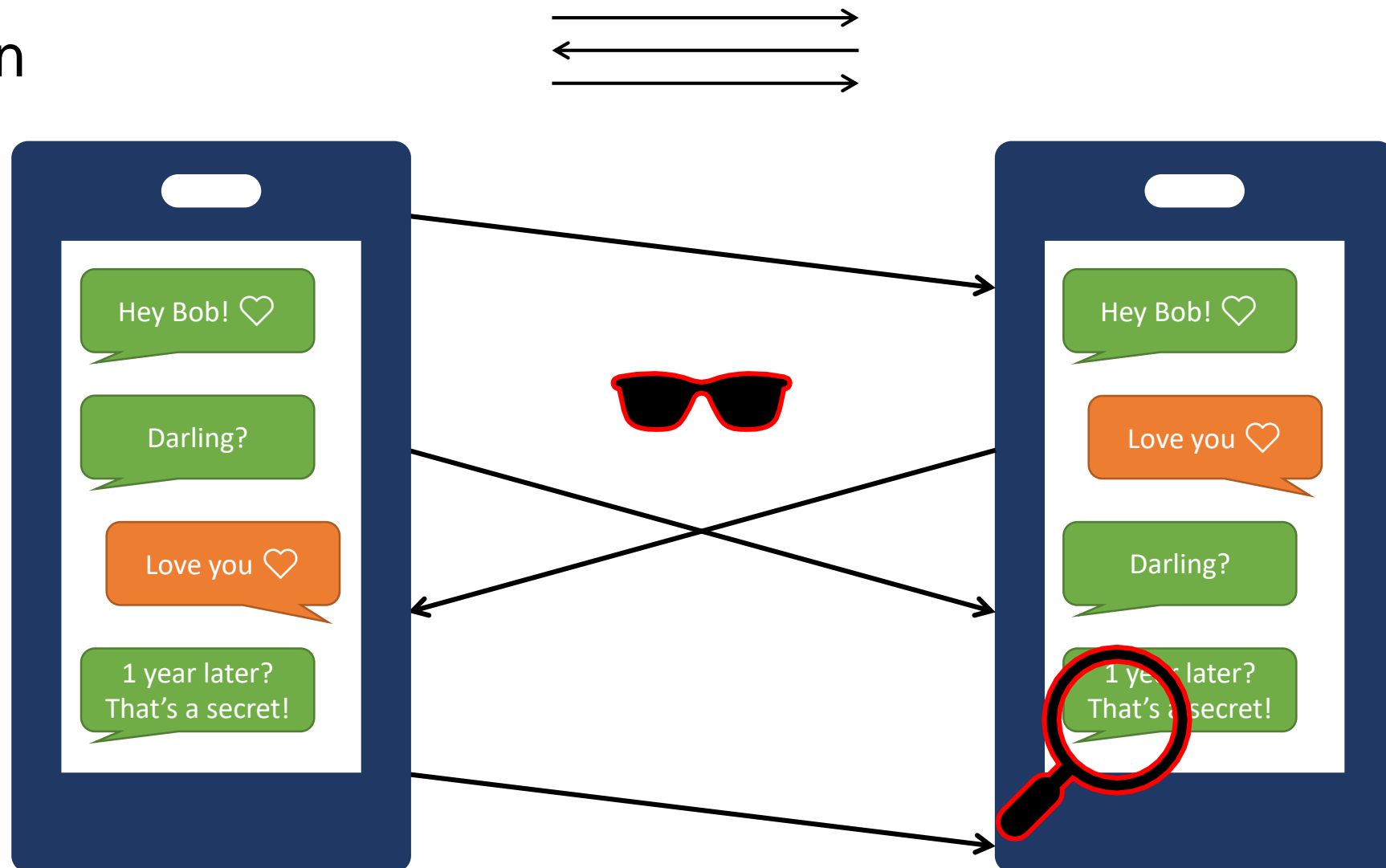
5. Results



- What is Ratcheting?
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Natural Security Notion for Ratcheting?

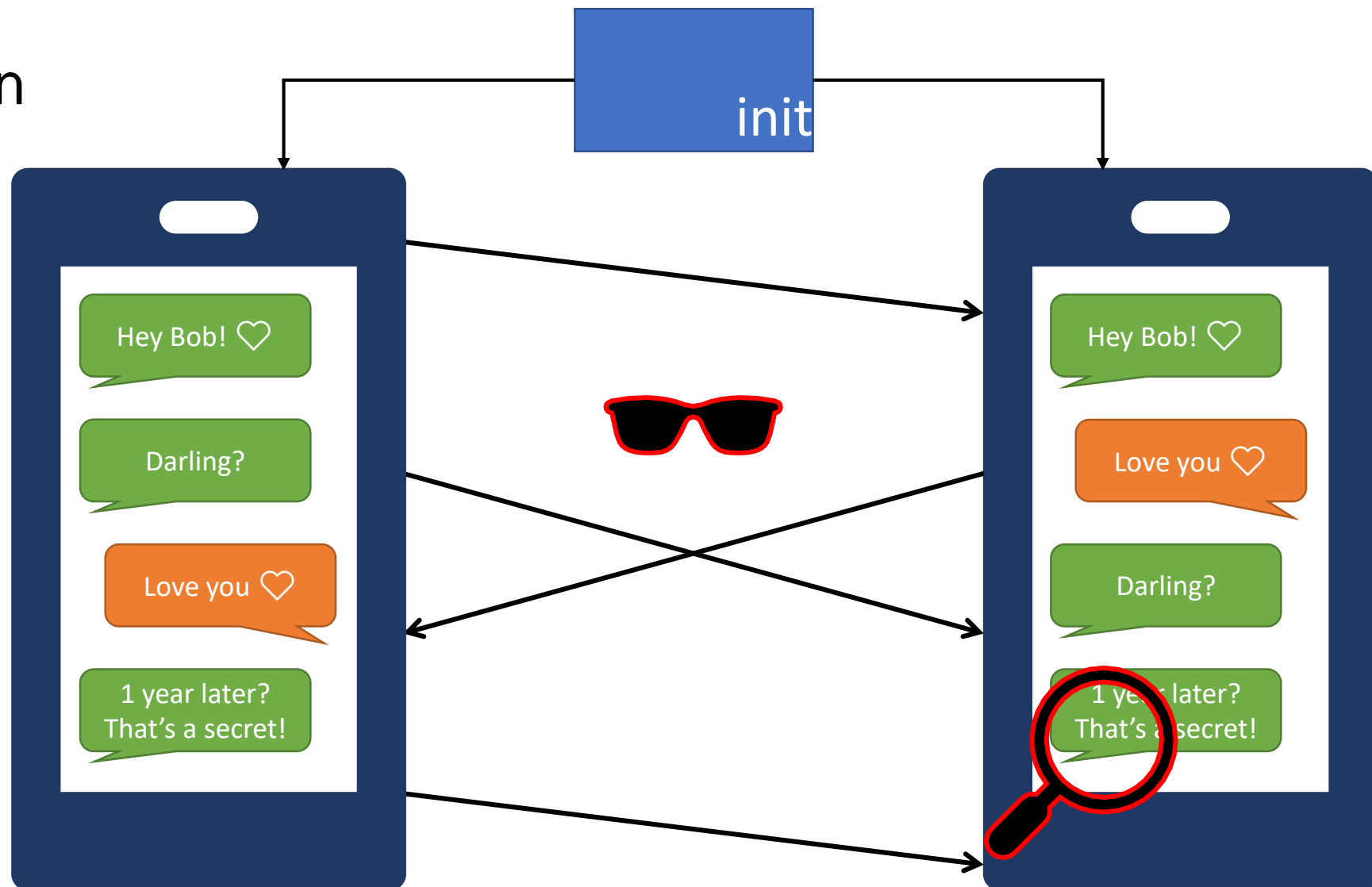
- Natural security notion
 - Definition based only on trivial attacks
- Syntax:
 - Initialization



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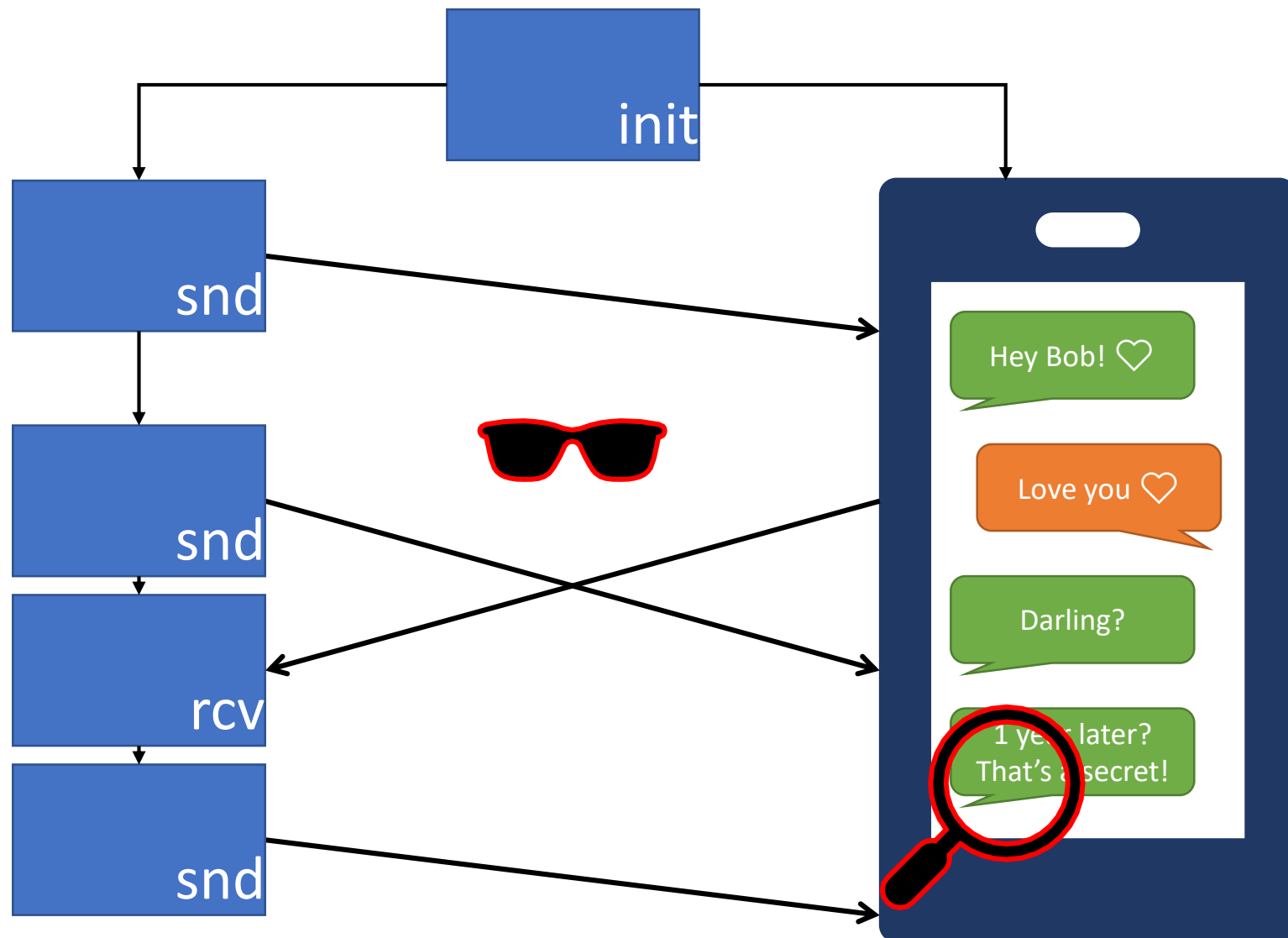
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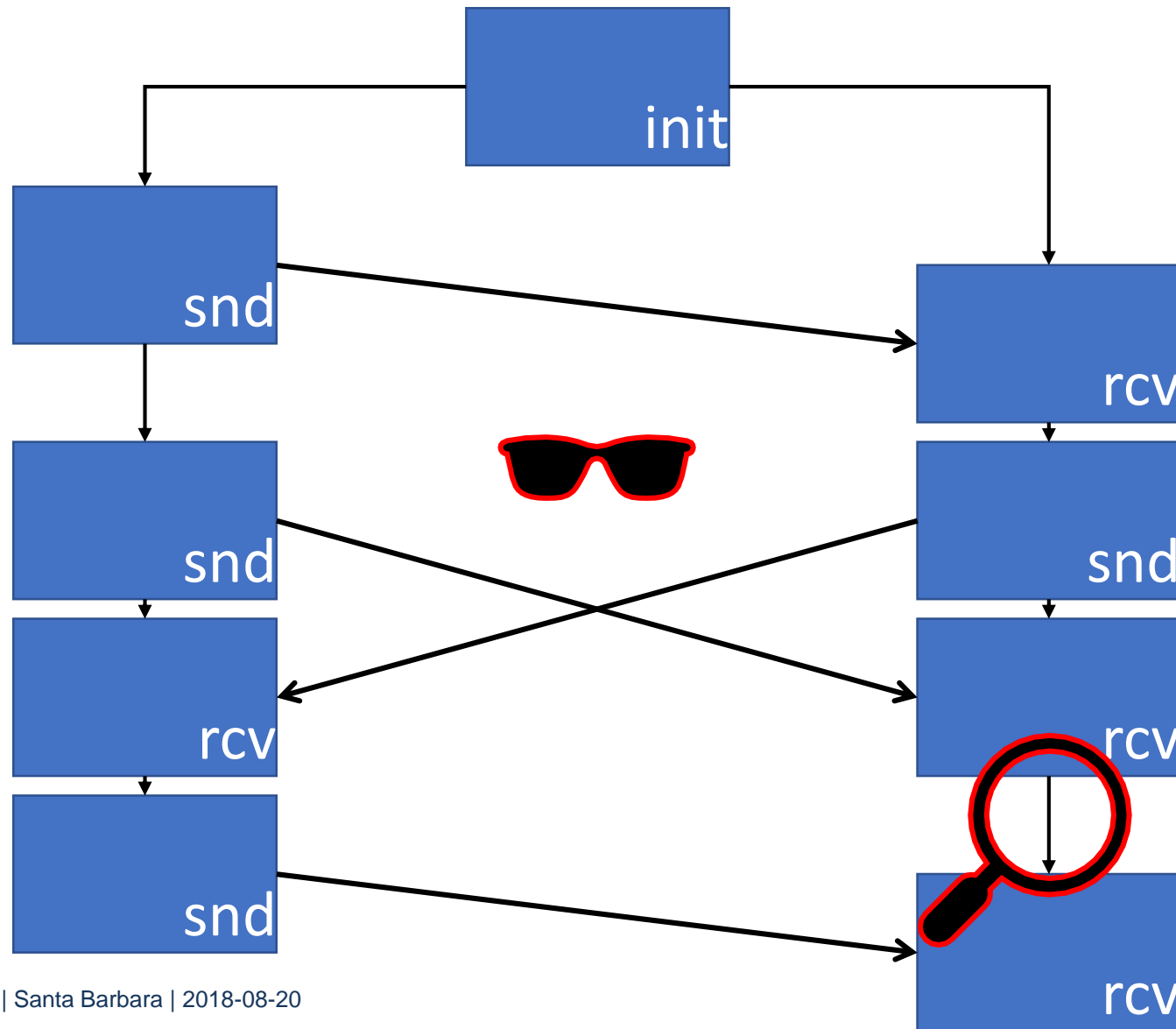
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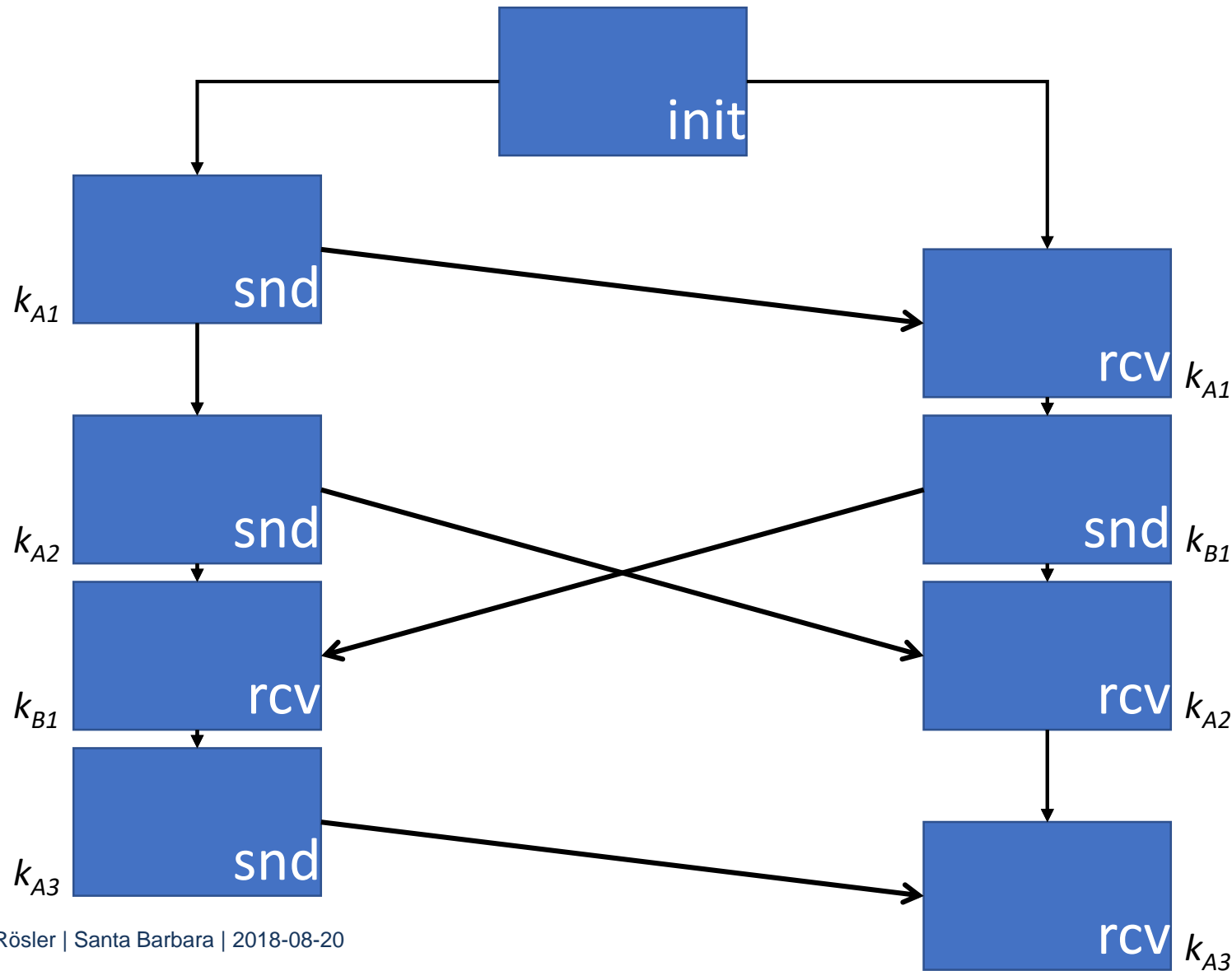
- Natural security notion
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Natural Security Notion for Ratcheting?

- Natural security notion
 - Definition based only on trivial attacks
- Syntax:
 - Initialization
 - Sending & receiving
 - Key exchange
 - Consecutive establishment of keys in session

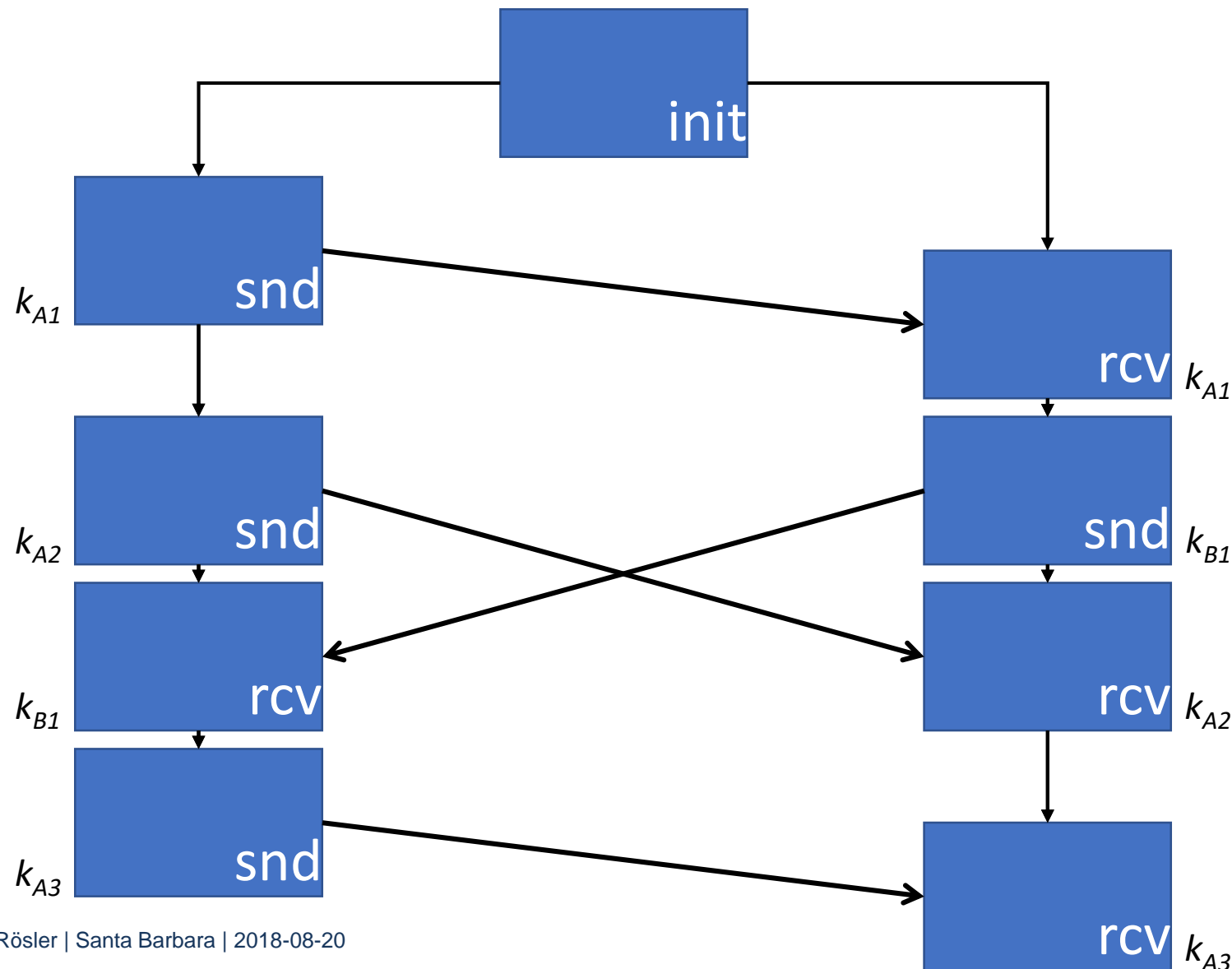
≠ Authenticated key exchange!



Natural Security Notion for Ratcheting?

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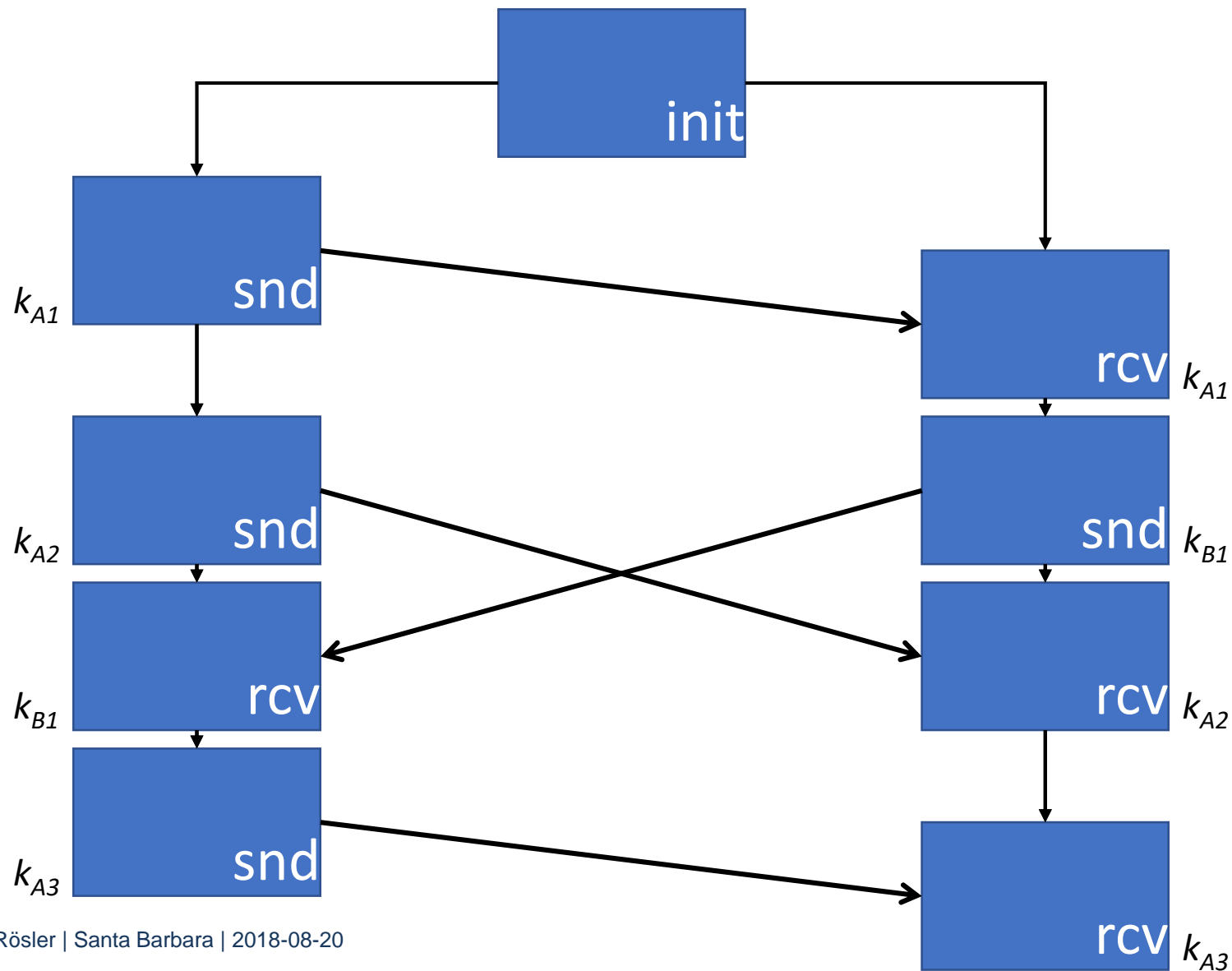
- Natural security notion
 - Definition based only on trivial attacks
- Syntax:
 - Initialization
 - Sending & receiving
 - Key exchange
 - Composition in Bellare et al. C'17



Three Variants of Ratcheting

- What is Ratcheting?
Modeling RKE
Construction Intuition
Results

- Bidirectional ratcheting is complicated
→ Understand its components



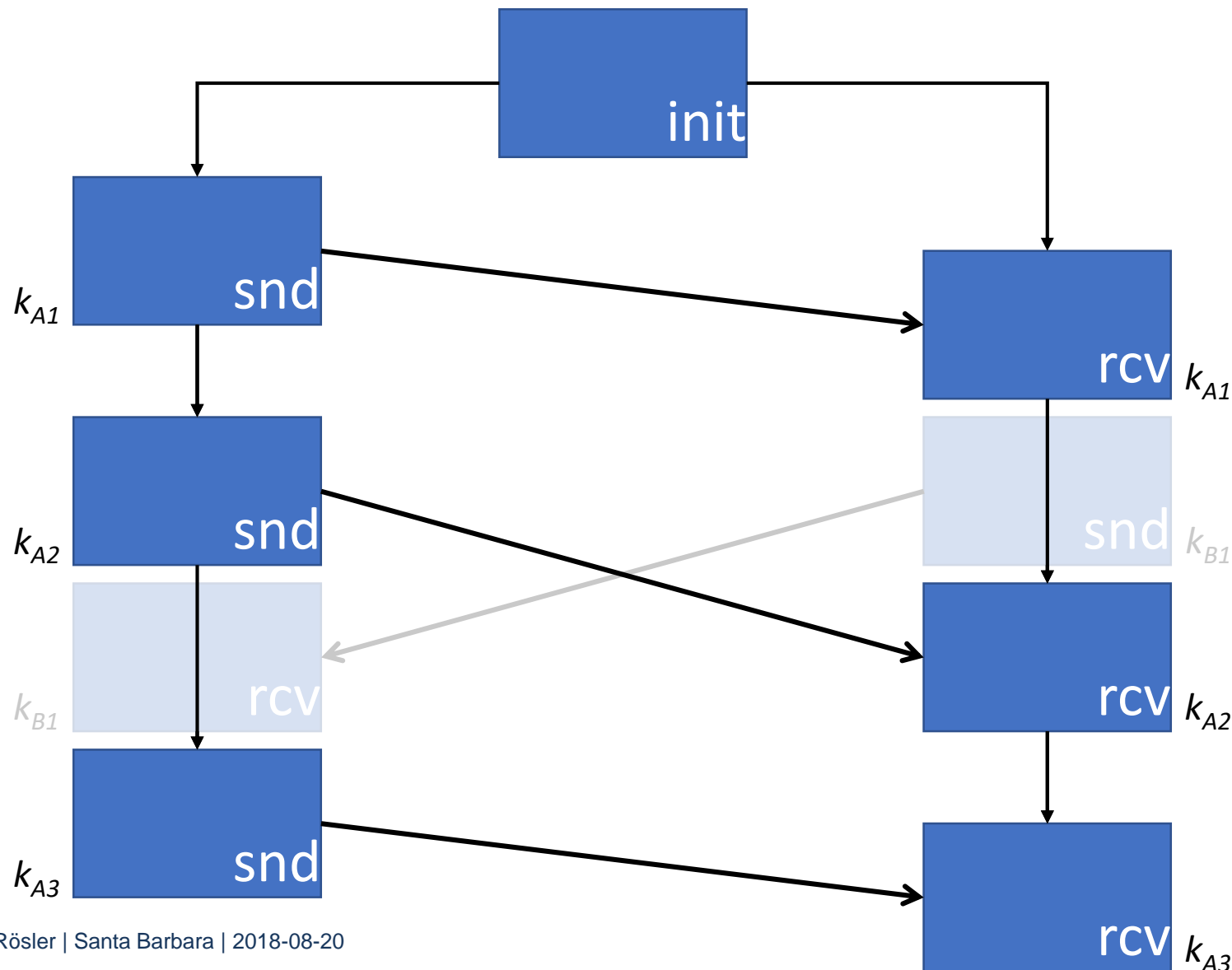
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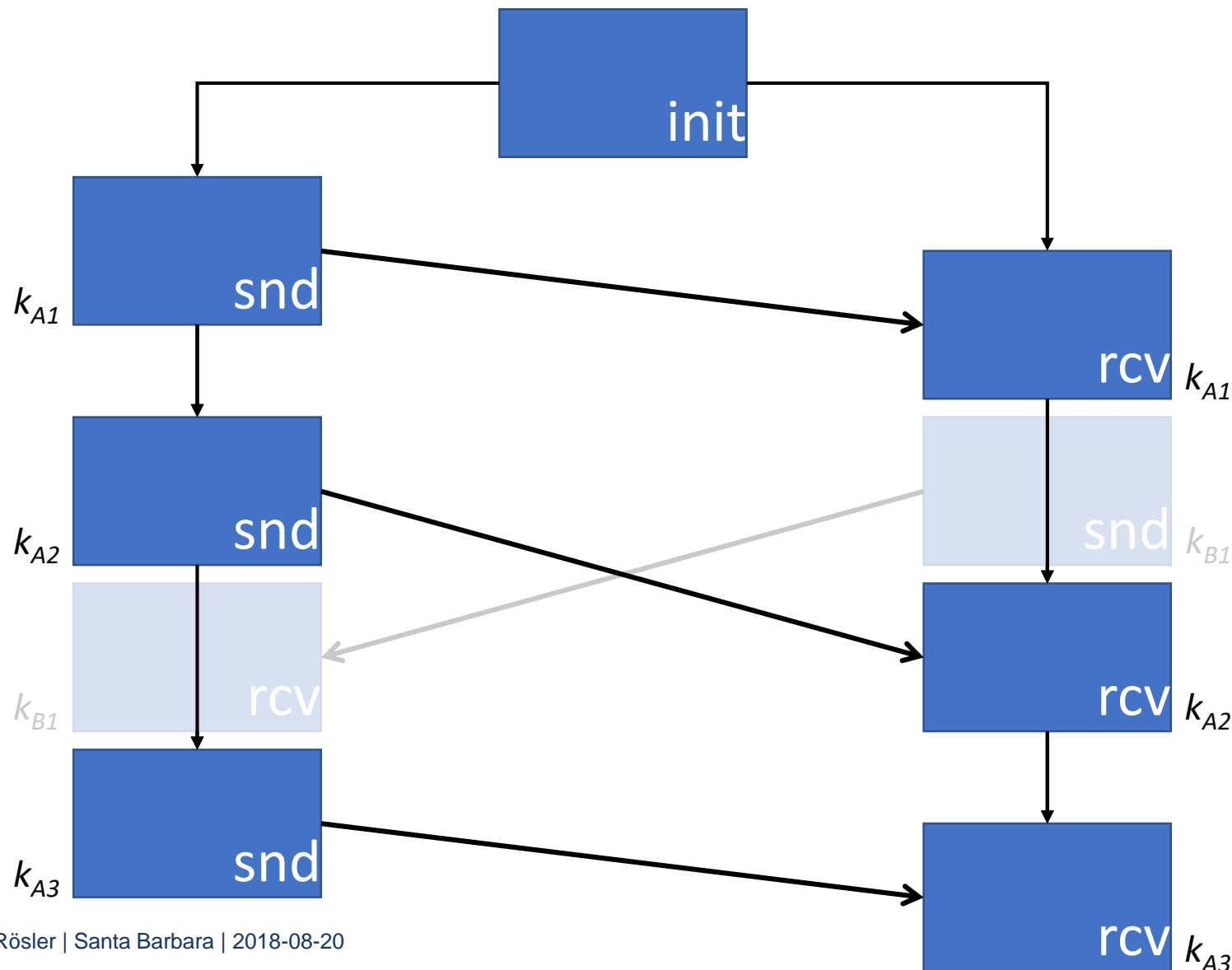
- Unidirectional key establishment



Three Variants of Ratcheting

- What is Ratcheting?
Modeling RKE
Construction Intuition
Results

- Bidirectional ratcheting is complicated
- Understand its components:
 - Unidirectional key establishment
 - Alice initiates computation of new key
 - Bob does not respond



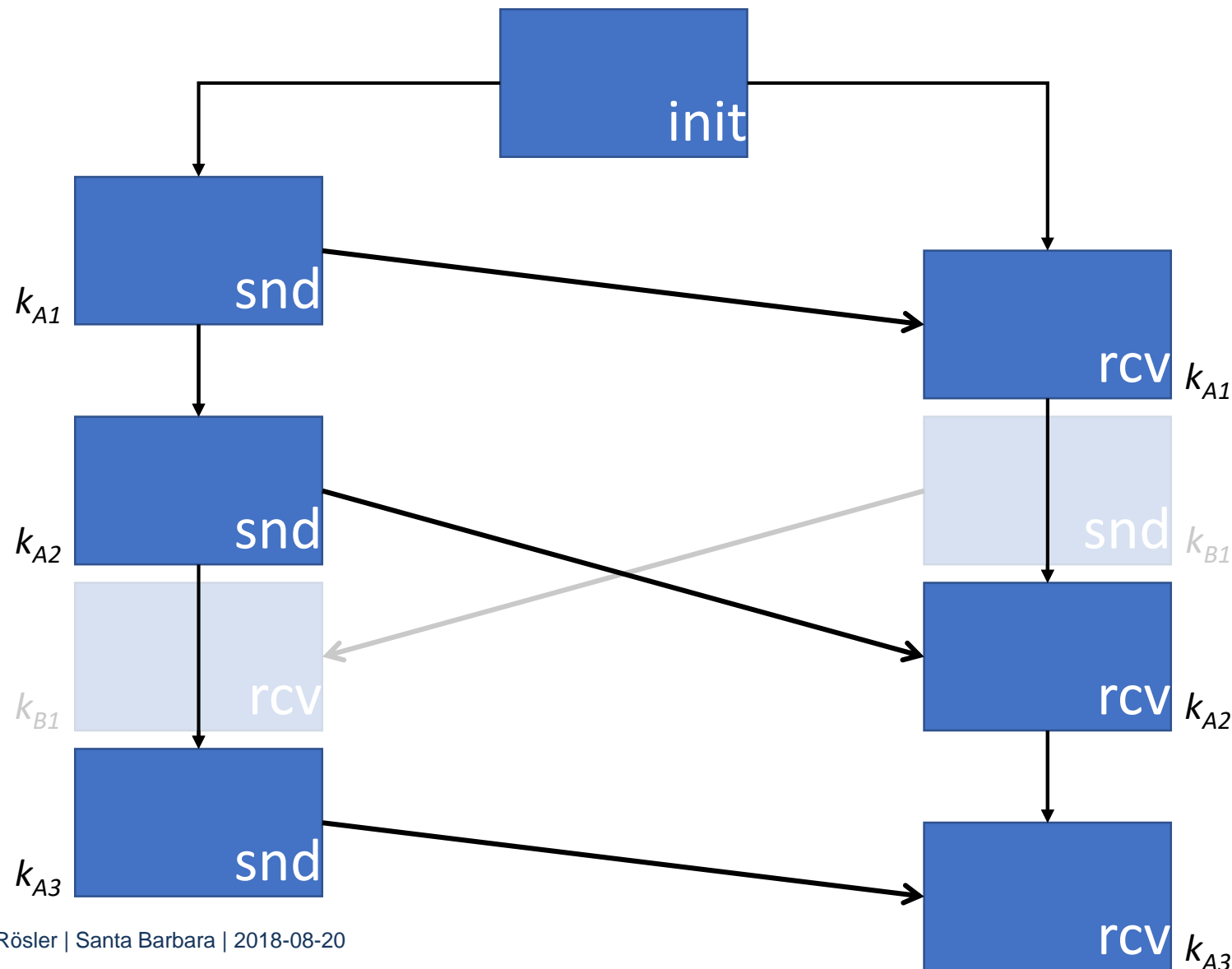
Three Variants of Ratcheting

- What is Ratcheting?
Modeling RKE
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Results

- Bidirectional ratcheting is complicated

→ Understand its components:

- Unidirectional ratcheted key exchange (RKE)



Three Variants of Ratcheting

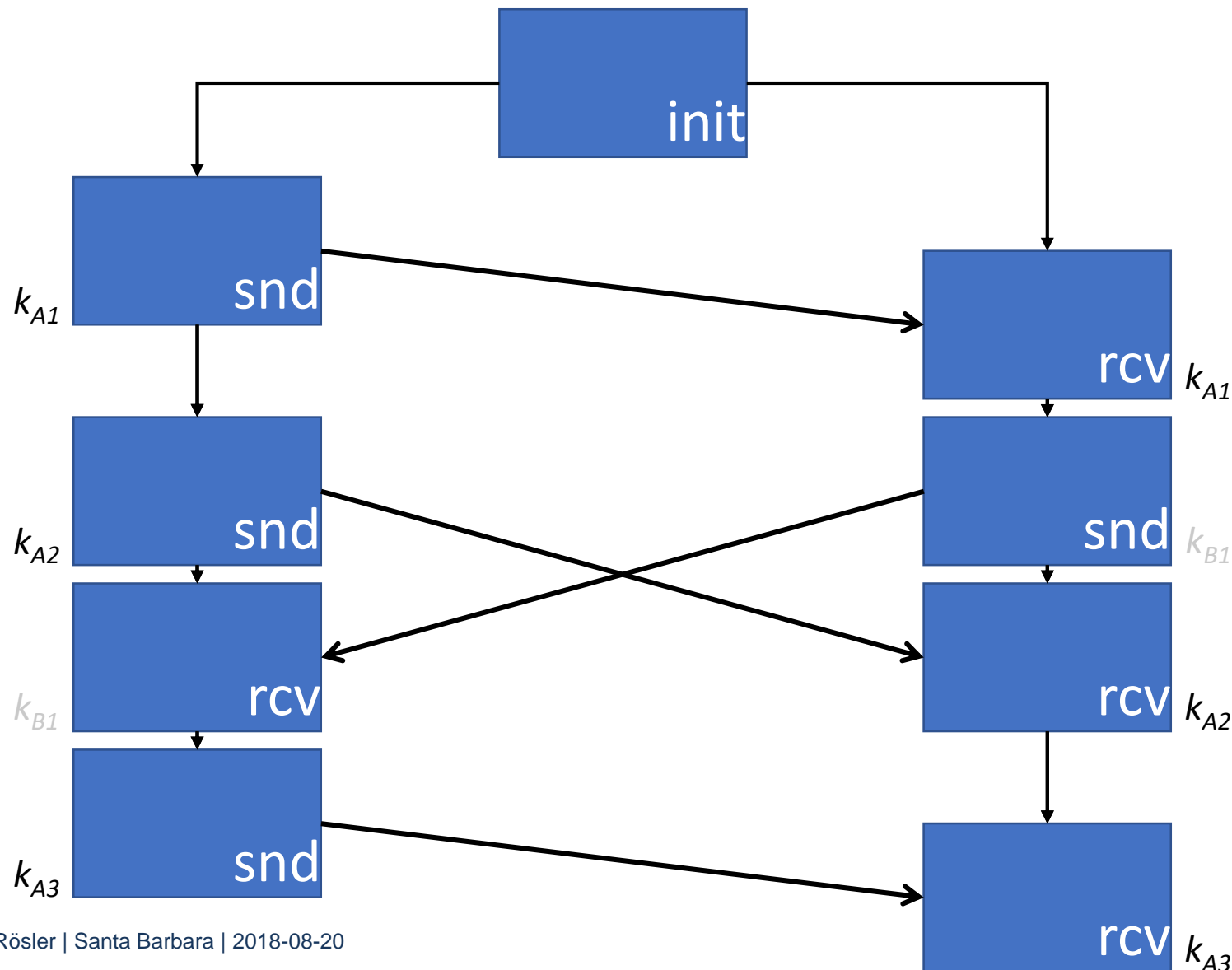
- What is Ratcheting?
Modeling RKE
Construction Intuition
Results

• Bidirectional ratcheting is complicated

→ Understand its components:

- Unidirectional RKE
- Sesquidirectional RKE
- Bob contributes (but cannot establish keys)
- Adds security

(sesqui = 1.5)



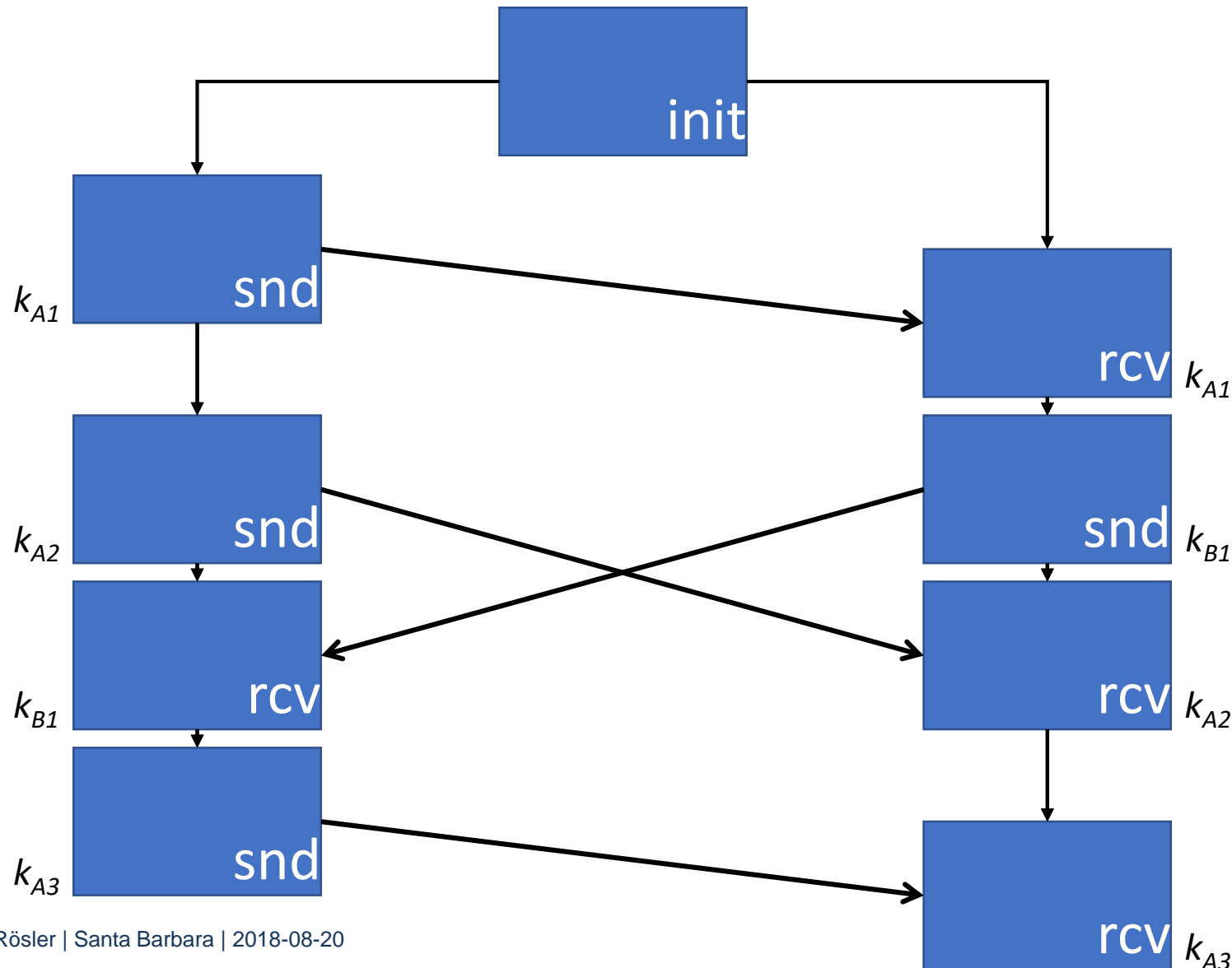
Three Variants of Ratcheting

- What is Ratcheting?
Modeling RKE
Construction Intuition
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• Bidirectional ratcheting is complicated

→ Understand its components:

- Unidirectional RKE
- Sesquidirectional RKE
- Symmetric roles



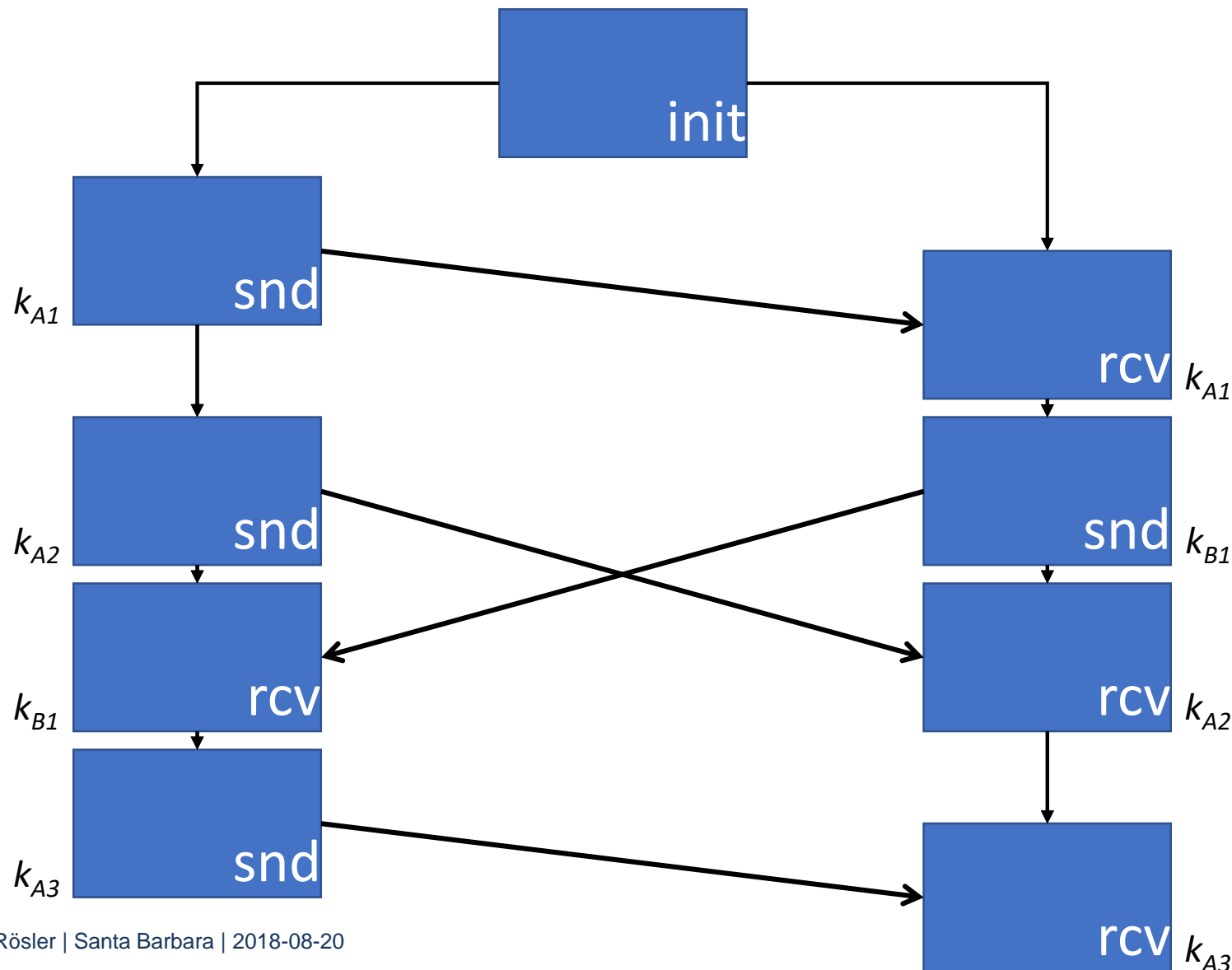
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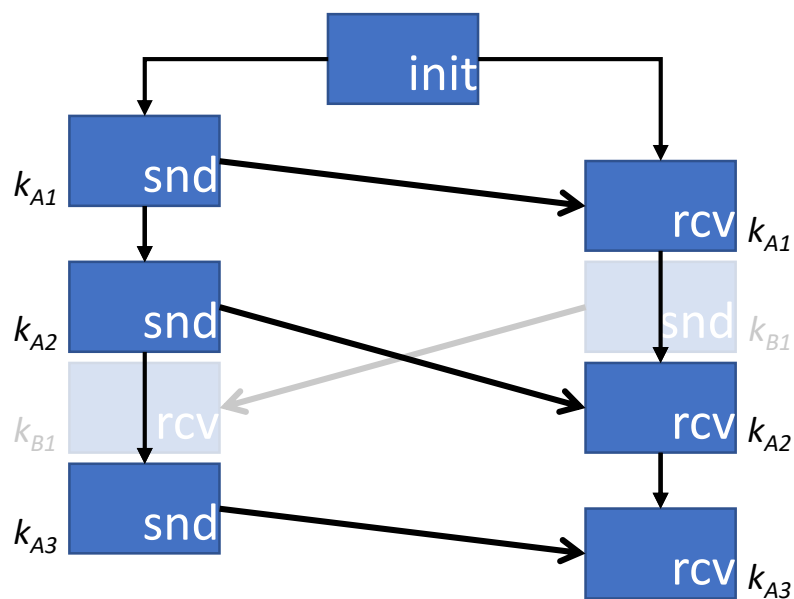
- Unidirectional RKE
- Sesquidirectional RKE
- Symmetric roles
- Bidirectional RKE = 2x Sesquid. RKE (extended version)



- What is Ratcheting?
Modeling RKE
Construction Intuition
Results

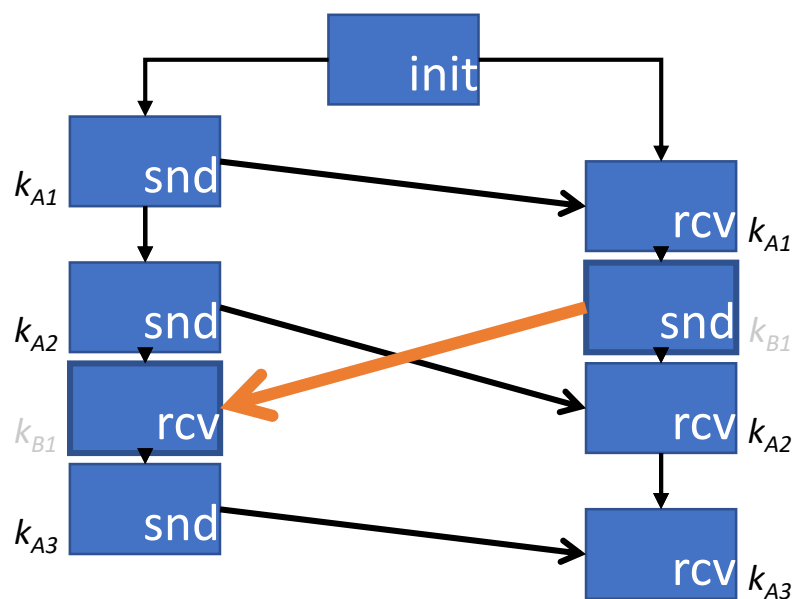
Three Variants of Ratcheting

Unidirectional RKE (+ Exposure of Bob)



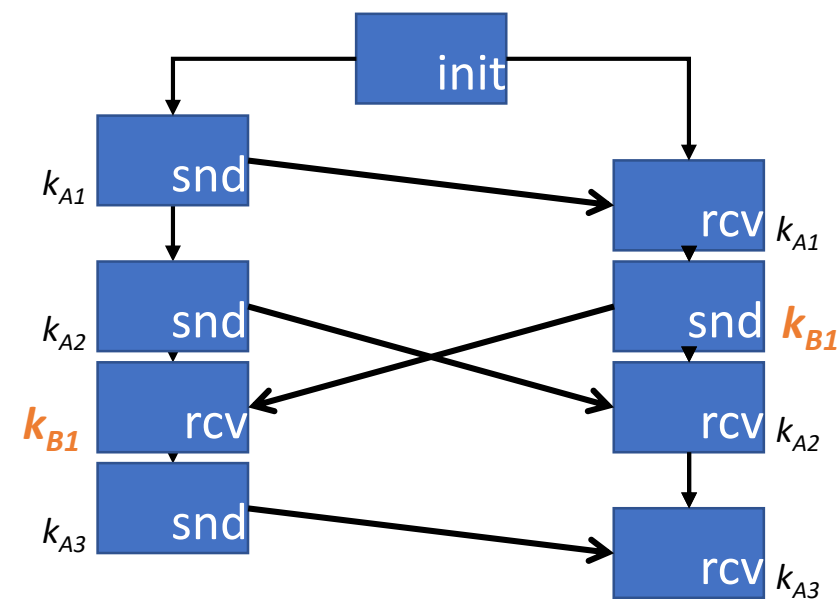
No responses
from Bob

Sesquidirectional RKE



Bob's responses
only help to recover

Bidirectional RKE



Symmetric roles
(extended version)

Agenda

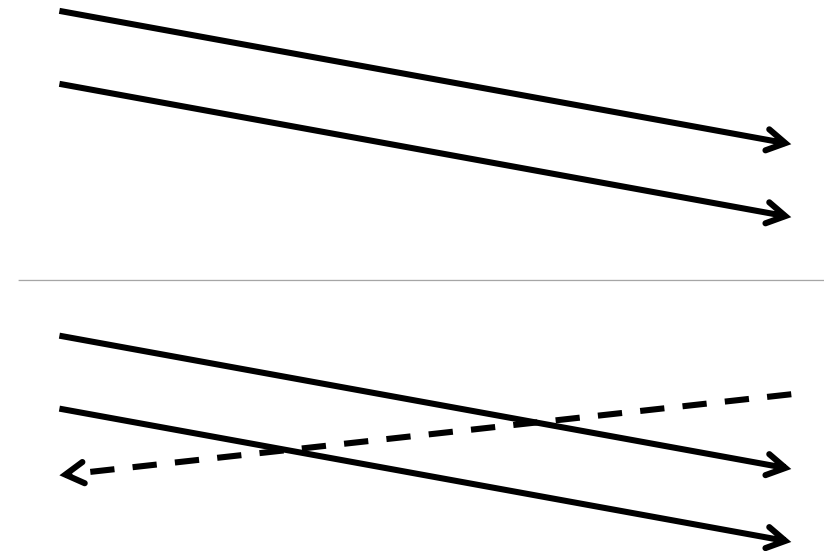
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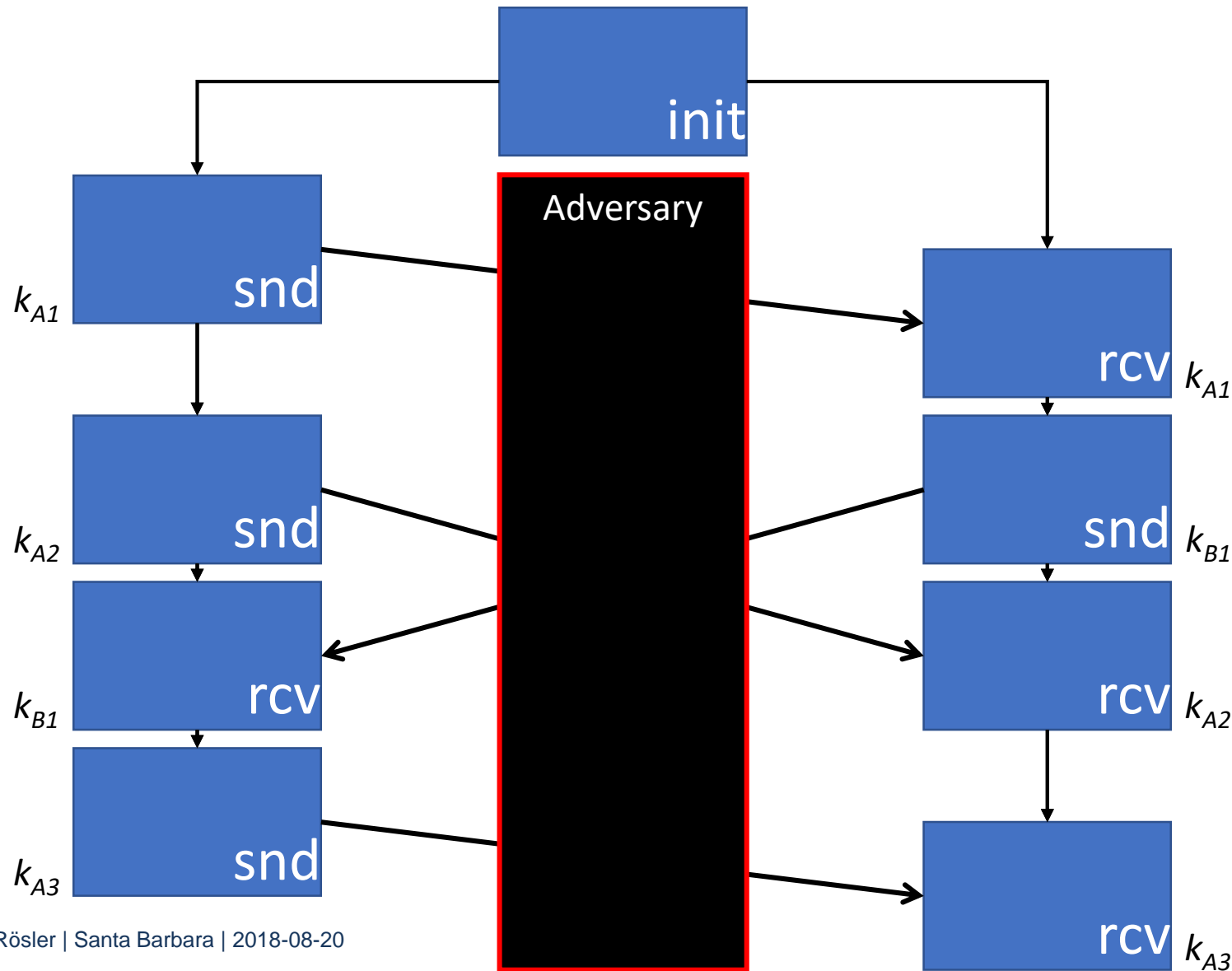
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Modeling Ratcheted Key Exchange

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

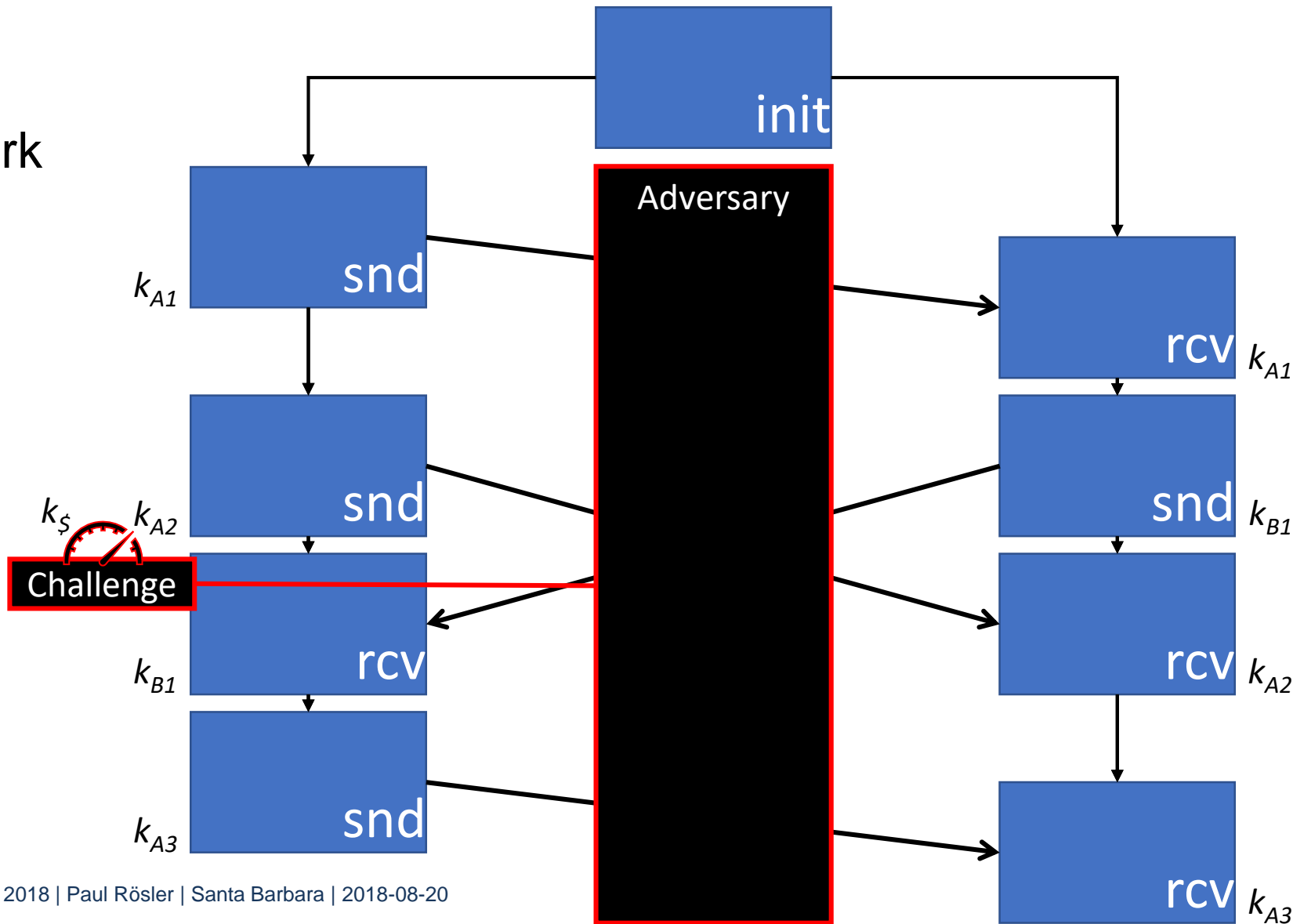
- Active adversary
 - Control whole network traffic



Modeling Ratcheted Key Exchange

What is Ratcheting?
 Modeling RKE
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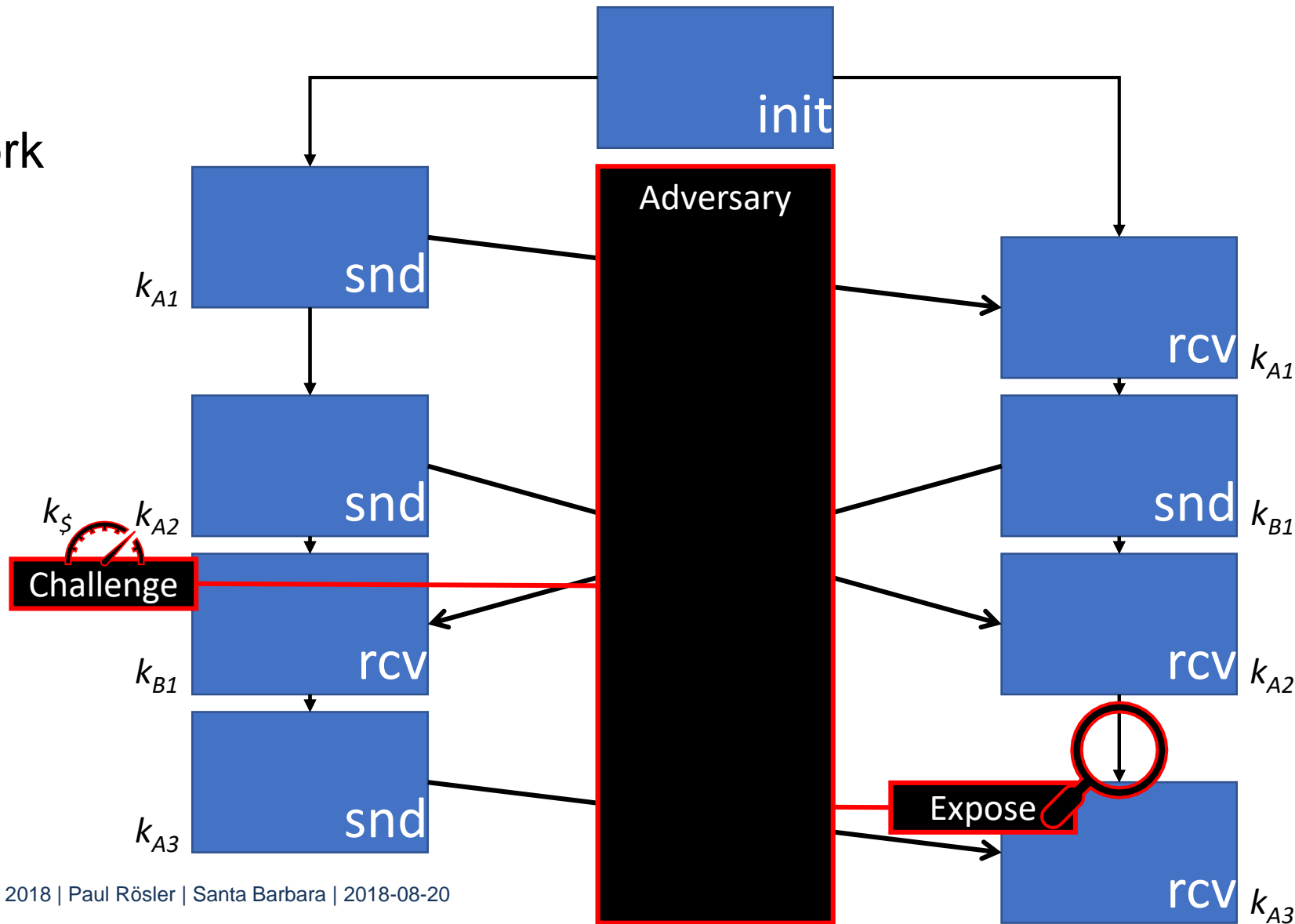
- Active adversary
 - Control whole network traffic
 - Analyze key indistinguishability
 - Multi-challenge real or random key
- Guess bit $b \in \{0,1\}$



Modeling Ratcheted Key Exchange

- What is Ratcheting?
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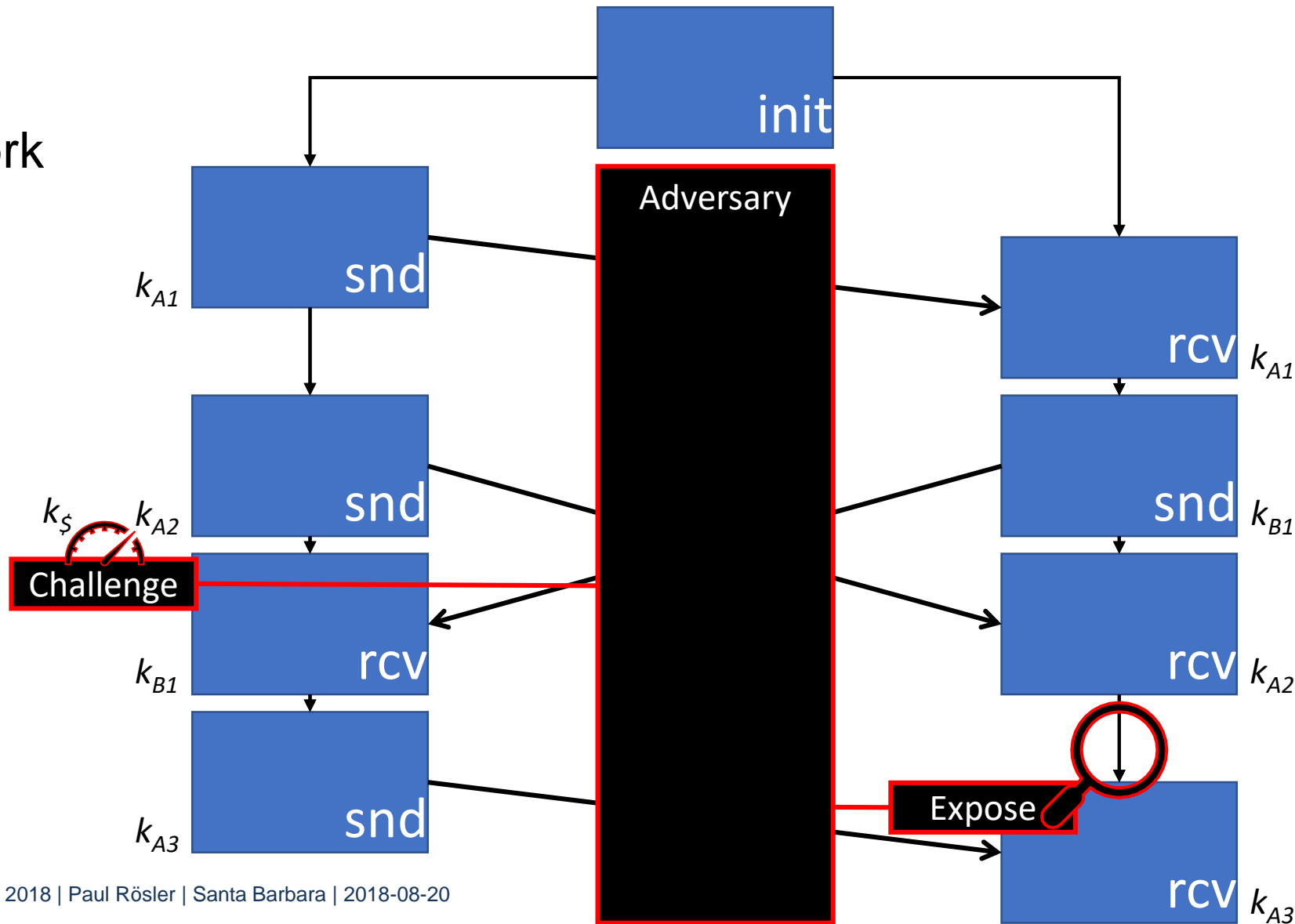
- Active adversary
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 - Multi-challenge real or random key
- Model exposures of local state



Modeling Ratcheted Key Exchange

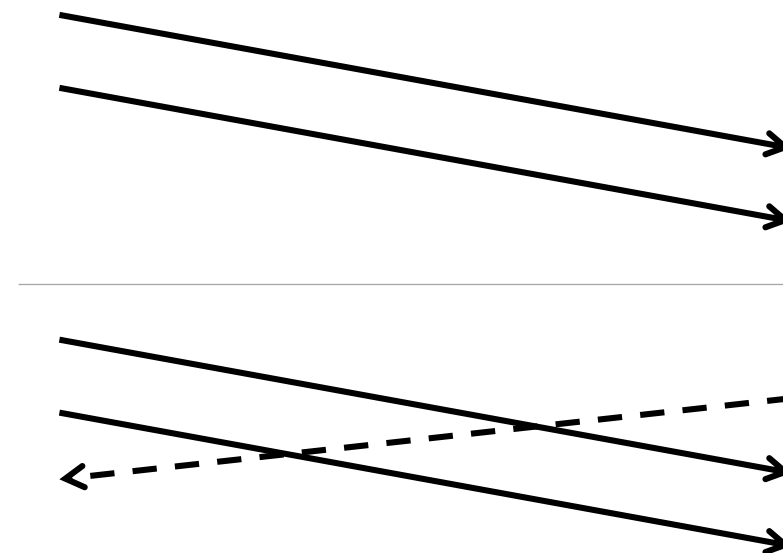
- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Active adversary
 - Control whole network traffic
- Analyze key indistinguishability
 - Multi-challenge real or random key
- Model exposures of local state
- Single session
- Init abstracted



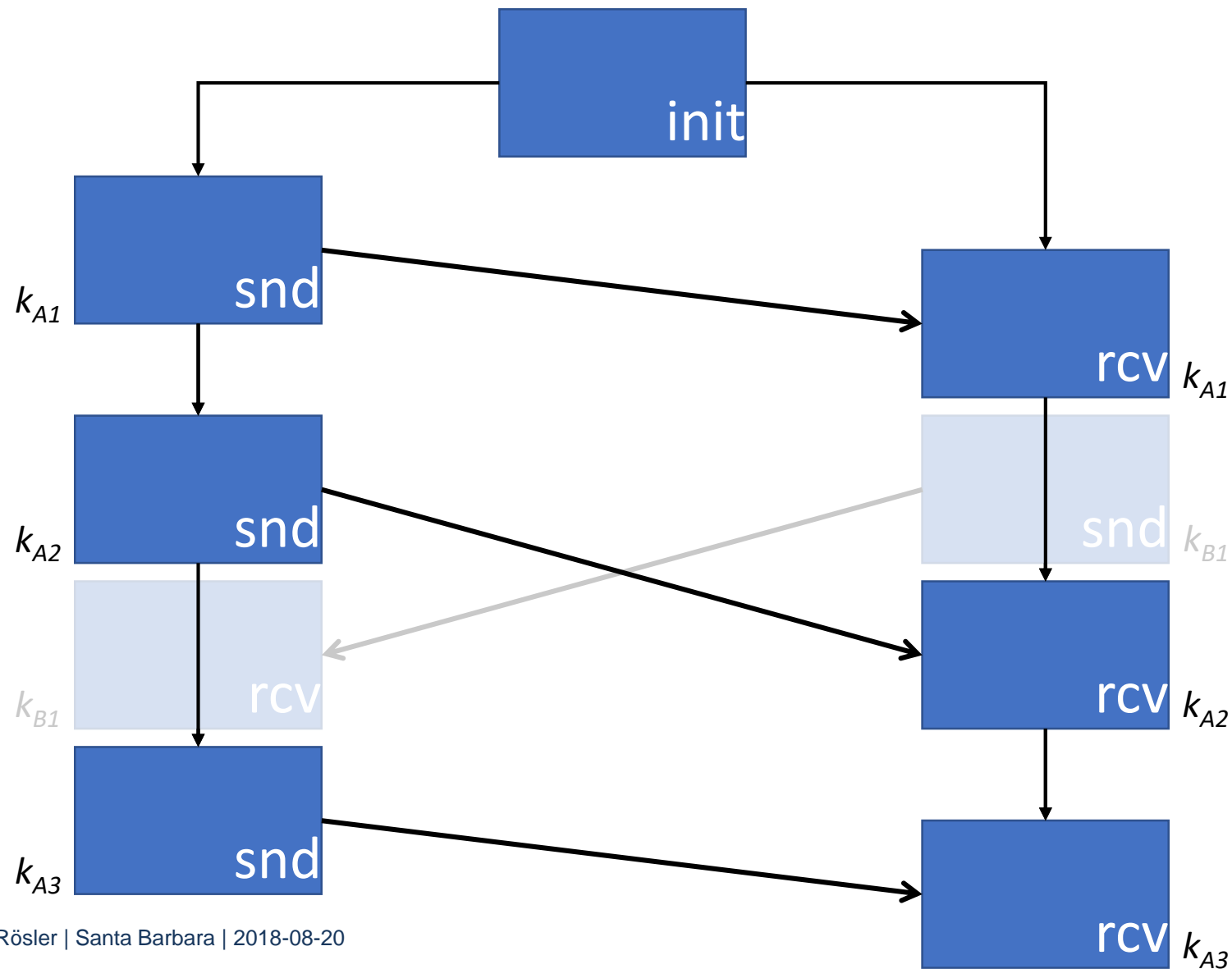
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1. The Primitive Ratcheted Key Exchange
2. General Adversary Model
3. **Unidirectional Ratcheting**
→ **Model** and Construction
4. Sesquidirectional Ratcheting
→ Model and Construction
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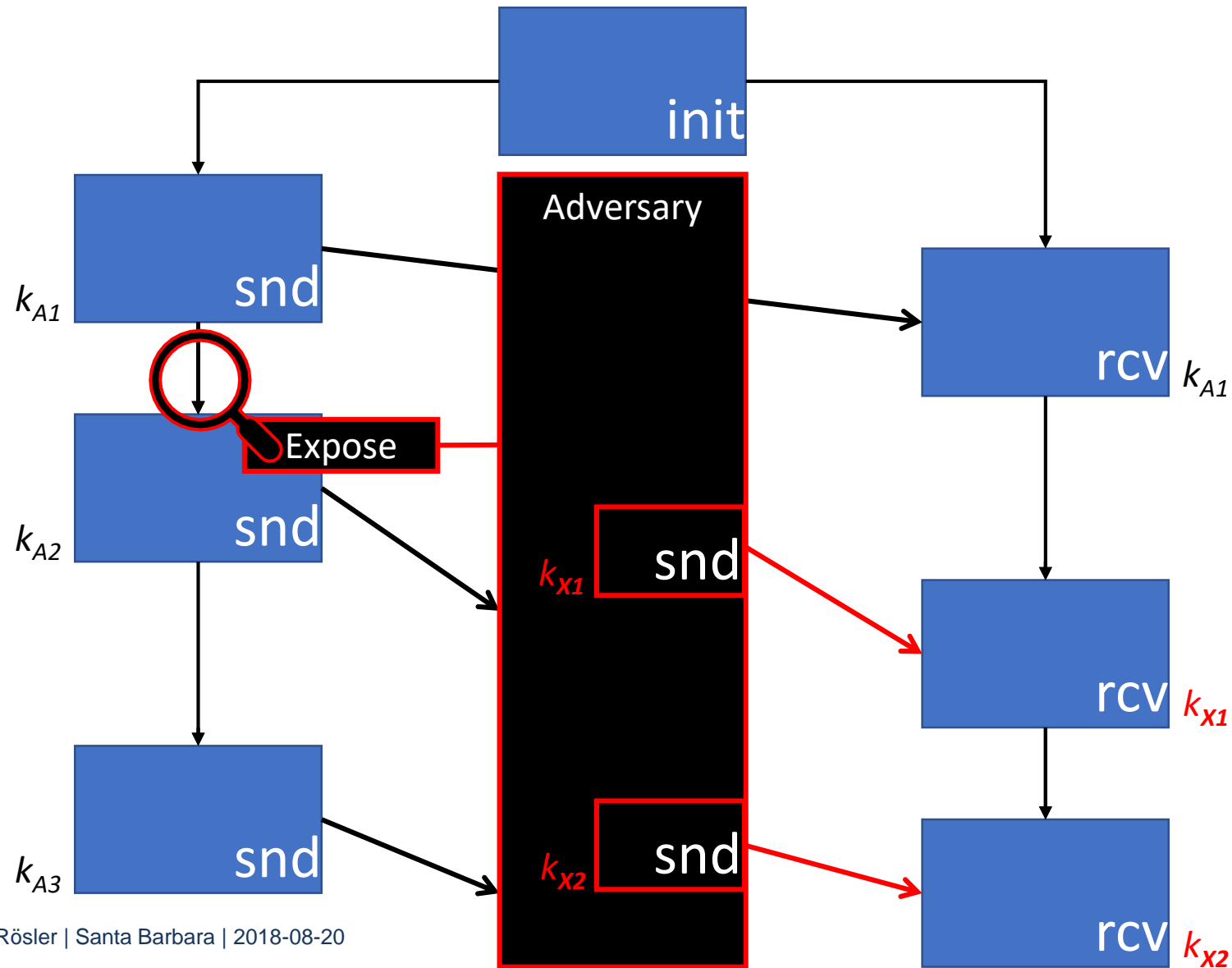
Modeling Unidirectional RKE



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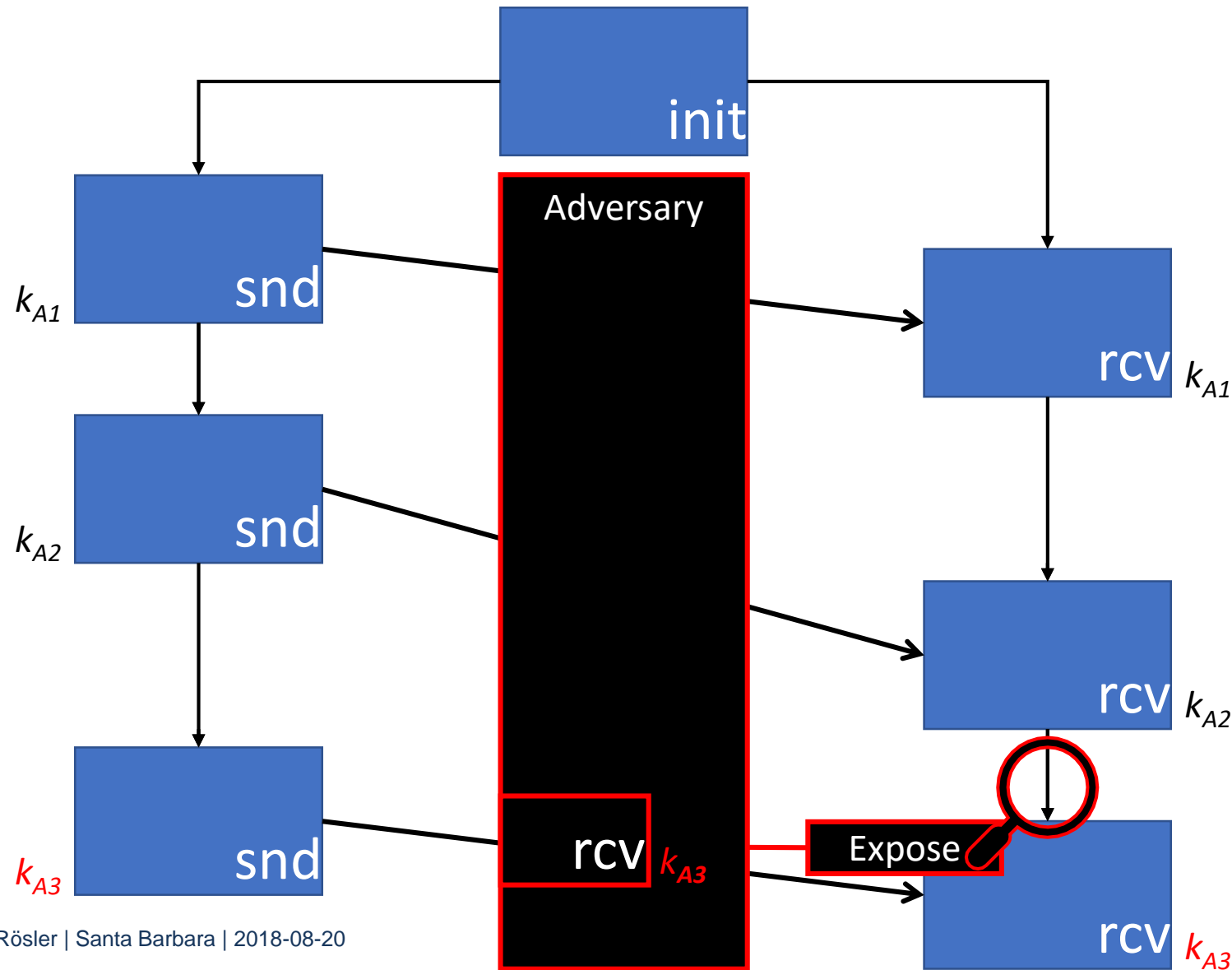
- Impersonation
⇒ No future Challenge on Bob



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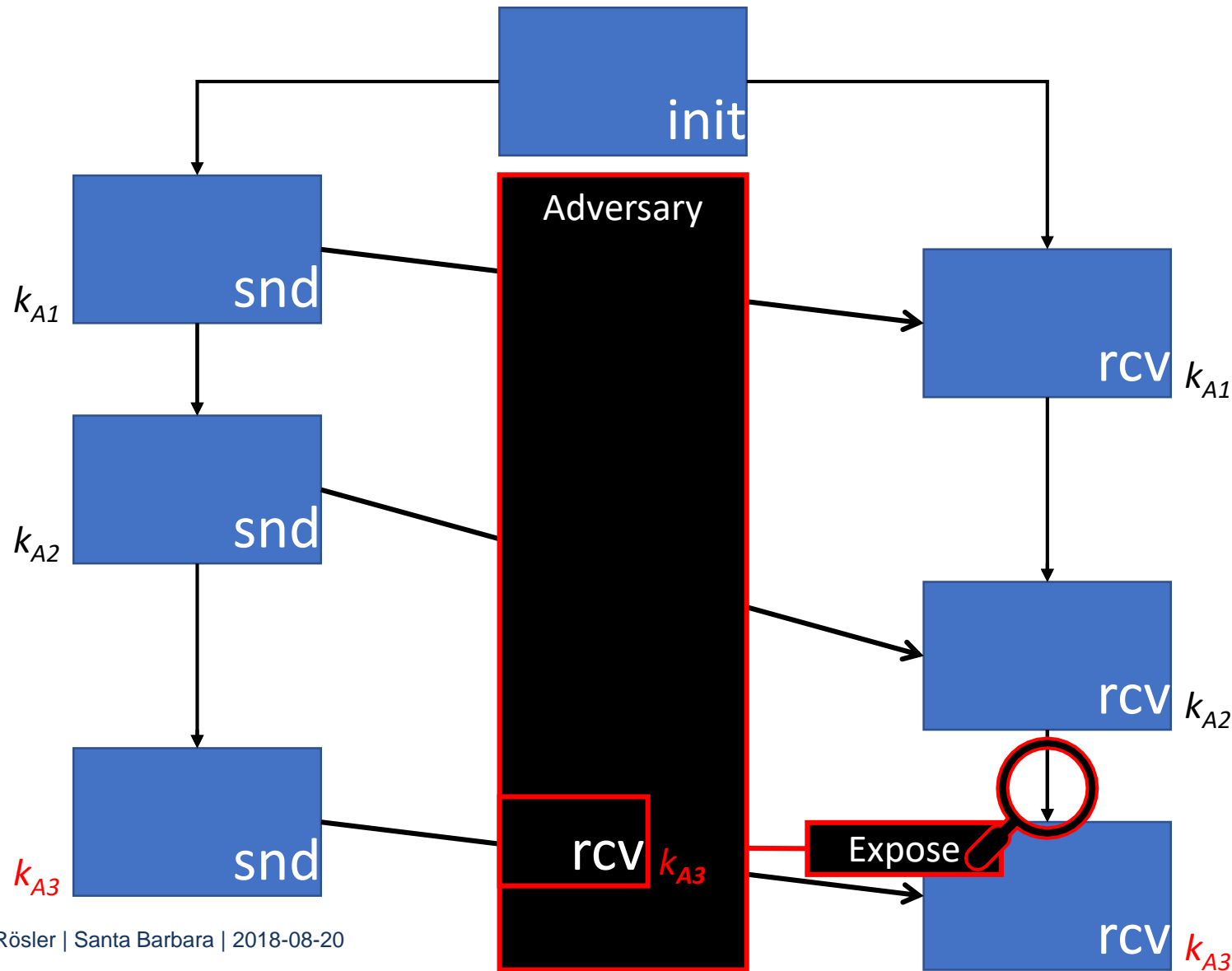
- Impersonation
⇒ No future Challenge on Bob
- Expose Bob
→ Allowed in our model



Modeling Unidirectional RKE

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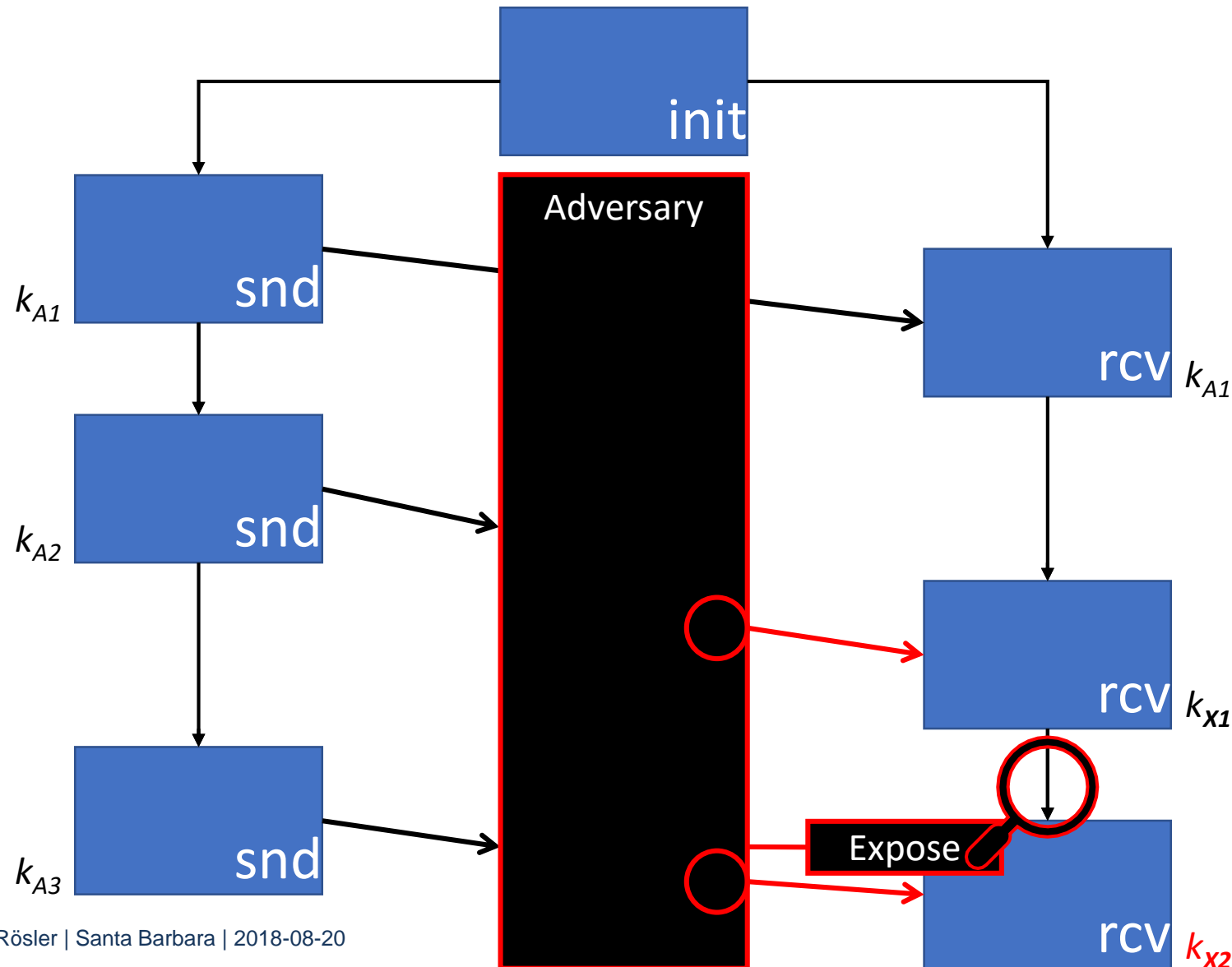
- Impersonation
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- Expose Bob
⇒ No future Challenge



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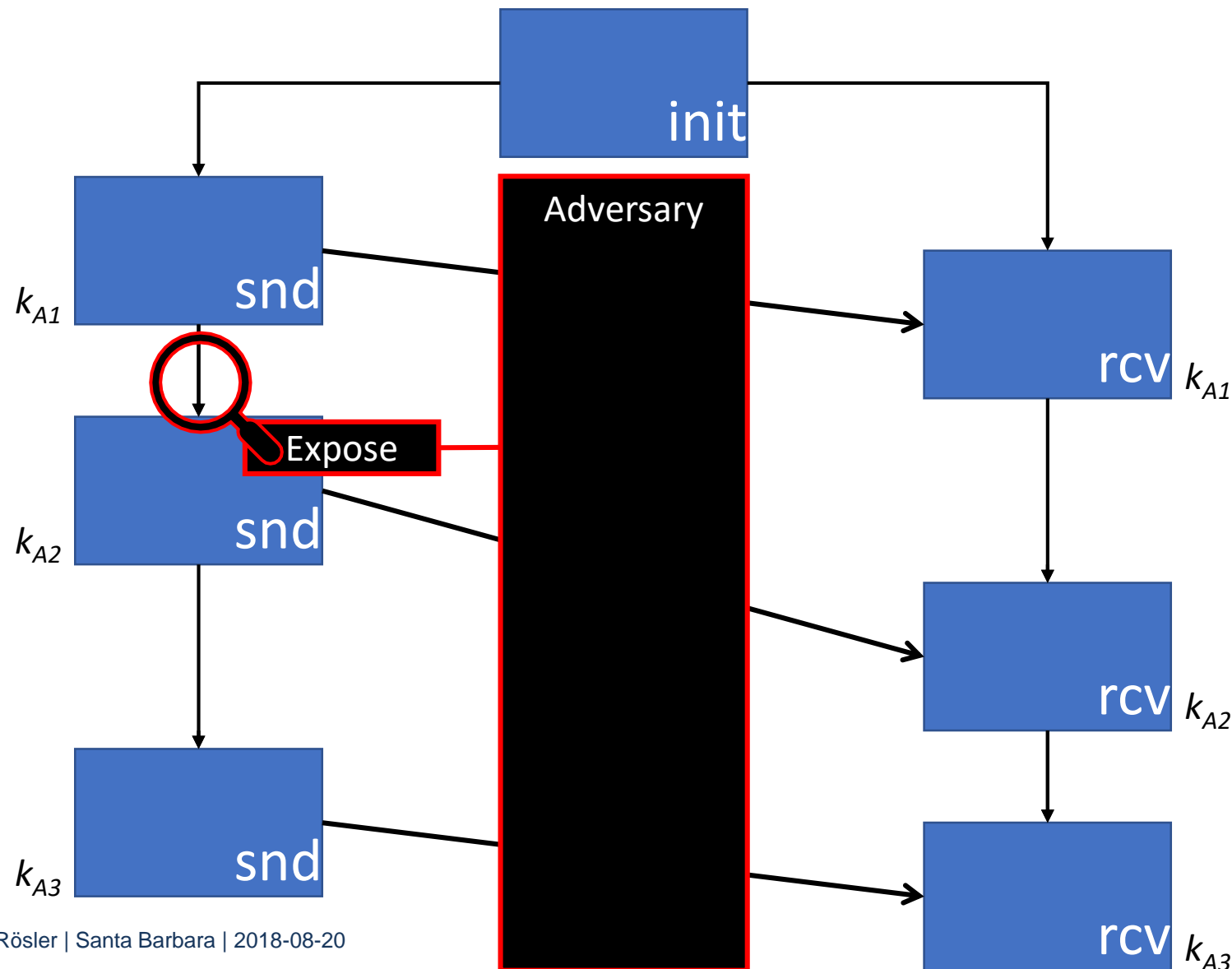
- Impersonation
⇒ No future Challenge on Bob
- Expose Bob
⇒ No future Challenge **if synchronous**
(= if no previous active attack)



Modeling Unidirectional RKE

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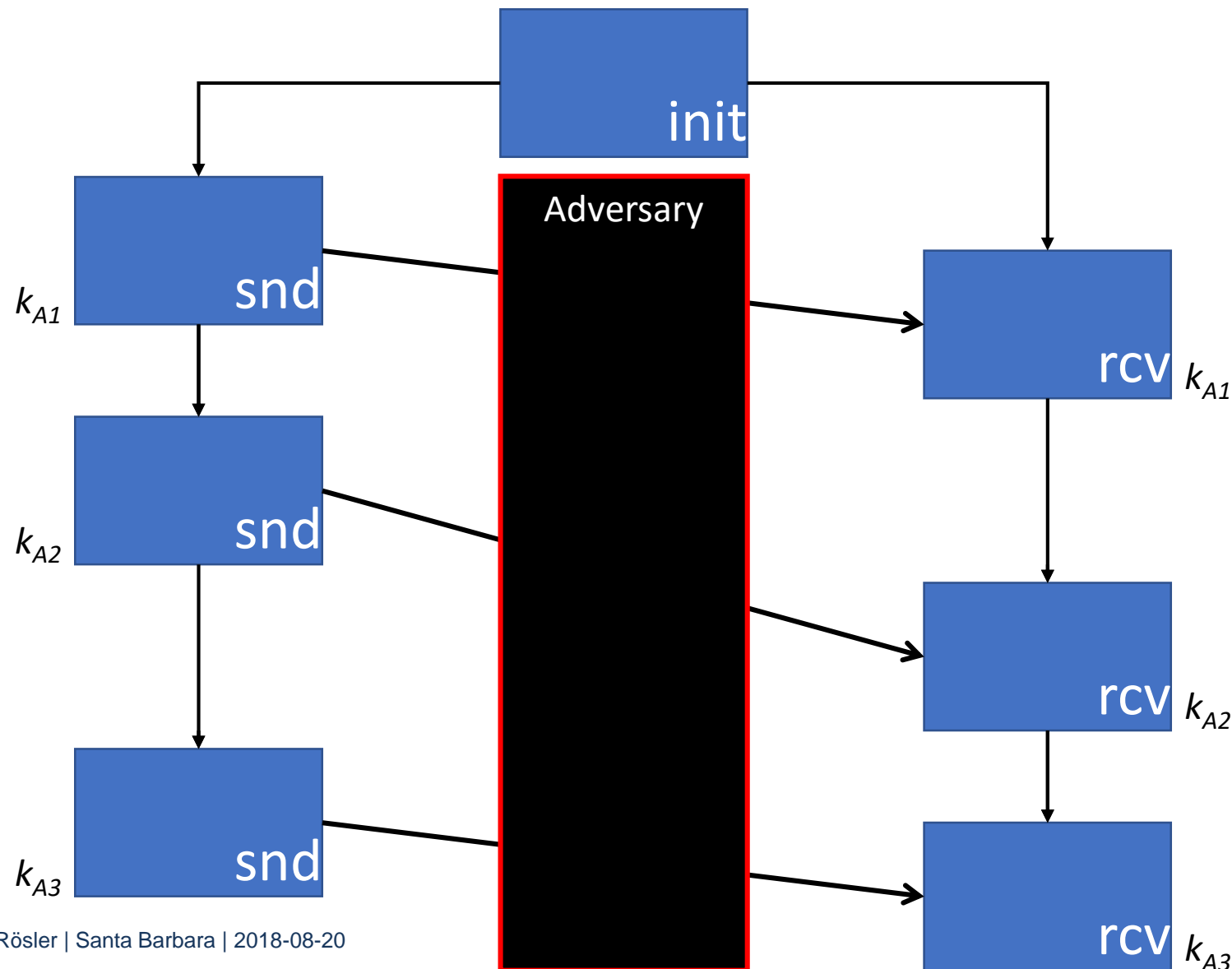
- Impersonation
⇒ No future Challenge on Bob
 - Expose Bob
⇒ No future Challenge if synchronous
- ⇒ Exposure of Alice (solely) “okay”



Modeling Unidirectional RKE

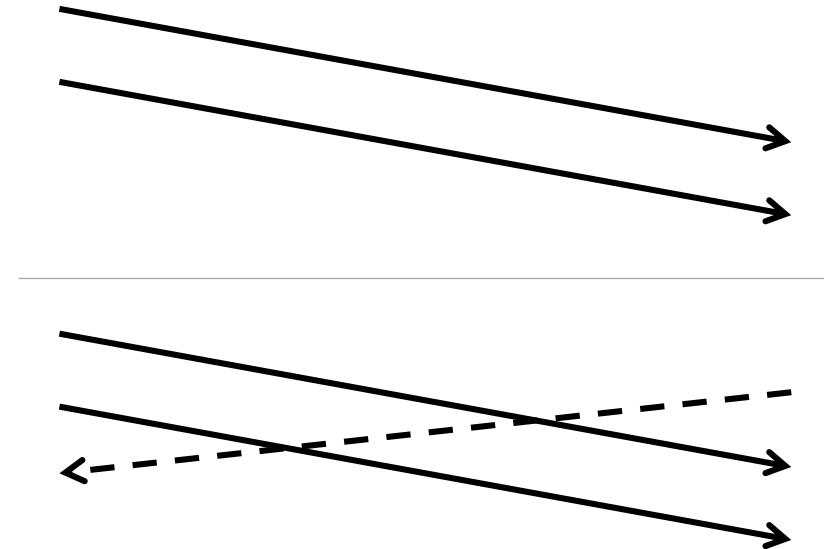
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- Impersonation
⇒ No future Challenge on Bob
- **Expose Bob**
⇒ **No future Challenge if synchronous**
- ⇒ Exposure of Alice (solely) “okay”



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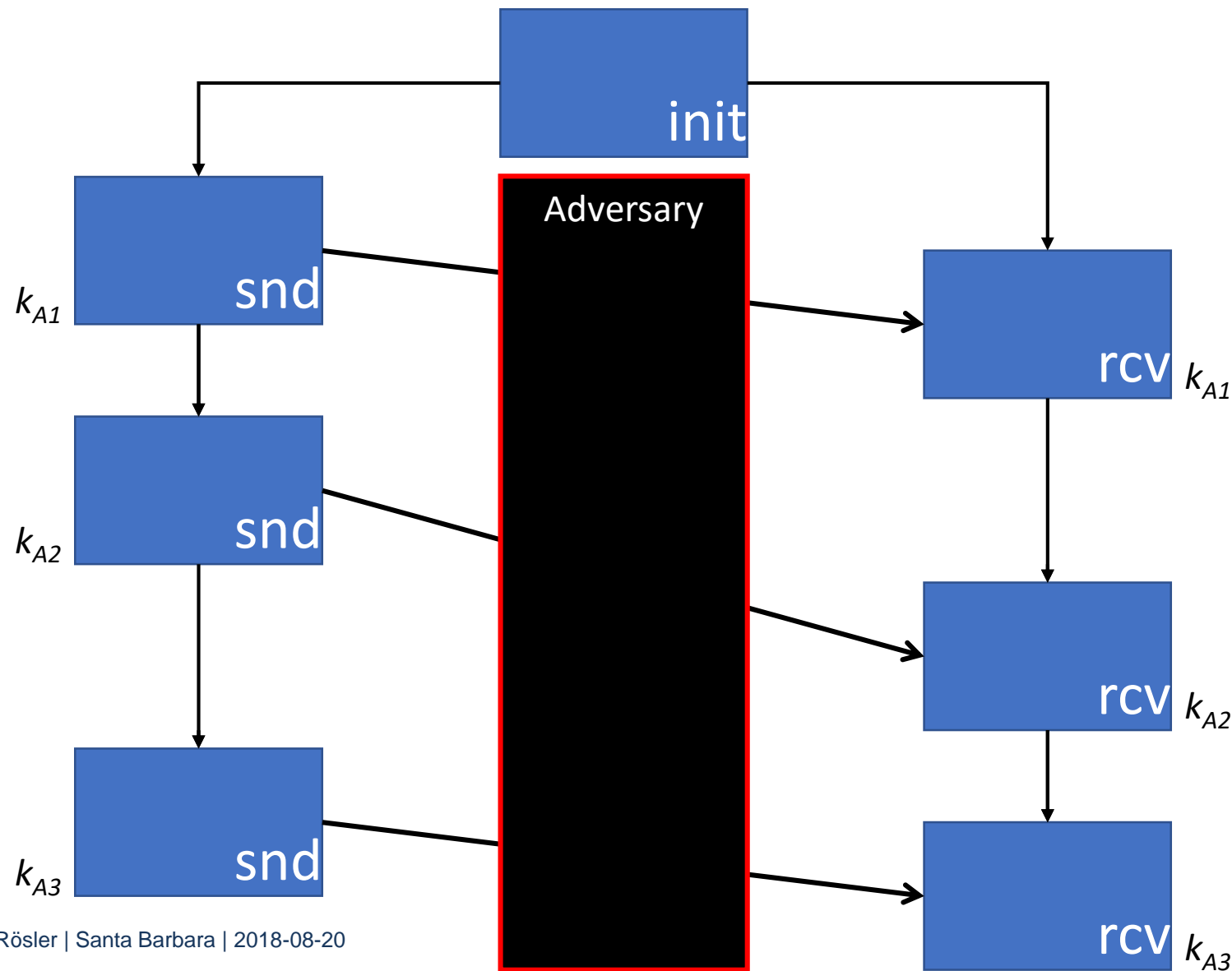
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→ Model and **Construction**
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Constructing Unidirectional RKE

- What is Ratcheting?
- Modeling RKE
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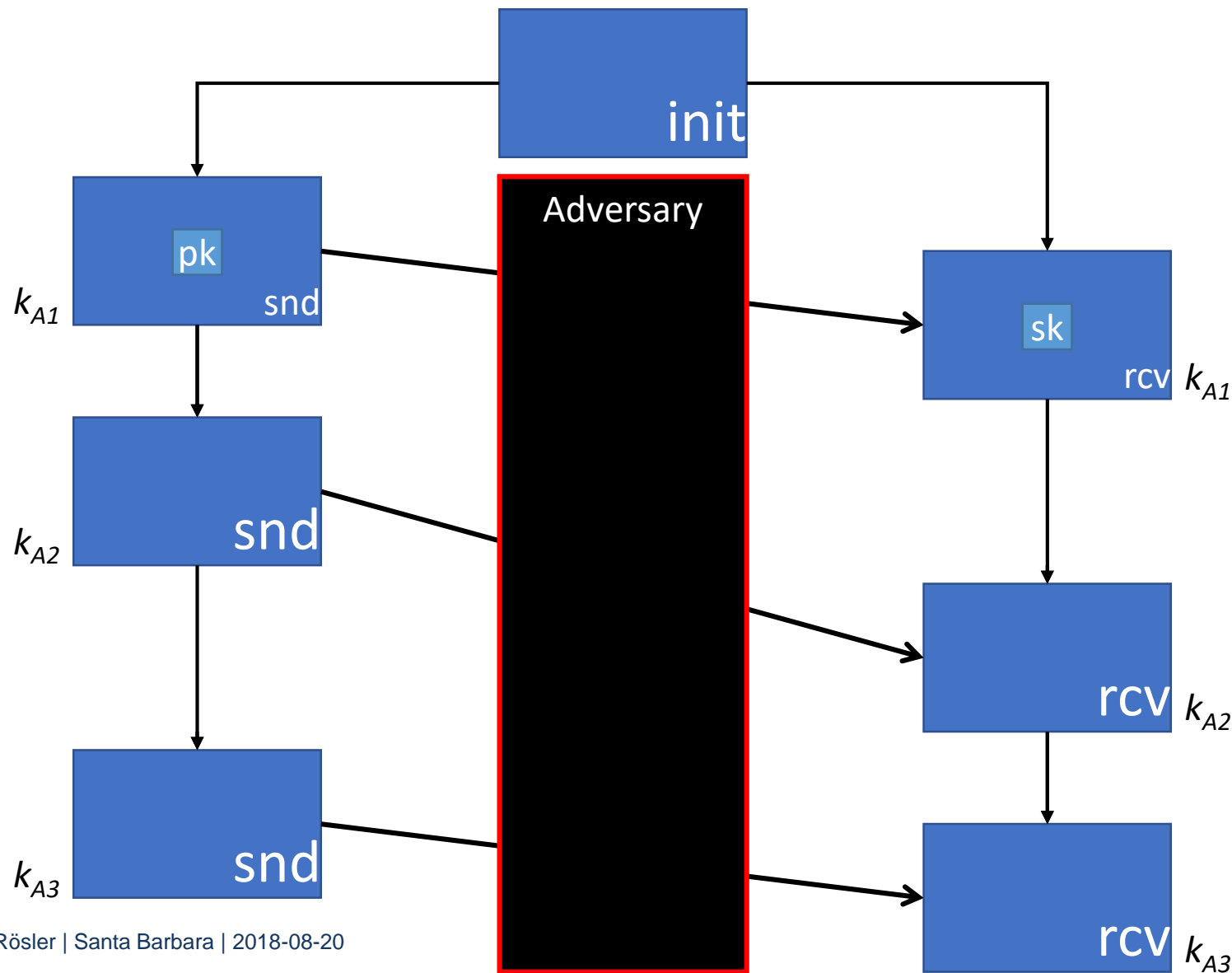
- **Expose Alice okay**
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Constructing Unidirectional RKE

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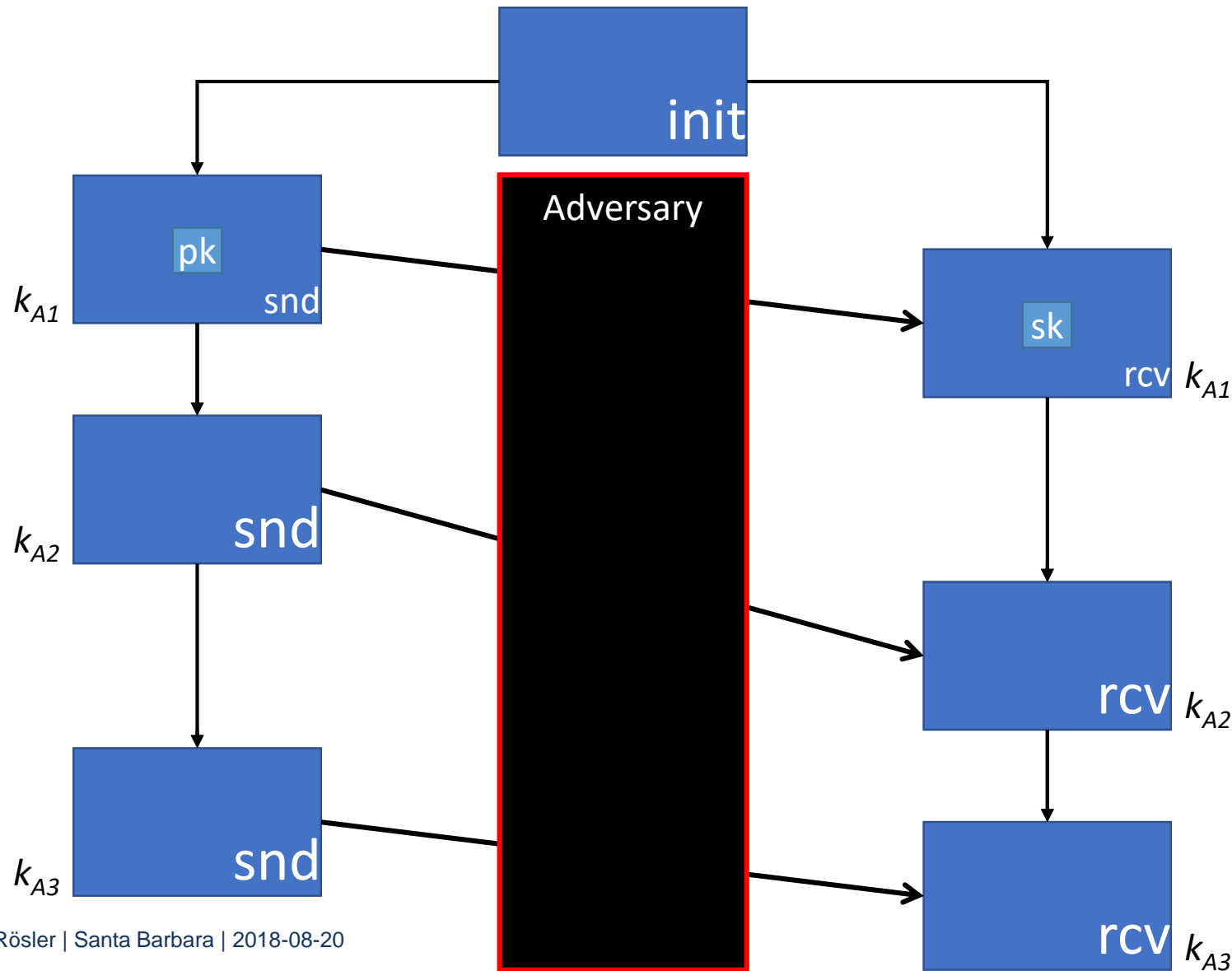
- **Expose Alice okay**
→ Public key crypto
- **Expose Bob**
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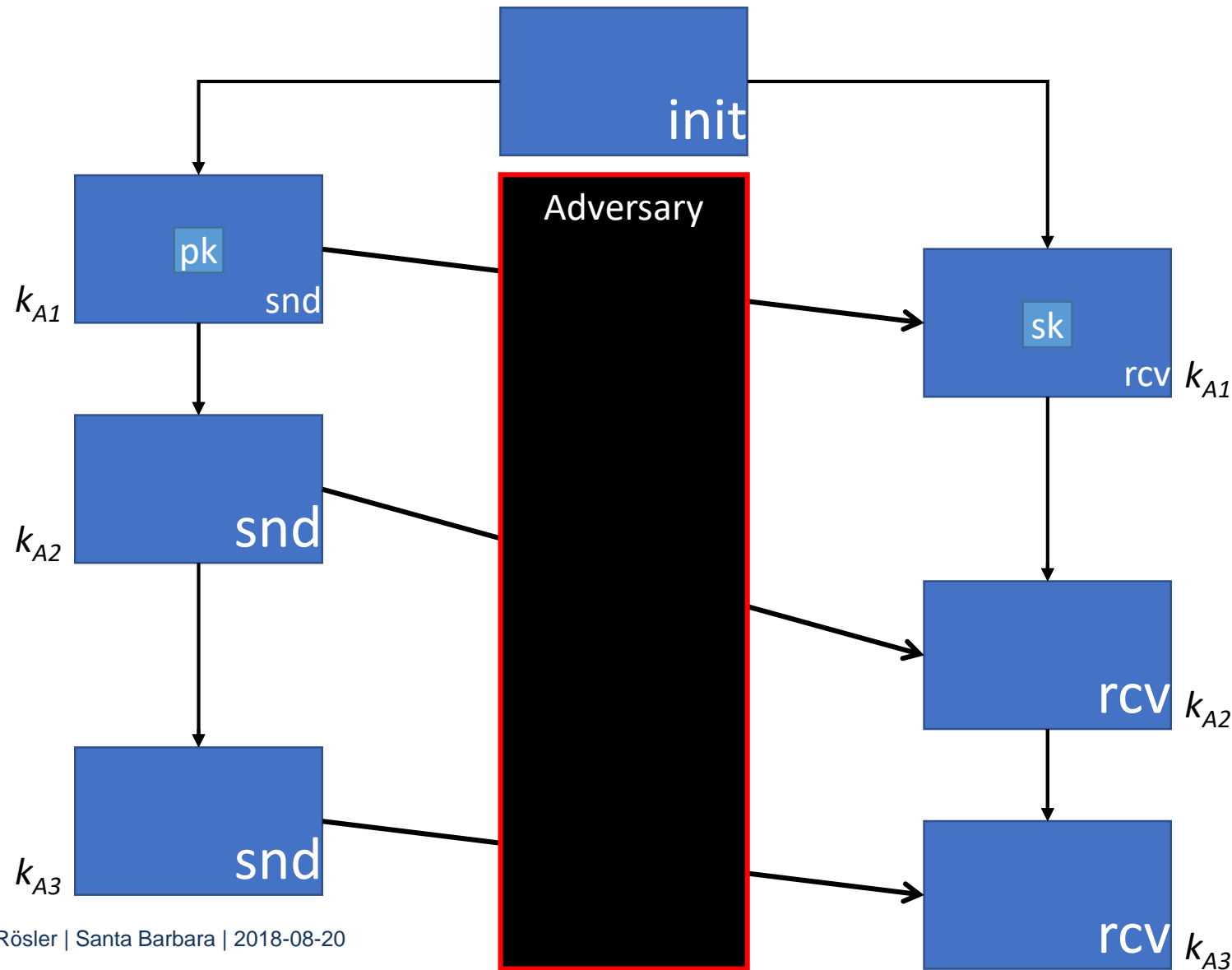
- **Expose Alice okay**
→ KEM:
 $\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \text{ k}$ $\text{dec}(\text{sk} \text{ c}) \rightarrow_{\xi} \text{k}$
- **Expose Bob**
⇒ **No future Challenge**
if synchronous



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- Expose Alice okay
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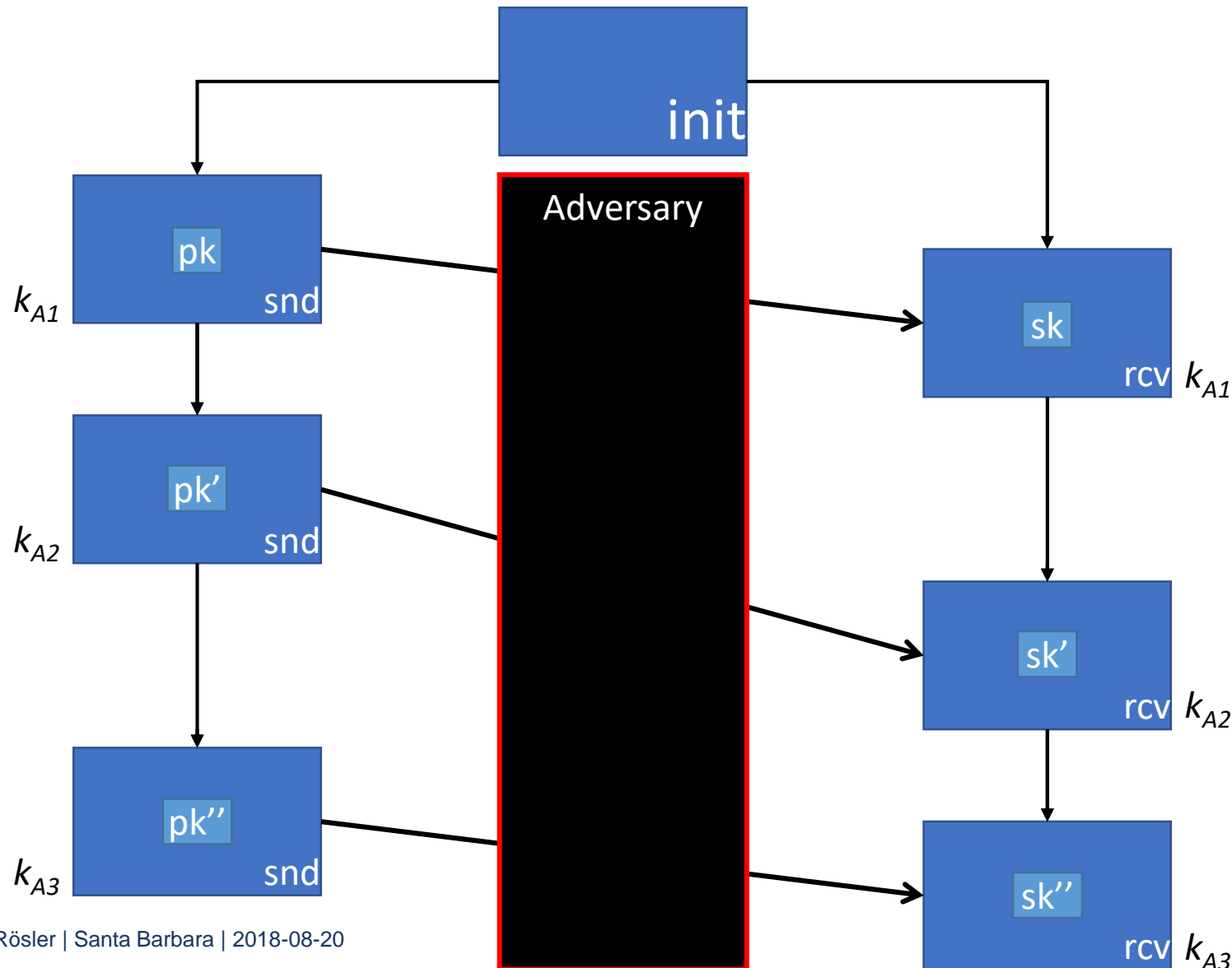
→ KEM:

$$\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \parallel \text{k} \quad \text{dec}(\text{sk} \parallel \text{c}) \rightarrow_{\xi} \text{k}$$

- Expose Bob**

⇒ **No future Challenge if synchronous**

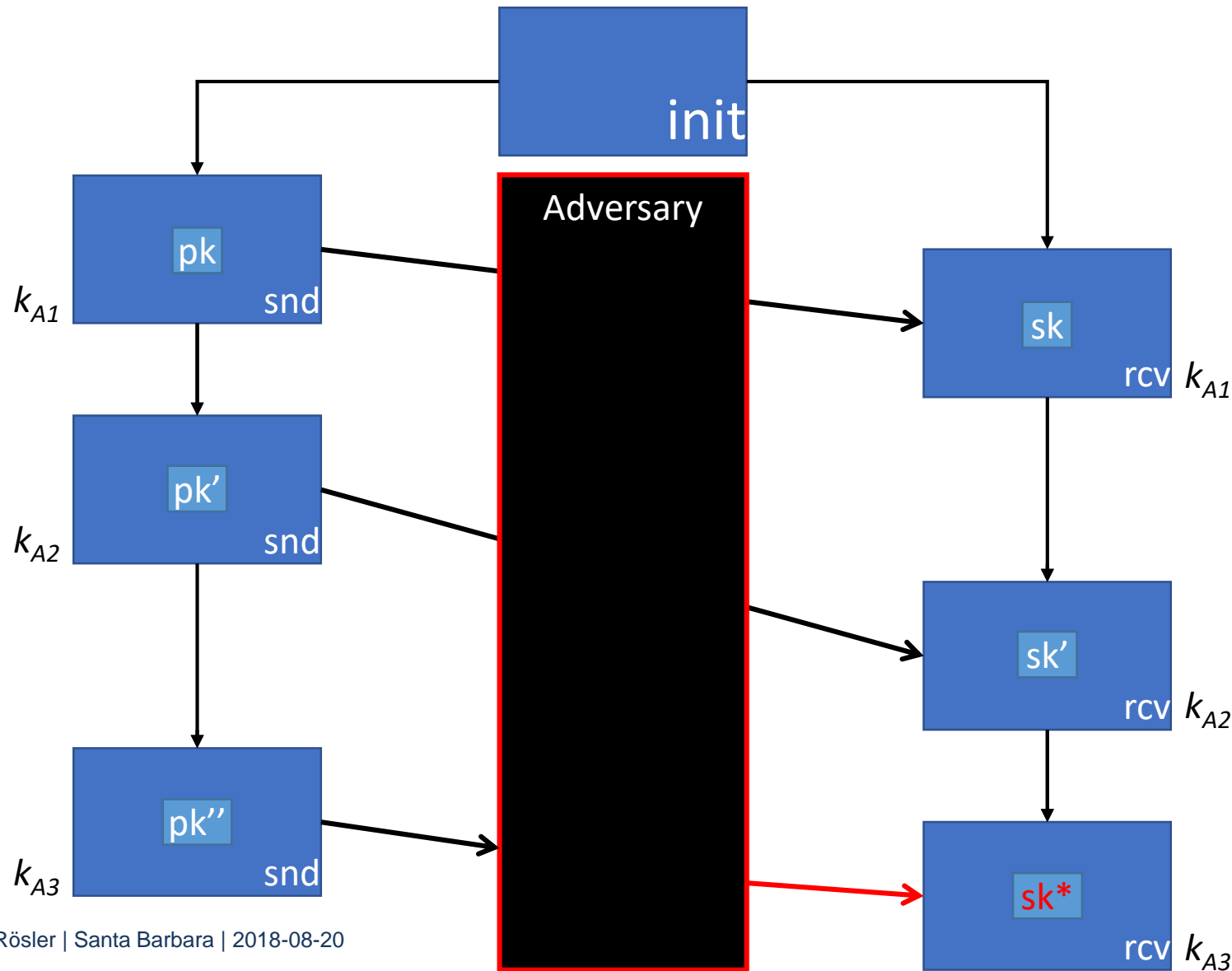
→ Forward secrecy of Bob's state



Constructing Unidirectional RKE

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 $\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \text{ k}$ $\text{dec}(\text{sk} \text{ c}) \rightarrow_{\xi} \text{k}$
- **Expose Bob**
 ⇒ **No future Challenge if synchronous**
 → Forward secrecy of Bob's state
 → Divergence of states



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→ KEM:

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- Expose Bob**

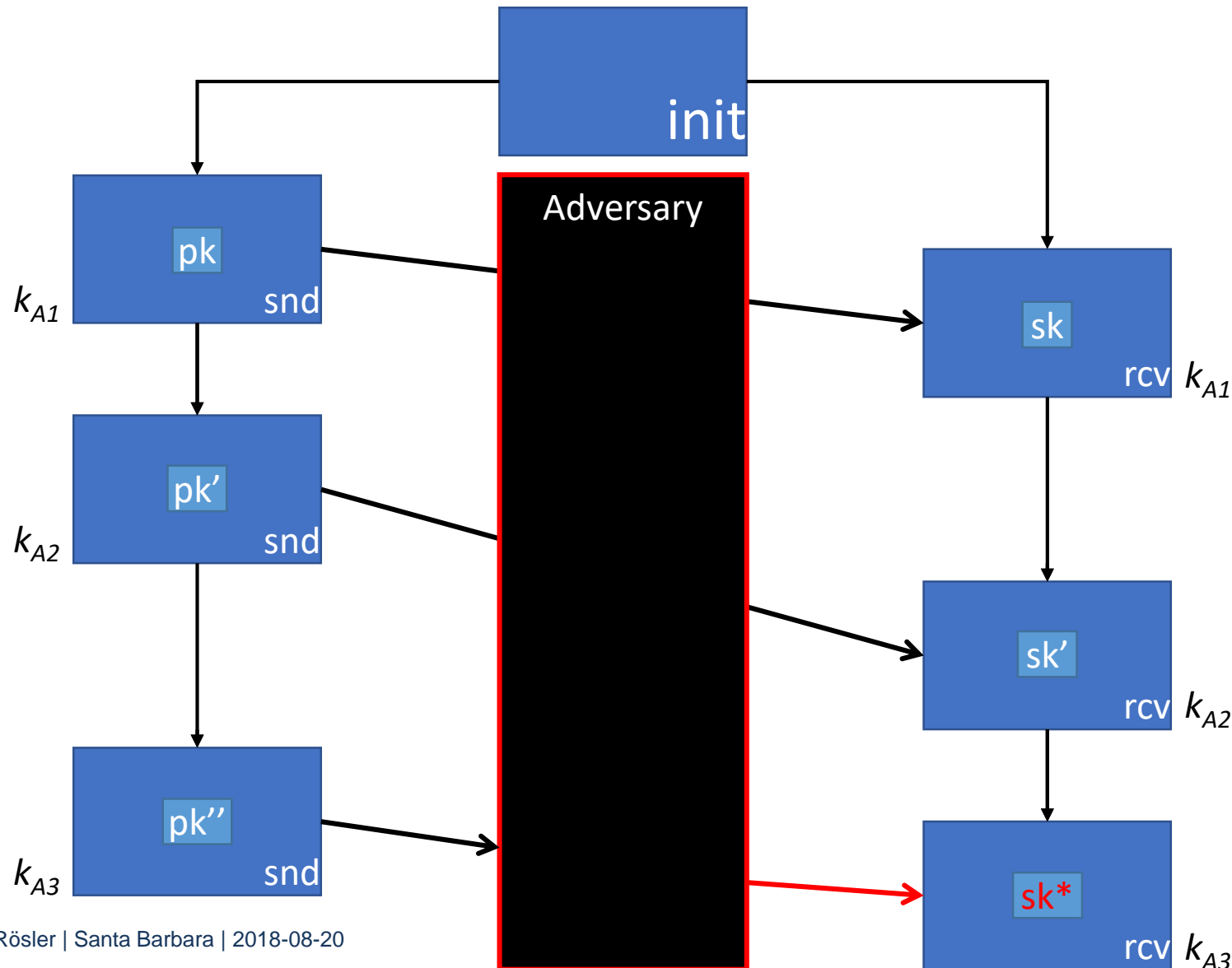
⇒ **No future Challenge if synchronous**

→ Forward secrecy of Bob's state

→ Divergence of states

→ Random oracle:

$$\text{H}(\text{c} \text{ k}) \rightarrow k_{xn} \text{ sk}$$



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→ KEM:

$$\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \text{ k} \quad \text{dec}(\text{sk} \text{ c}) \rightarrow_{\xi} \text{k}$$

- Expose Bob**

⇒ **No future Challenge if synchronous**

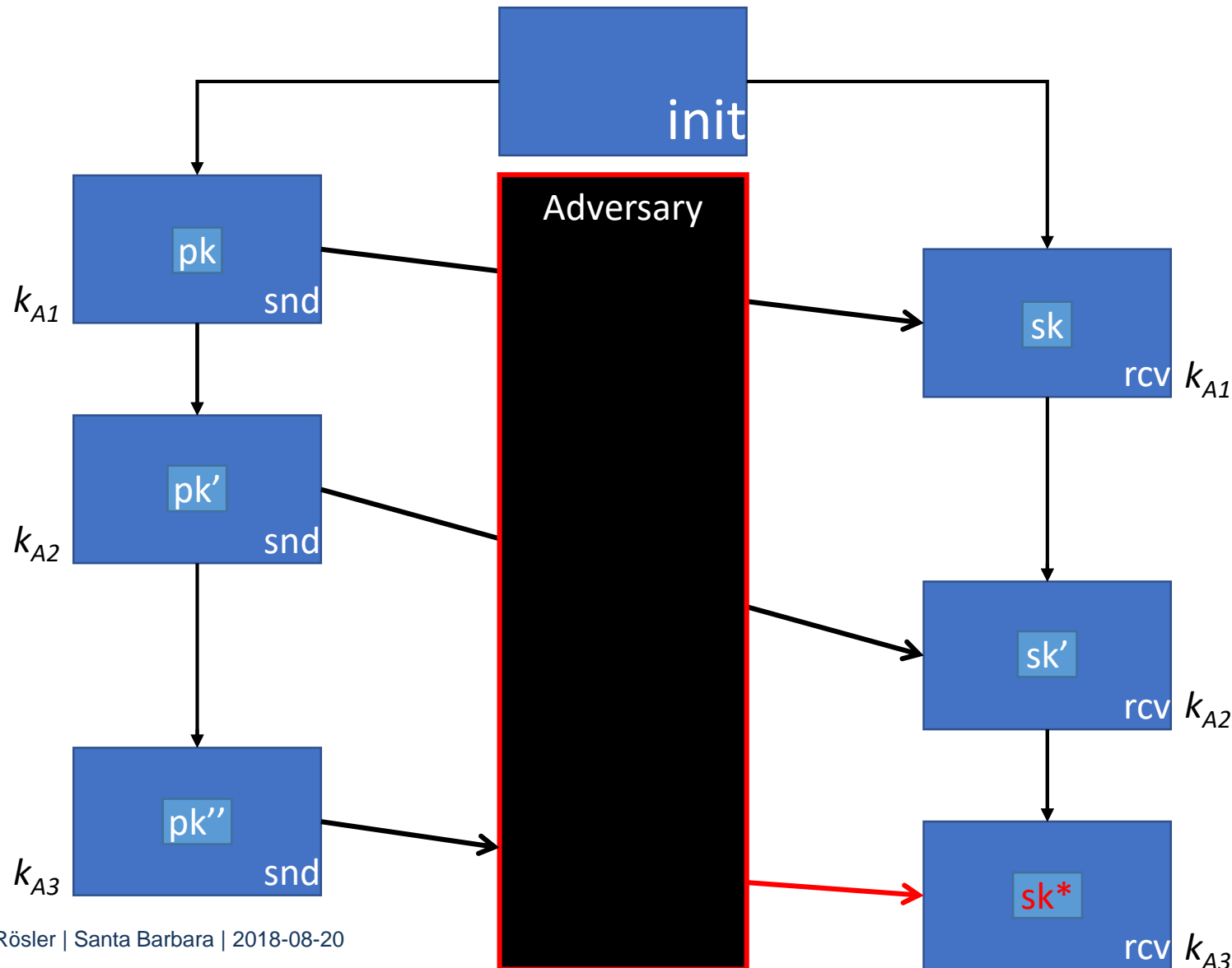
→ Forward secrecy of Bob's state

→ Divergence of states

→ Random oracle:

$$\text{H}(\text{c} \text{ k}) \rightarrow k_{xn} \text{ sk}$$

$$\text{gen}(\text{sk}) \rightarrow \text{pk}$$



Constructing Unidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Alice okay**

→ KEM:

$$\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \text{ k} \quad \text{dec}(\text{sk} \text{ c}) \rightarrow_{\xi} \text{k}$$

- Expose Bob**

⇒ **No future Challenge if synchronous**

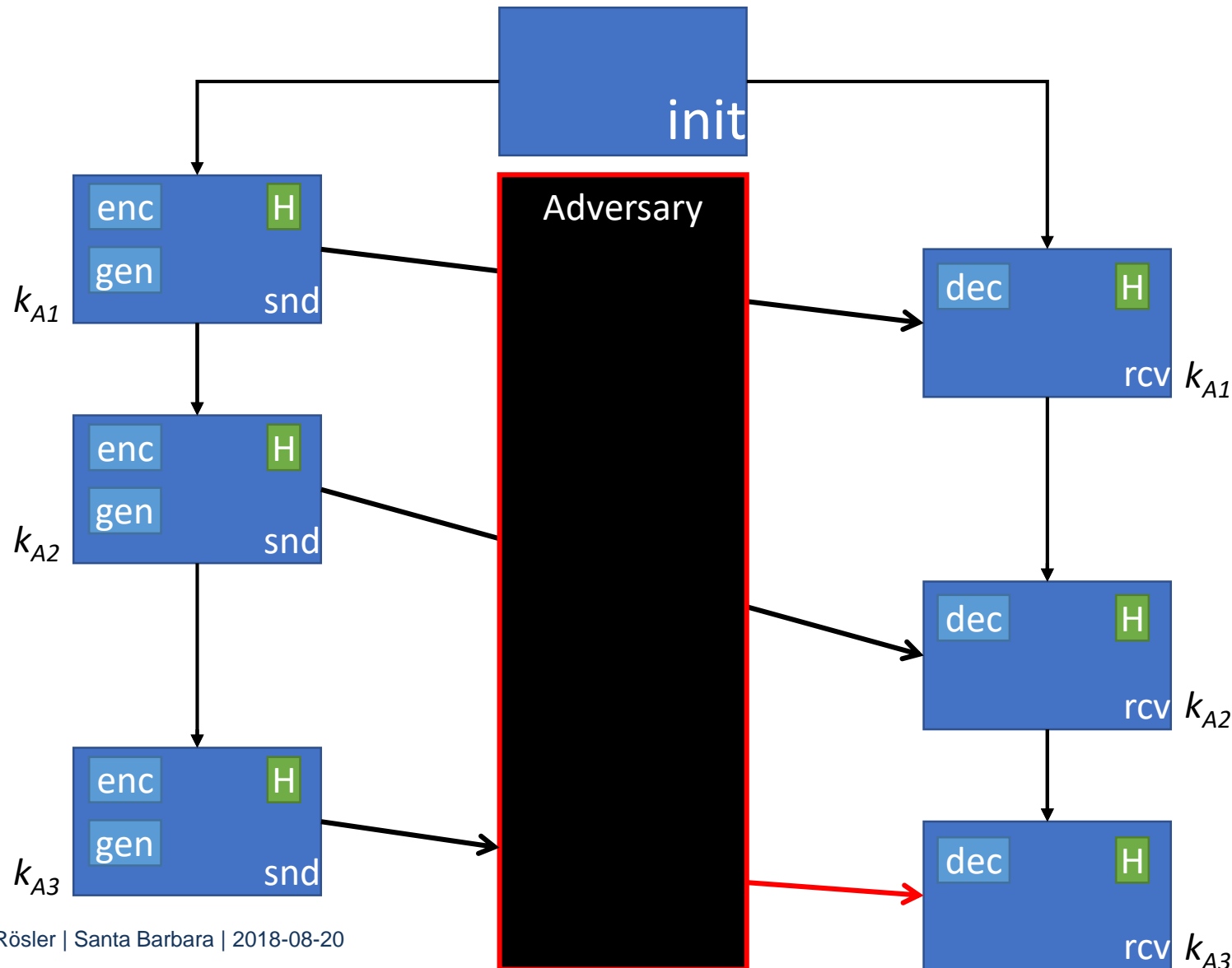
→ Forward secrecy of Bob's state

→ Divergence of states

→ Random oracle:

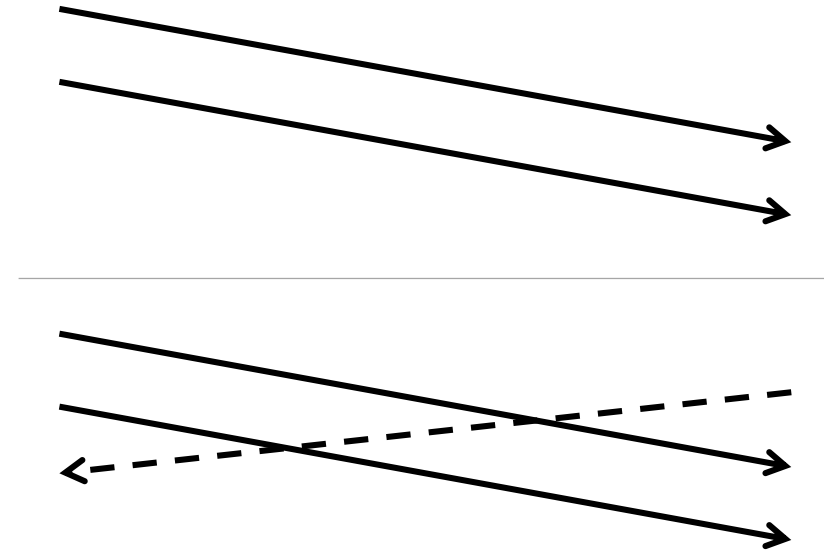
$$\text{H}(\text{c} \text{ k}) \rightarrow k_{xn} \text{ sk}$$

$$\text{gen}(\text{sk}) \rightarrow \text{pk}$$



Agenda

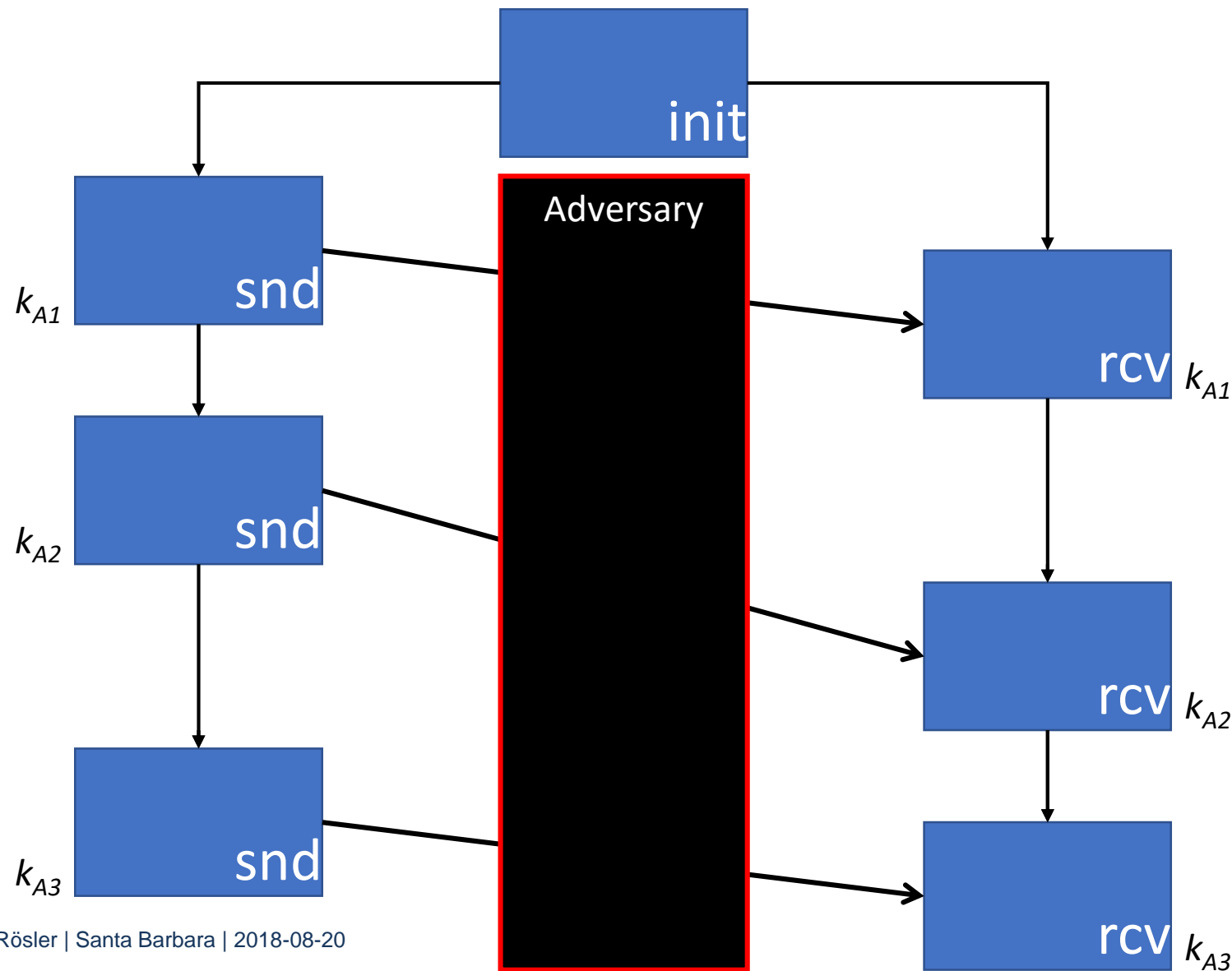
1. The Primitive Ratcheted Key Exchange
2. General Adversary Model
3. Unidirectional Ratcheting
→ Model and Construction
4. **Sesquidirectional Ratcheting**
→ **Model** and Construction
5. Results



Modeling Unidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

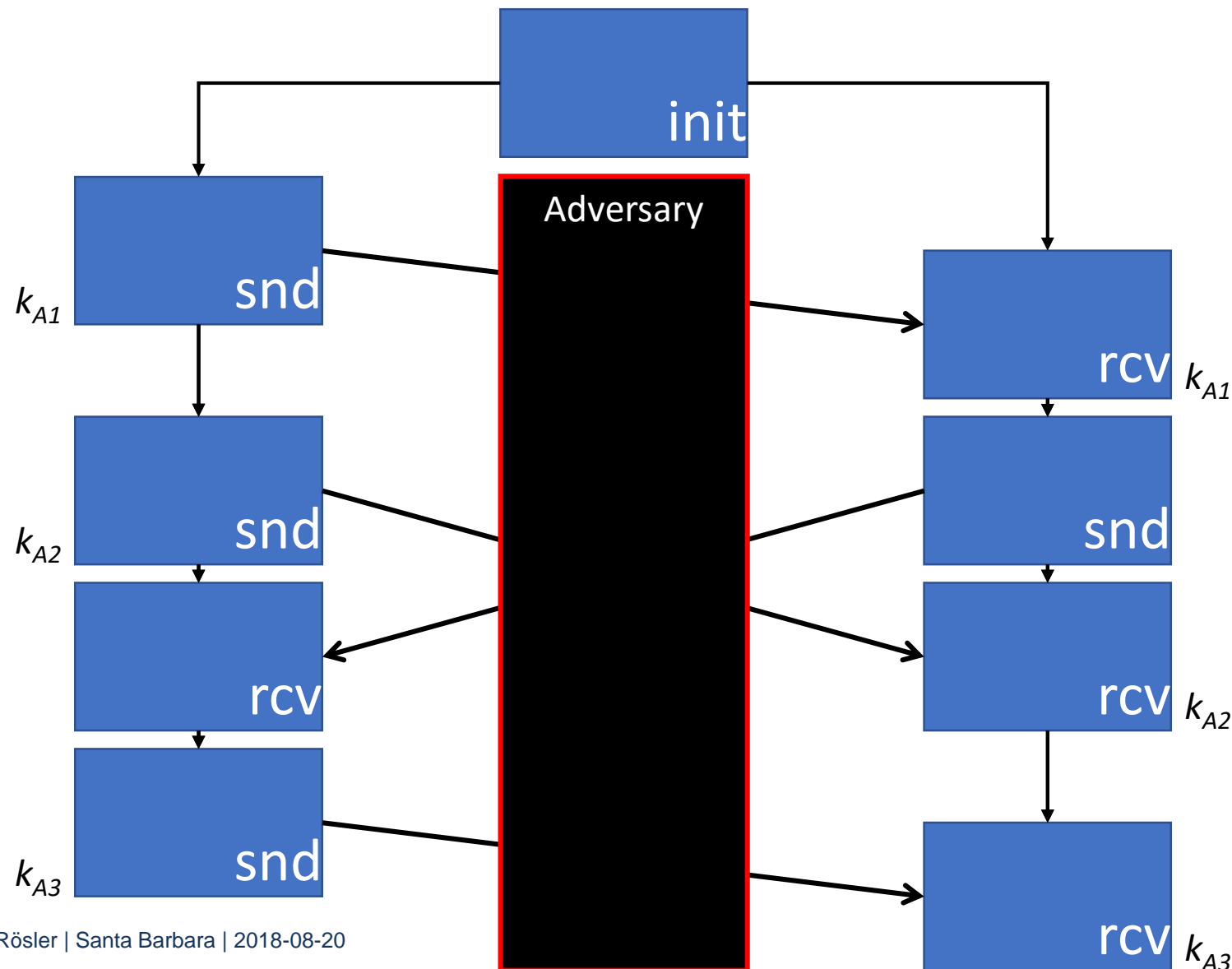
- Impersonation $A \rightarrow B$
 \Rightarrow No future Challenge on Bob
- Expose Bob
 \Rightarrow No future Challenge if synchronous



Modeling Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

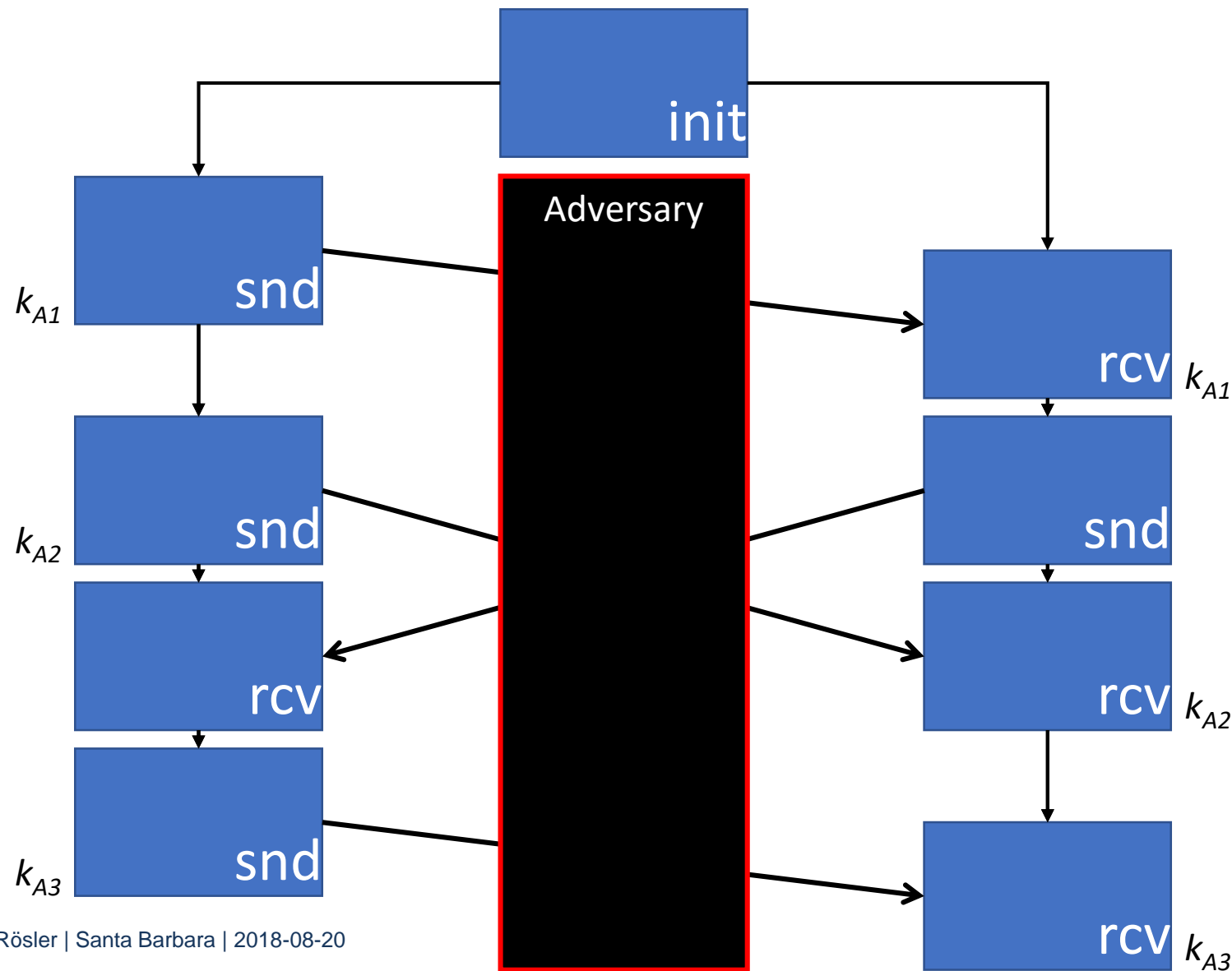
- Impersonation $A \rightarrow B$
 \Rightarrow No future Challenge on Bob
- Expose Bob
 \Rightarrow No future Challenge if synchronous



Modeling Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

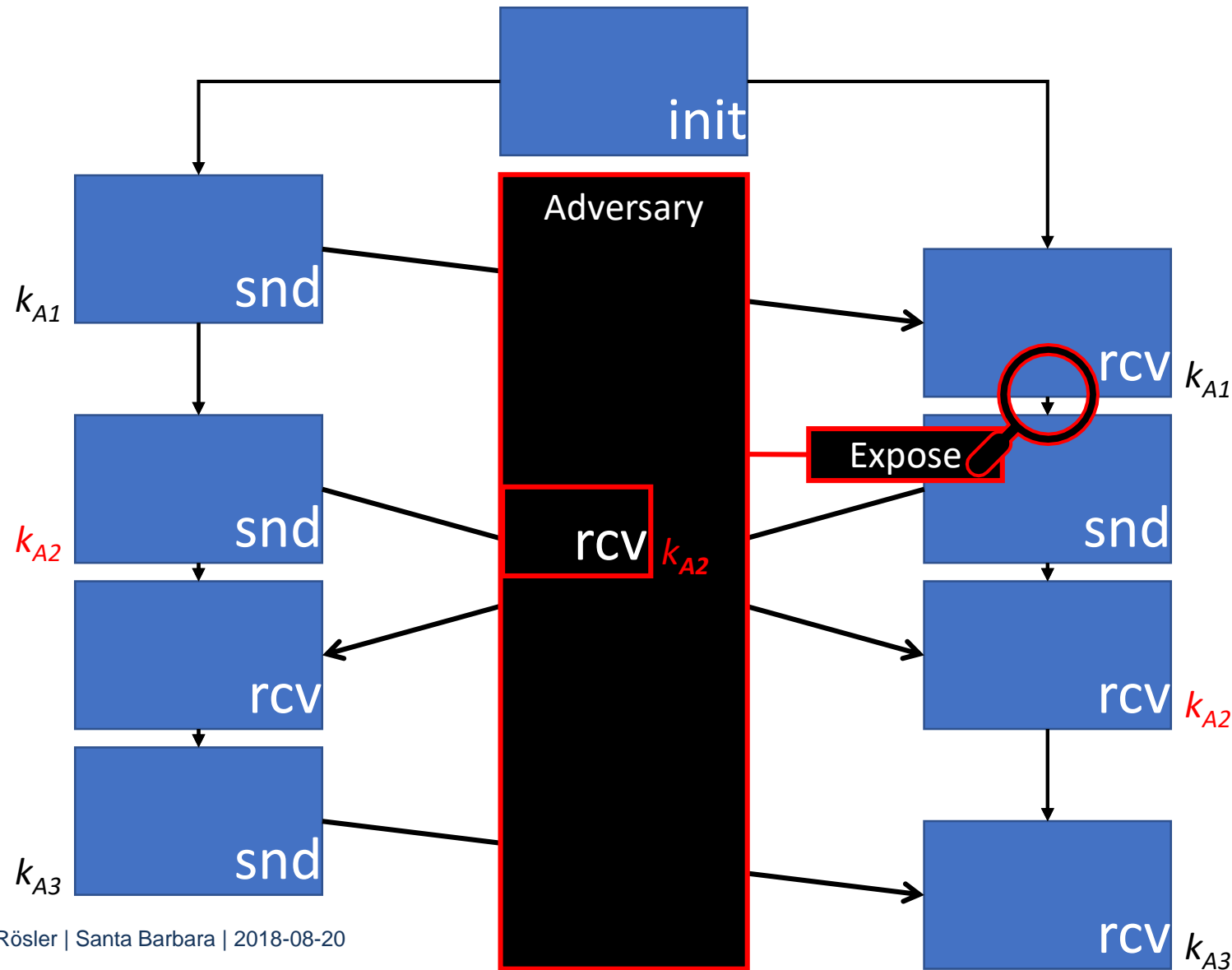
- Impersonation $A \rightarrow B$
 \Rightarrow No future Challenge on Bob
- Impersonation $B \rightarrow A$
 \Rightarrow No future Challenge on Alice
- Expose Bob
 \Rightarrow No future Challenge if synchronous



Modeling Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

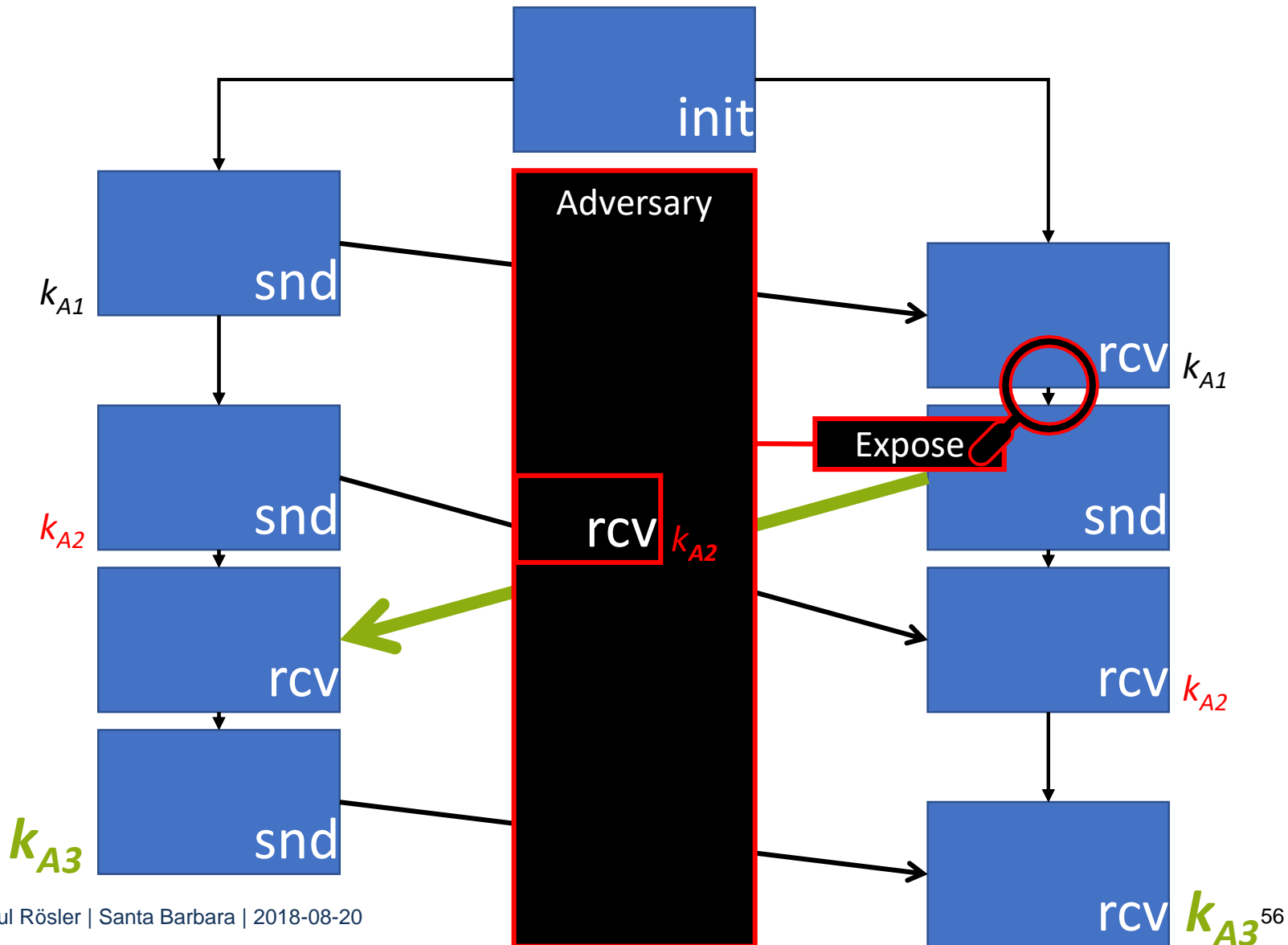
- Impersonation $A \rightarrow B$
 \Rightarrow No future Challenge on Bob
- Impersonation $B \rightarrow A$
 \Rightarrow No future Challenge on Alice
- Expose Bob
 \Rightarrow No future Challenge if synchronous
until Bob recovered



Modeling Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

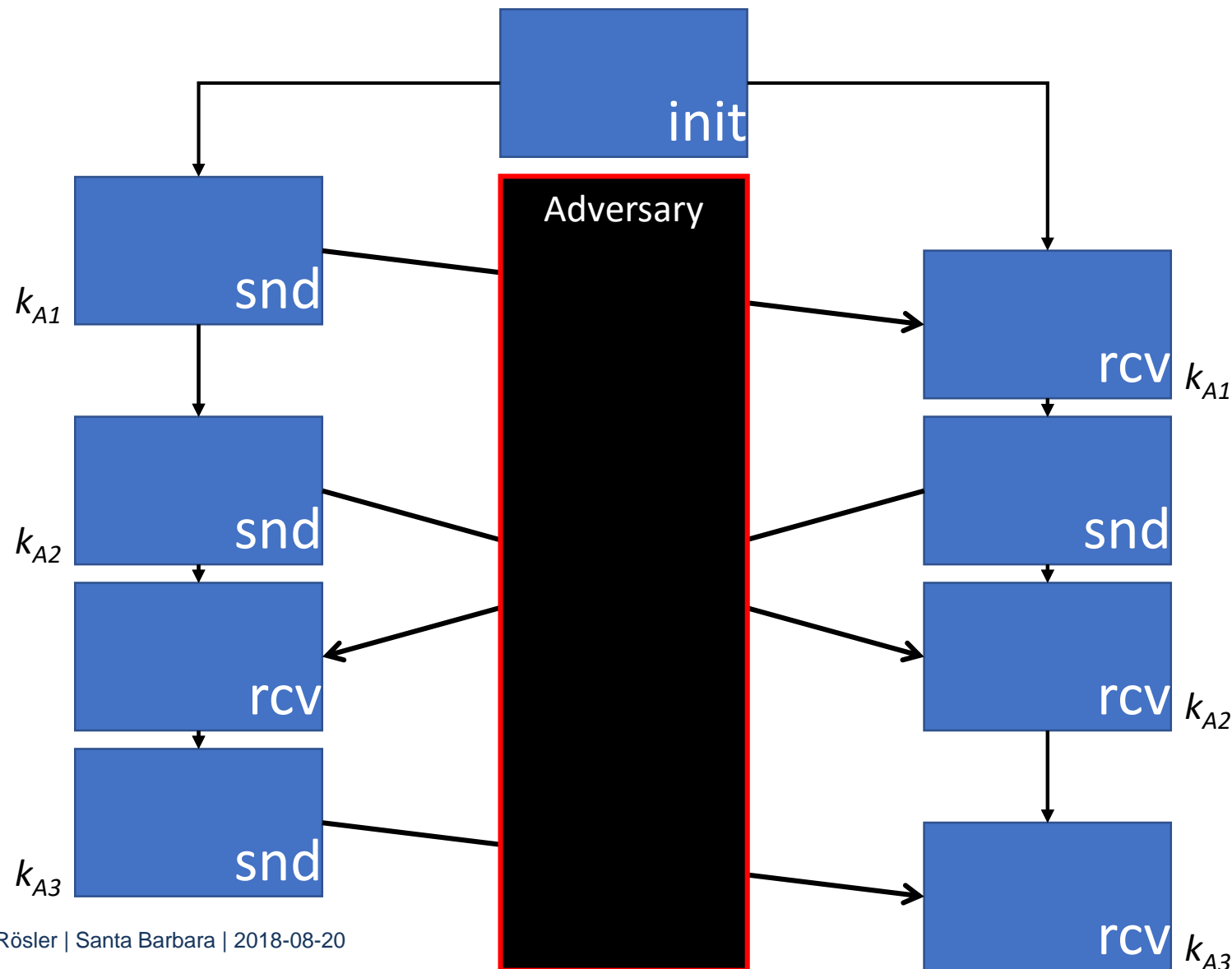
- Impersonation $A \rightarrow B$
 \Rightarrow No future Challenge on Bob
- Impersonation $B \rightarrow A$
 \Rightarrow No future Challenge on Alice
- Expose Bob
 \Rightarrow No future Challenge if synchronous
until Bob recovered



Modeling Sesquidirectional RKE

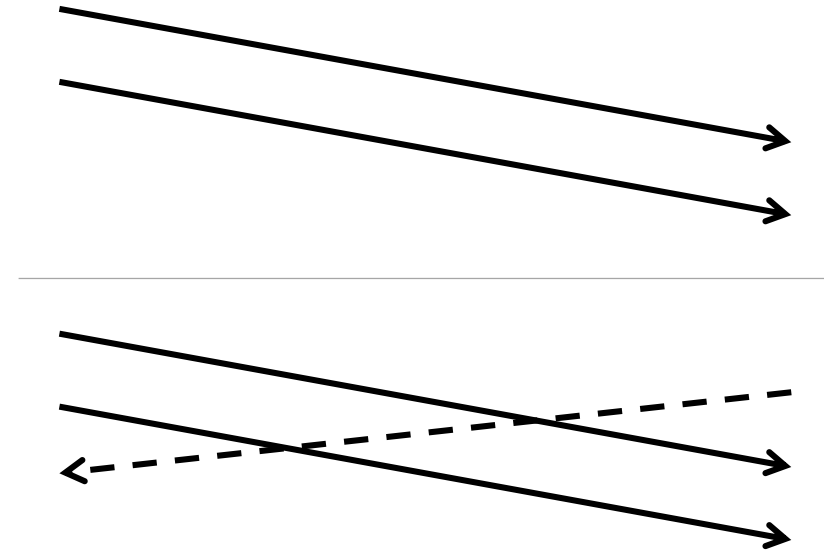
- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Impersonation $A \rightarrow B$
 \Rightarrow No future Challenge on Bob
- Impersonation $B \rightarrow A$
 \Rightarrow No future Challenge on Alice
- **Expose Bob**
 \Rightarrow **No future Challenge if synchronous until Bob recovered**



Agenda

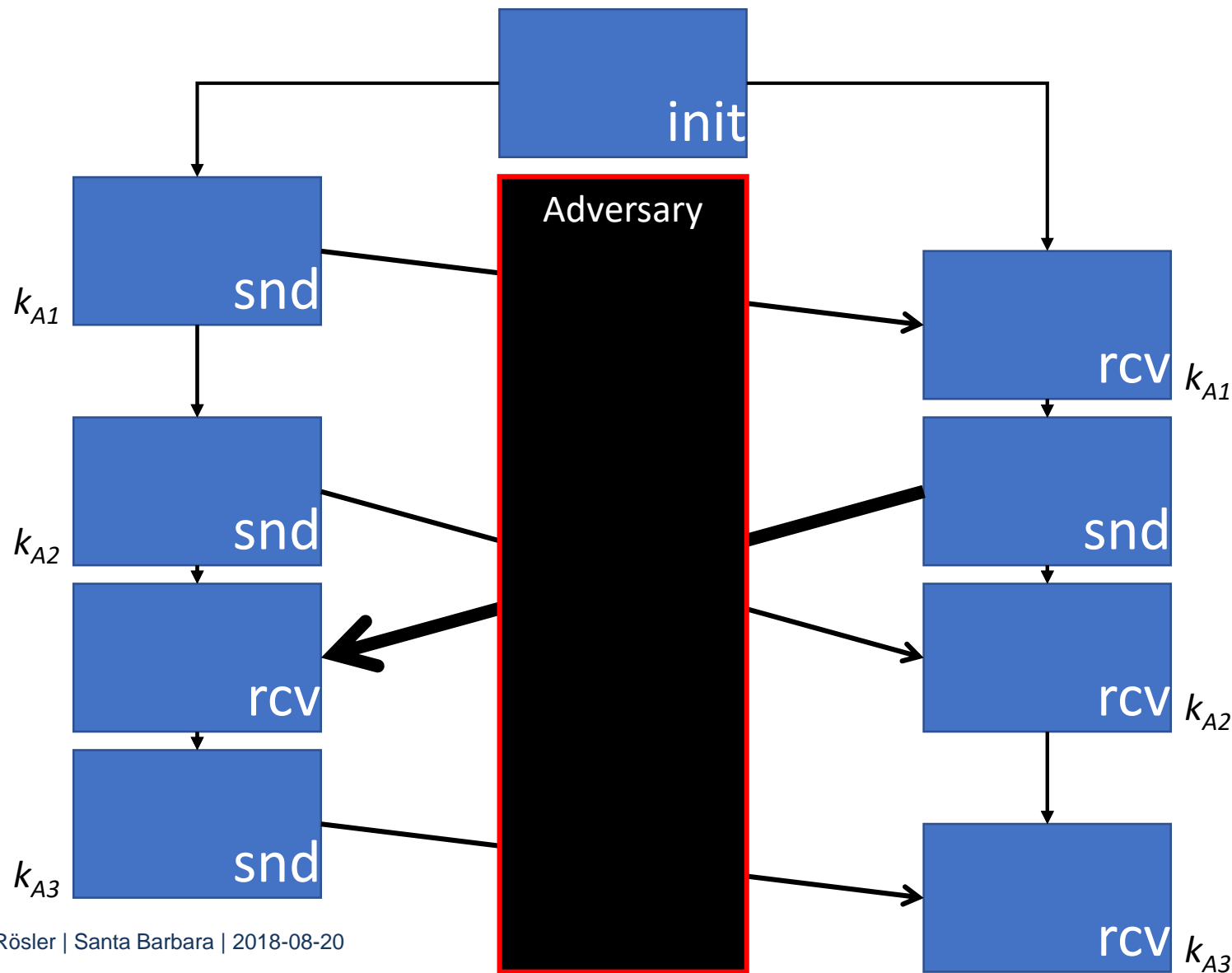
1. The Primitive Ratcheted Key Exchange
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3. Unidirectional Ratcheting
→ Model and Construction
4. **Sesquidirectional Ratcheting**
→ Model and **Construction**
5. Results



Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

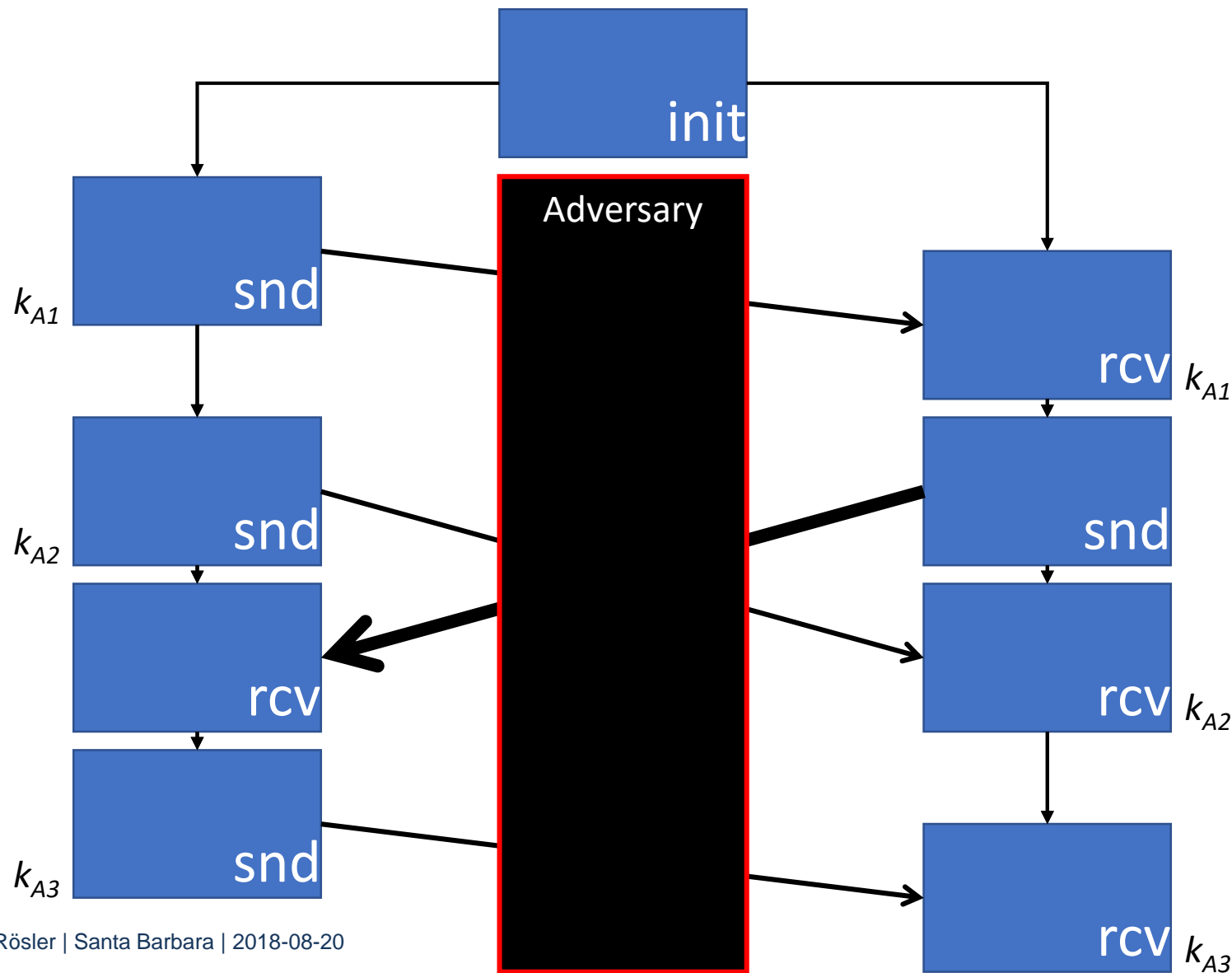
- **Expose Bob**
 ⇒ **No future Challenge**
if synchronous
until Bob recovered



Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

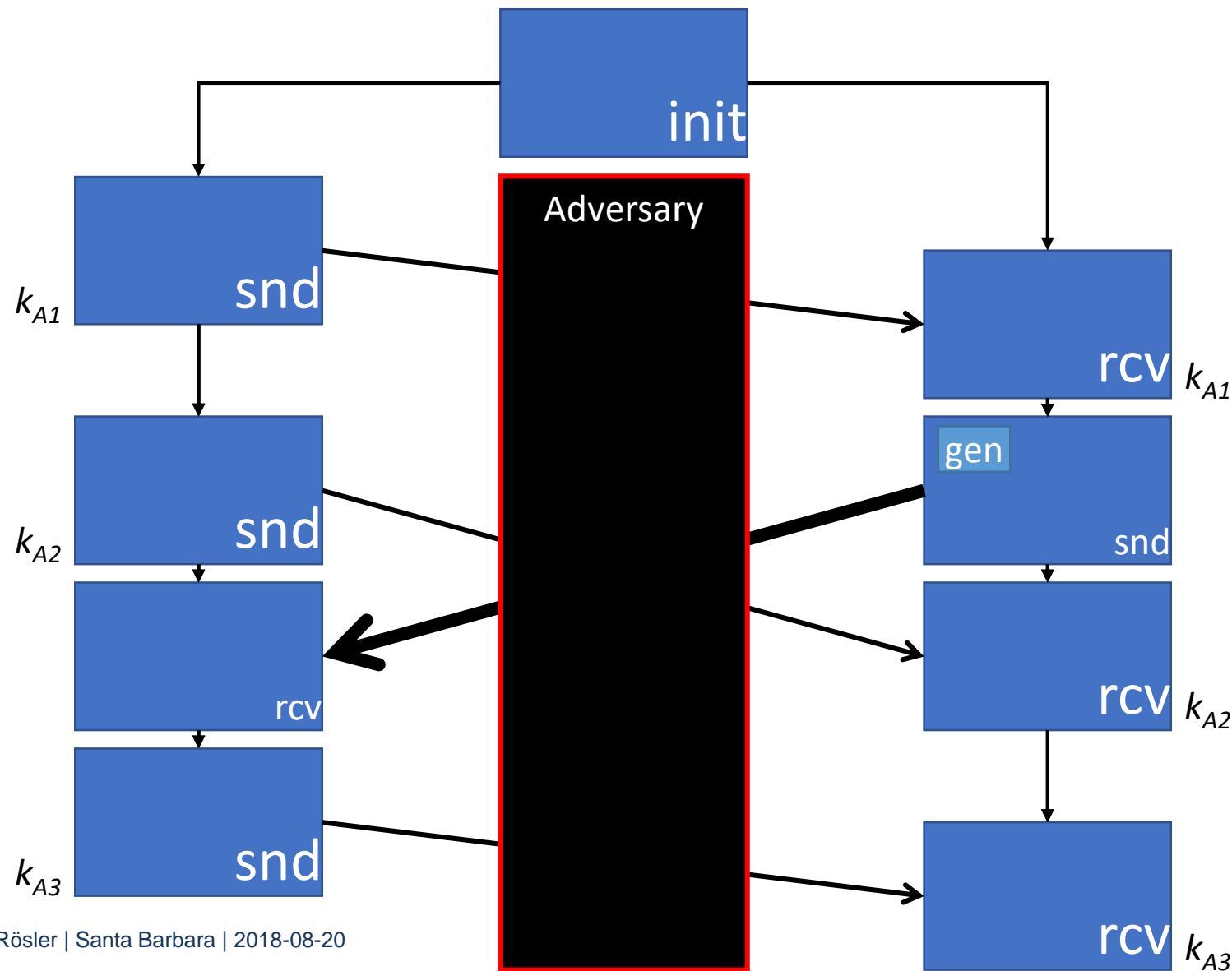
- **Expose Bob**
 ⇒ **No future Challenge if synchronous until Bob recovered**
 → Forward secrecy and recovery of Bob's state



Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

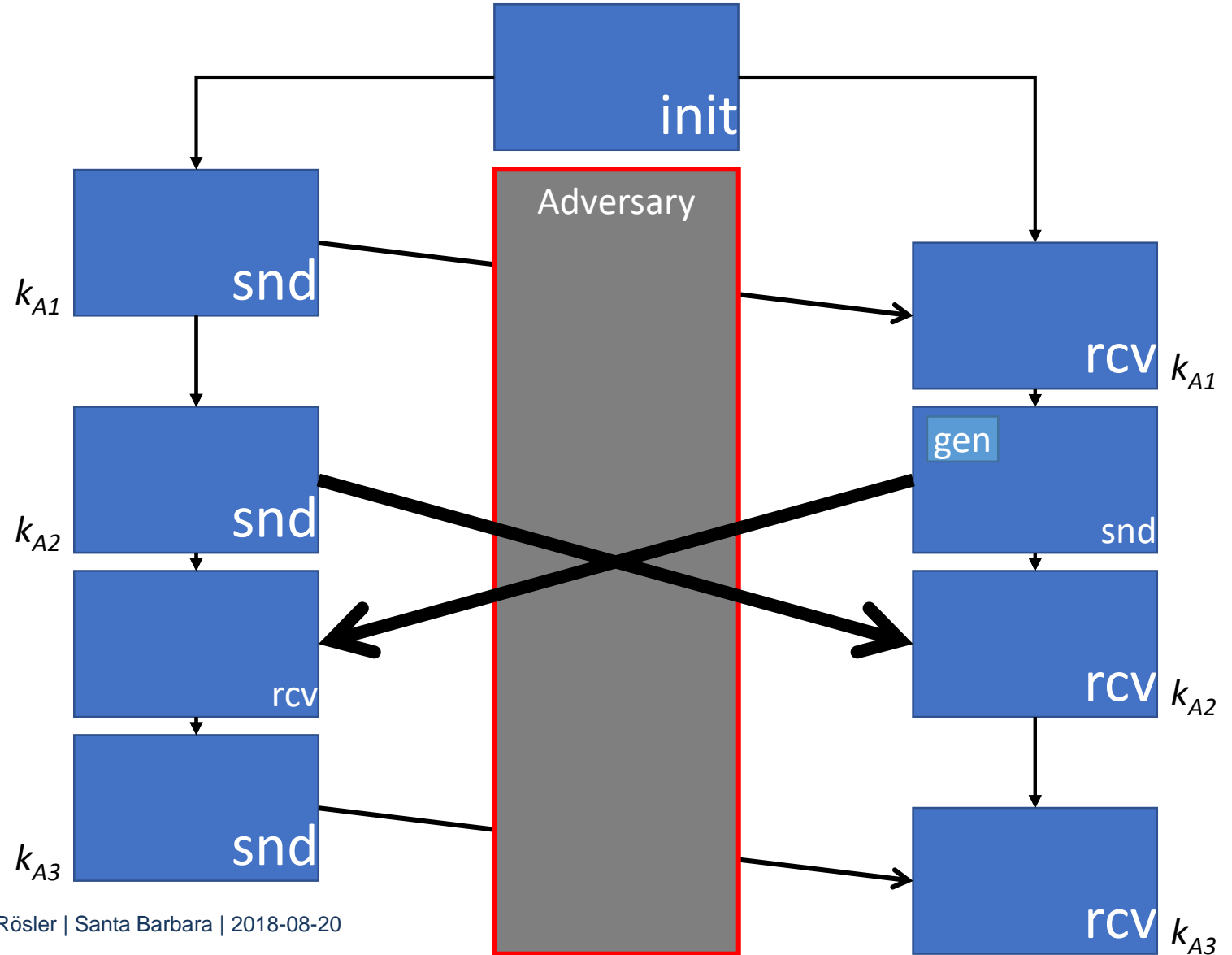
- Expose Bob
 - ⇒ No future Challenge if synchronous until Bob recovered
 - Forward secrecy and recovery of Bob's state
 - Send new **pk**



Constructing Sesquidirectional RKE

- What is Ratcheting?
Modeling RKE
- Construction Intuition
Results

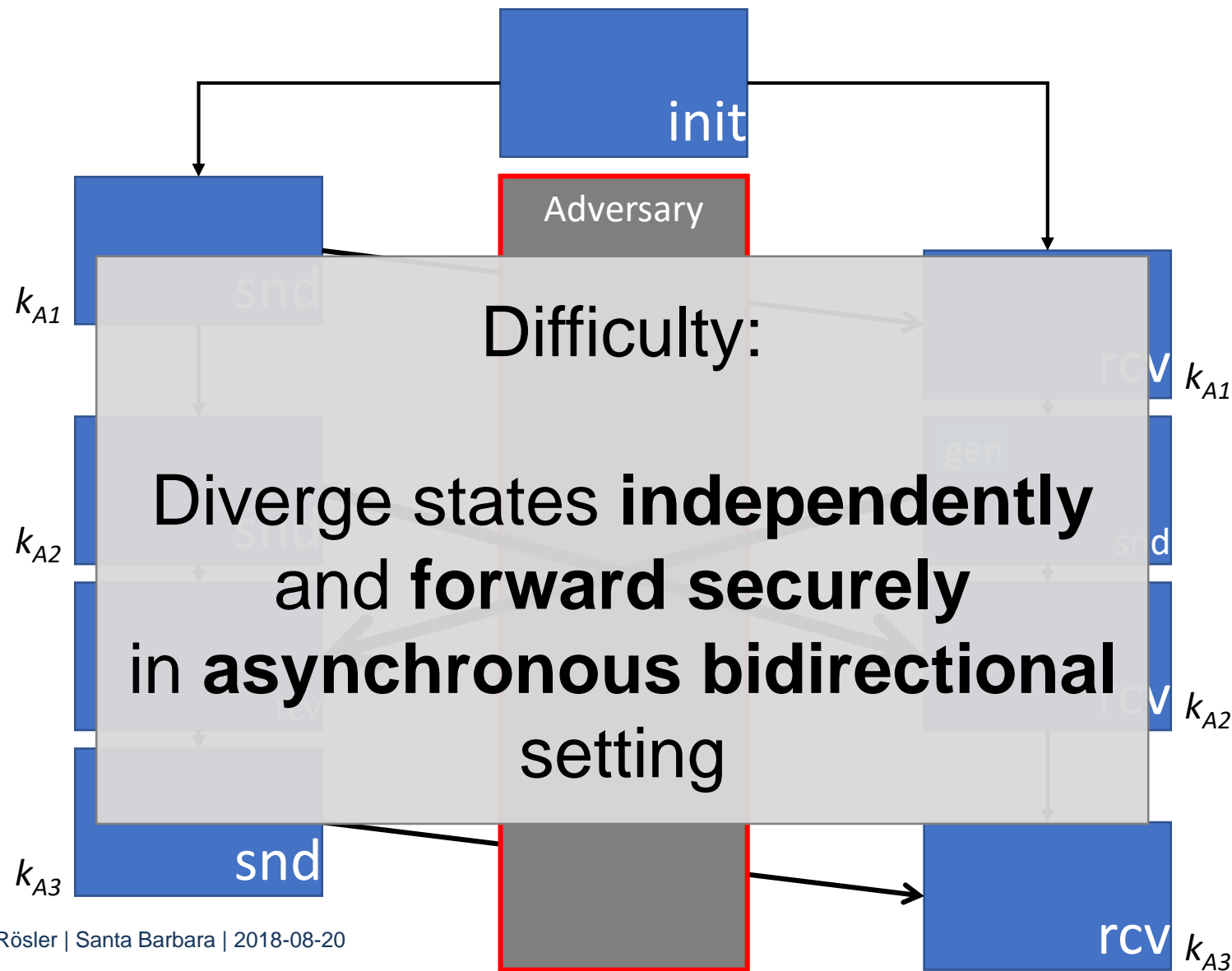
- **Expose Bob**
⇒ **No future Challenge**
if synchronous
until Bob recovered
→ Forward secrecy
and recovery
of Bob's state
→ Send new **pk**
→ Divergence of states



Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

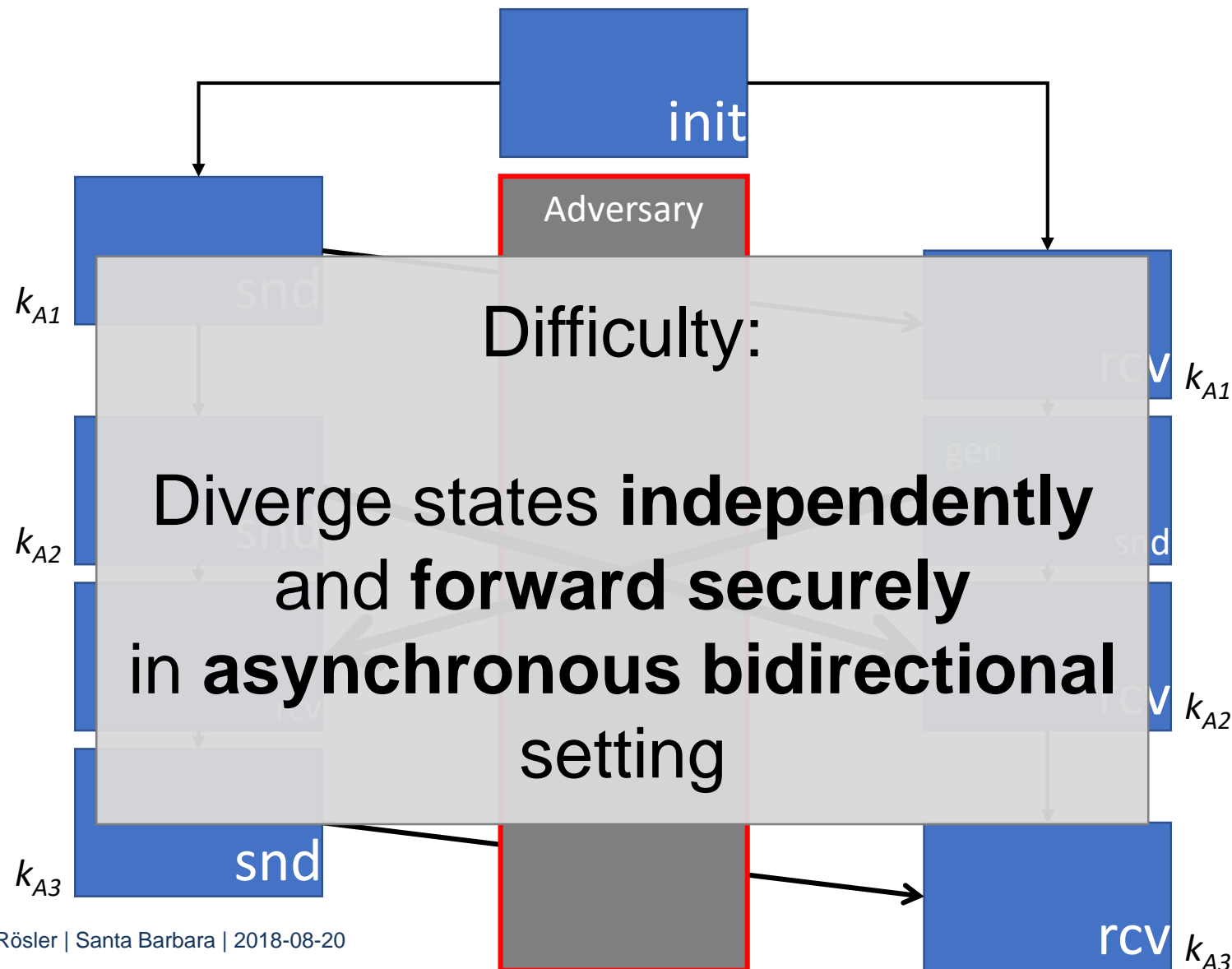
- Expose Bob
 - ⇒ No future Challenge if synchronous until Bob recovered
 - Forward secrecy and recovery of Bob's state
 - Send new **pk**
 - Divergence of states



Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Bob
 - ⇒ No future Challenge if synchronous until Bob recovered
 - Forward secrecy and recovery of Bob's state
 - Send new **pk**
 - Divergence of states
 - Update key pair



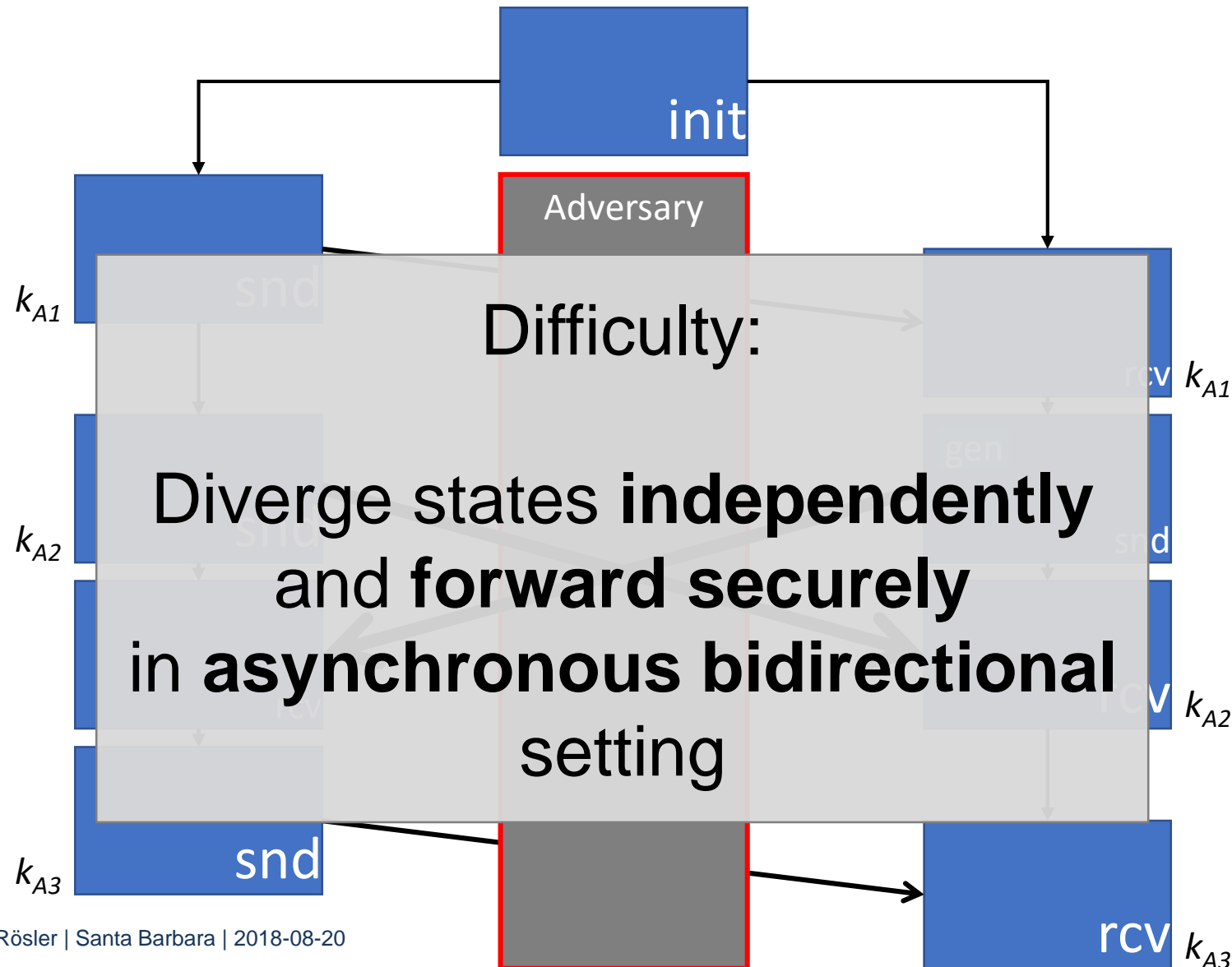
Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Bob
 - ⇒ No future Challenge if synchronous until Bob recovered
 - Forward secrecy and recovery of Bob's state
 - Send new **pk**
 - Divergence of states
 - Update key pair

up (**sk**, \mathcal{T}) → **sk**

up (**pk**, \mathcal{T}) → **pk**



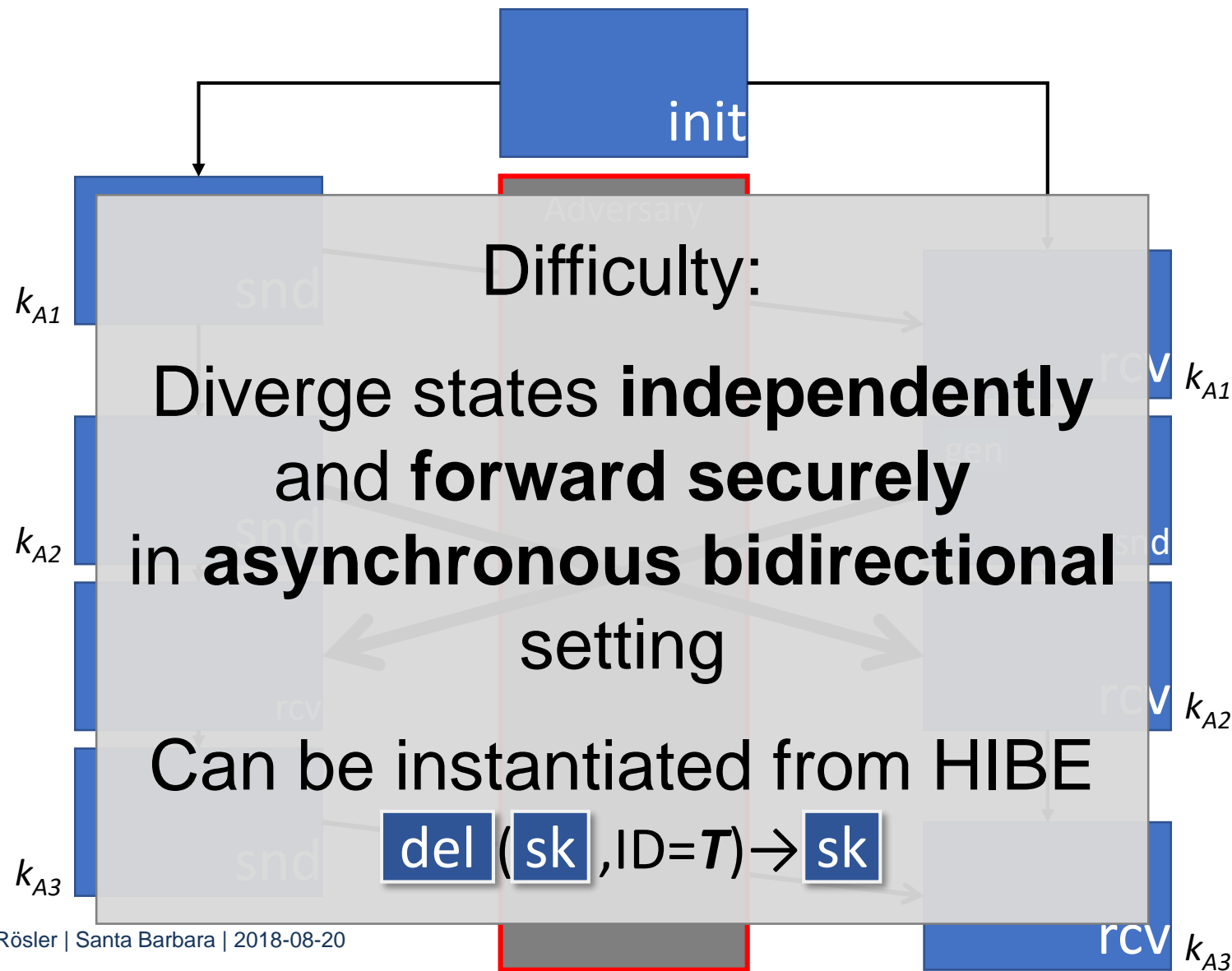
Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
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- Results

- Expose Bob
 - ⇒ No future Challenge if synchronous until Bob recovered
 - Forward secrecy and recovery of Bob's state
 - Send new **pk**
 - Divergence of states
 - Update key pair

up (**sk**, T) → **sk**

up (**pk**, T) → **pk**



Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
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- Results

- Expose Bob
- ⇒ No future Challenge if synchronous until Bob recovered

→ Forward secrecy and recovery of Bob's state

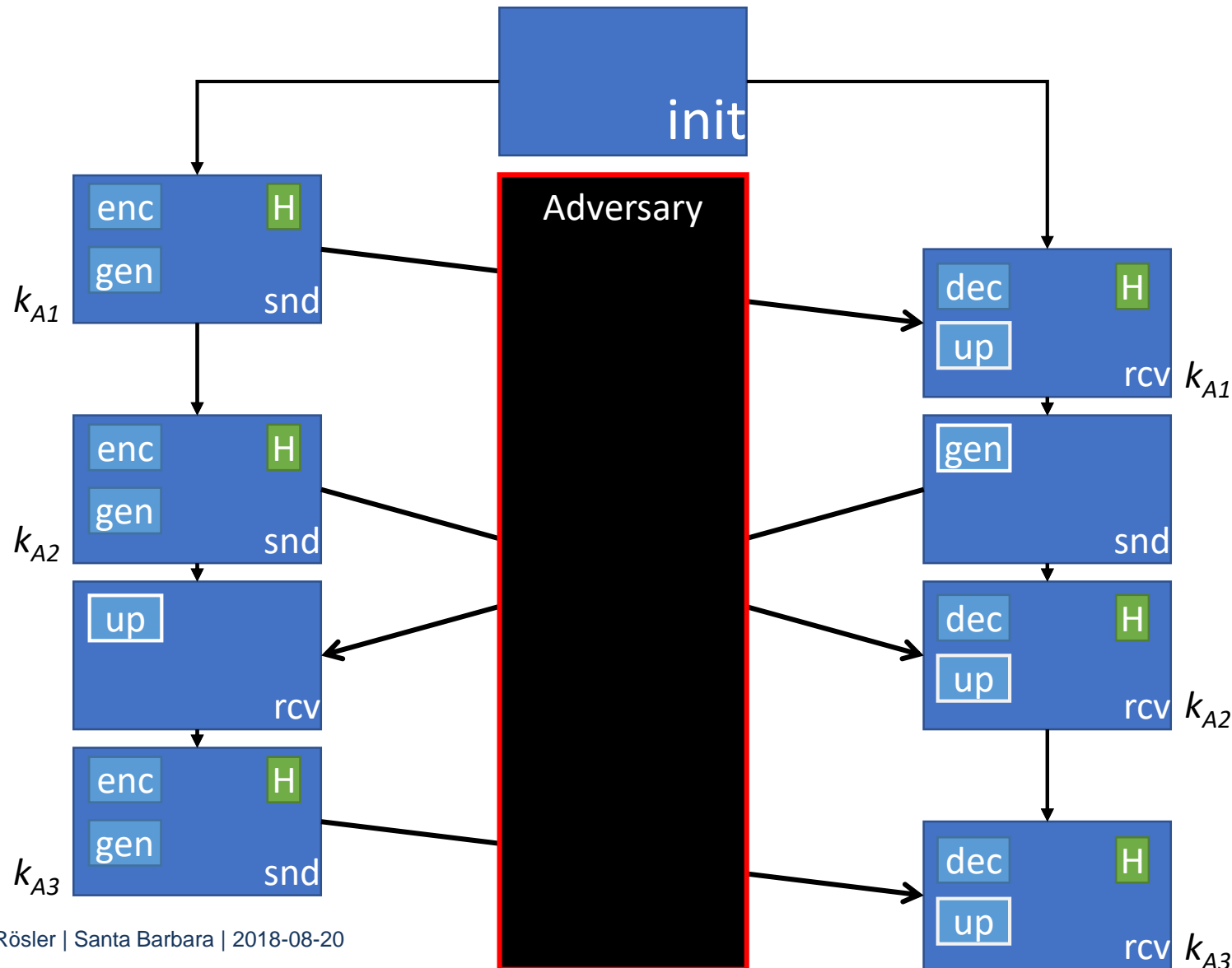
→ Send new **pk**

→ Divergence of states

→ Update key pair

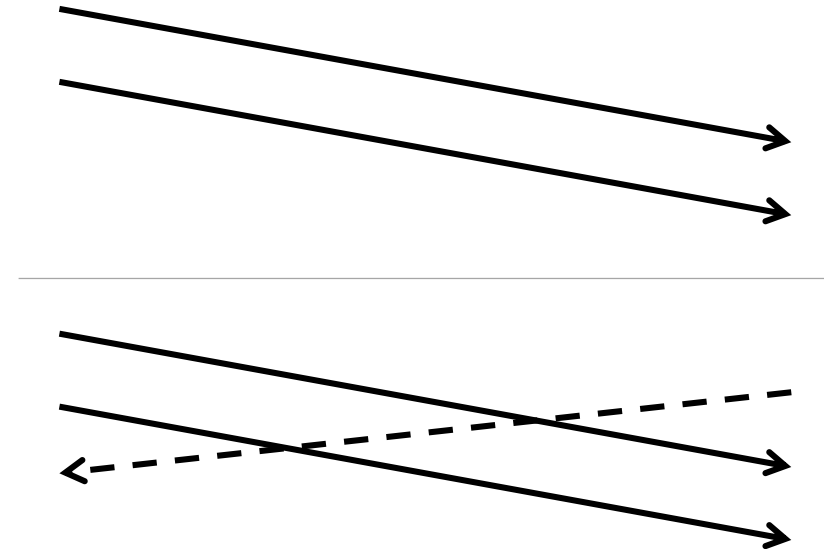
up (sk, T) → sk

up (pk, T) → pk



Agenda

1. The Primitive Ratcheted Key Exchange
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3. Unidirectional Ratcheting
→ Model and Construction
4. Sesquidirectional Ratcheting
→ Model and Construction
- 5. Results**



Results

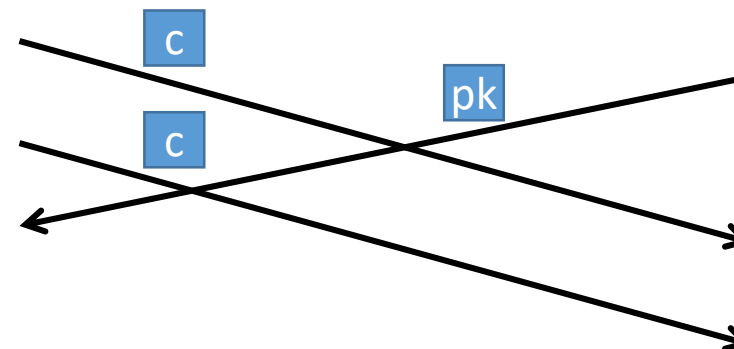
- Unidirectional RKE
 - KEM + ROM (+ MAC)

ia.cr/2018/296 (ext. version)

@roeslpa

Results

- Unidirectional RKE
 - KEM + ROM (+ MAC)
- Sesquidirectional RKE
 - Key updatable KEM (+ signatures)
 - # `up` (`sk` \mathcal{T}) = # *crossing* ciphertexts
→ Depth of HIBE practically bounded

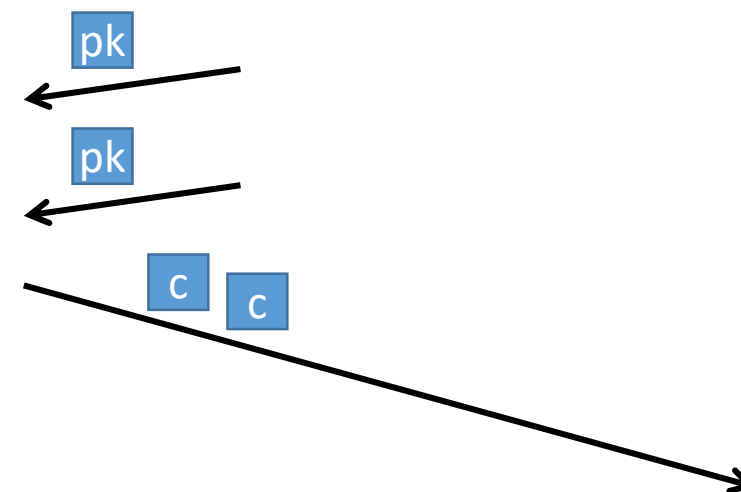


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Results

- Unidirectional RKE
 - KEM + ROM (+ MAC)
- Sesquidirectional RKE
 - Key updatable KEM (+ signatures)
 - # `up` (`sk` \mathcal{T}) = # *crossing* ciphertexts
 - Depth of HIBE practically bounded
 - Multi encapsulation
 - Bounded in ping-pong pattern
 - Alternative: key updatable signatures

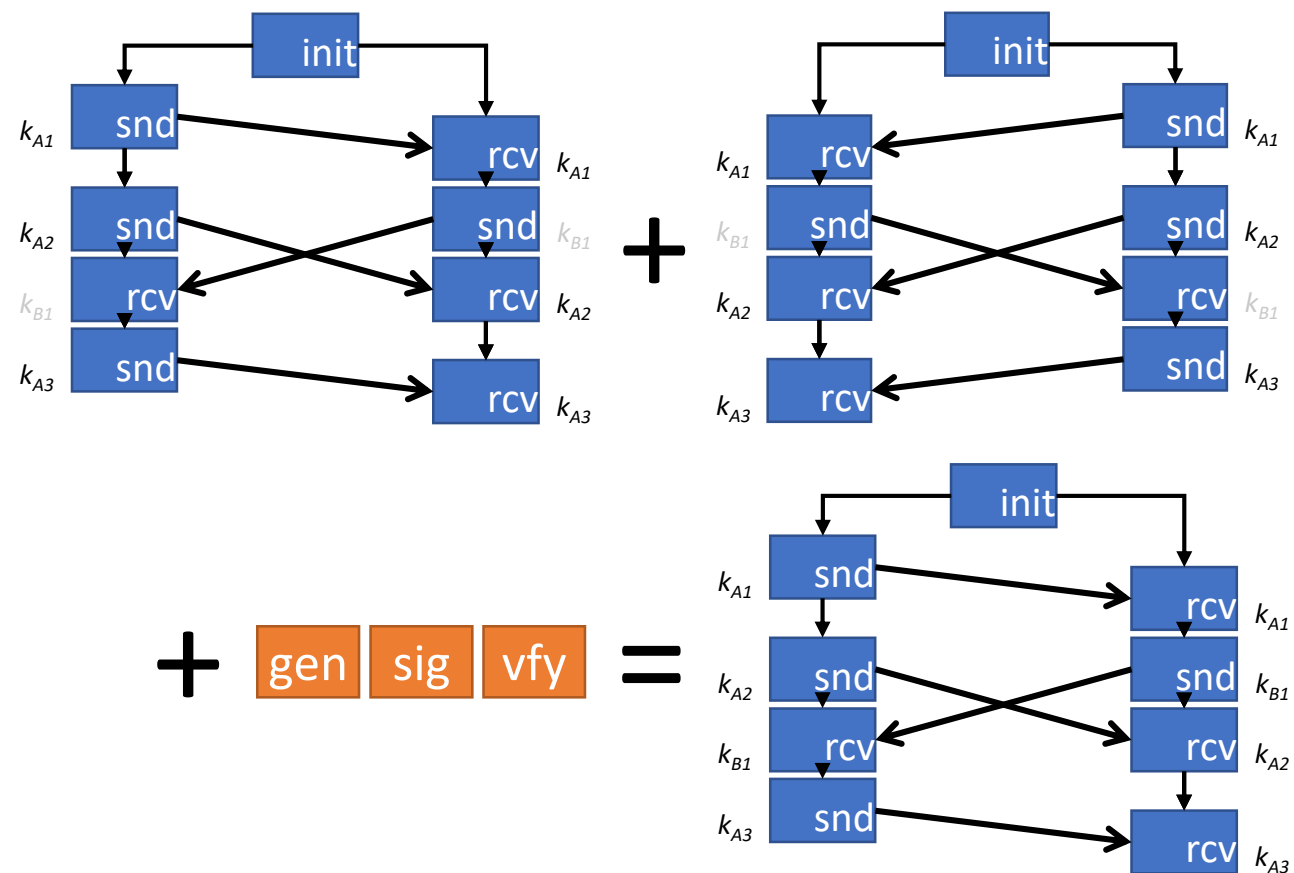


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Results

- Unidirectional RKE
 - KEM + ROM (+ MAC)
- Sesquidirectional RKE
 - Key updatable KEM (+ signatures)
 - # `up` (`sk` T) = #crossing ciphertexts
 - Depth of HIBE practically bounded
 - Multi encapsulation
 - Bounded in ping-pong pattern
 - Alternative: key updatable signatures
- BRKE = 2x SRKE + OT signatures
 - Build SRKE, BRKE too complex!



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